



Compliant Actuation Technologies for Emerging Humanoids

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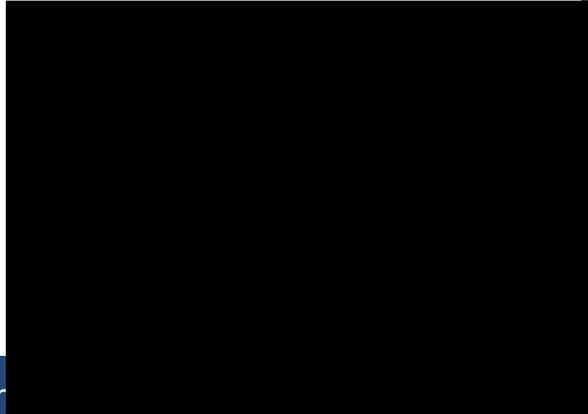
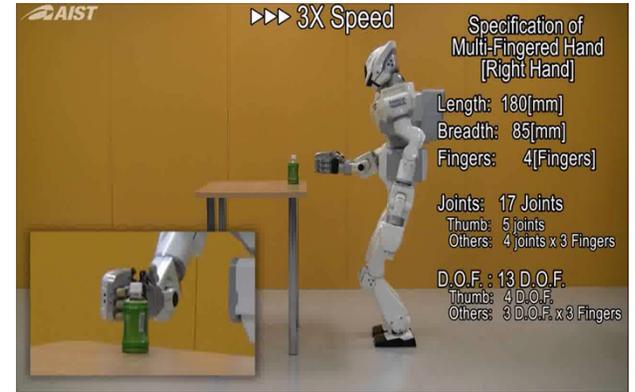
- Classical robotics actuation
 - Pros and cons
- Compliant actuators
 - Series elastic actuators (SEA)
 - CompAct unit and compliant humanoid COMAN
 - Variable stiffness actuation (VSAs)
- Variable damping actuation
 - the Variable physical damping actuator VPDA
 - CompAct manipulator

Robot soccer state

- relative slow motions
- absence of fast/high power motions
- always in static balancing
- physical game is missing
 - body to body physical interaction
 - dynamic balancing against strong disturbances
 - impacts with ground and other bodies can damage the robots



Humanoid SoA



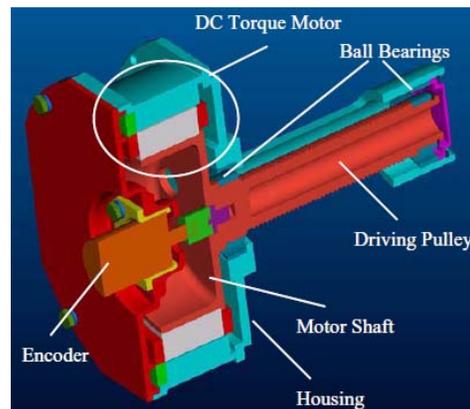
Robotics actuation (motorized)

- Direct drive actuation
- Geared actuators
 - Motor + reduction gearheads
 - Motor + low-friction cable /belt drive transmissions

Direct drive actuation

a high quality servomotor directly connected to the load

- Pros
 - the torque output can be accurately controlled through motor current regulation
 - robust against impacts
- Cons
 - servomotors operate inefficiently at low speeds and high torques
 - the power of direct drive servomotors is selected to be much higher than the actual useful power output
 - they are typically too large and heavy



Frisoli et al, 2005

a servomotor combined with a gearhead

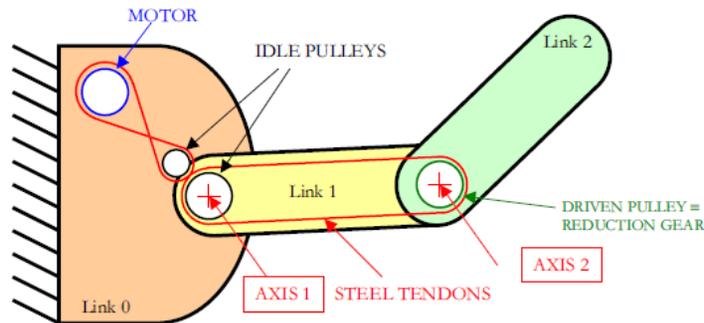
- Pros
 - motor operates in a more efficient spot (high speed/low torque) while driving a low speed/high torque trajectory
 - for low reduction ratio, current control can then be still applied to the geared actuator to control force output



- Cons
 - introduces significant friction
 - friction can become essentially high in some types of non-backdriveable gears
 - increases the reflected inertia at the output of the gearbox
 - large output mechanical impedance
 - non-linear, non-continuous dynamics such as stiction and backlash
 - force control through current regulation is unsuitable as it will result in extremely poor force fidelity
 - weak under impacts

a servomotor combined with a cable drive transmission

- Pros
 - cable drive transmissions, have low stiction and low backlash.
 - can be approximated by linear dynamics allowing to model the transmission and compensate for its effects
- Cons
 - only low to moderate ratios can be implemented
 - high ratios requiring large pulleys and multi-stages which need large space
 - More complex assembly with many pulleys requiring the fixation and pretension of cables



Frisoli et al, 2005

Humanoid actuation

- **Features**

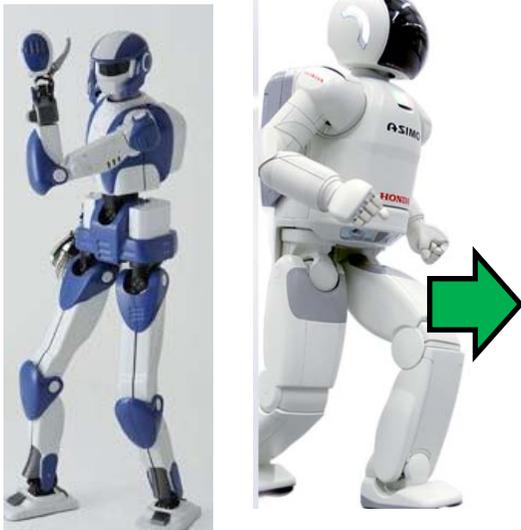
- DC brush or brushless motors combined with planetary or harmonic drive gears
 - relative high gearing position control groups (>100:1)
 - limited back-drivability
 - stiff Position / velocity servo loops
- minimum passive compliance (mostly from tendons)
- no direct joint torque sensing

- **Advantages**

- high disturbance rejection
- accuracy and repeatability

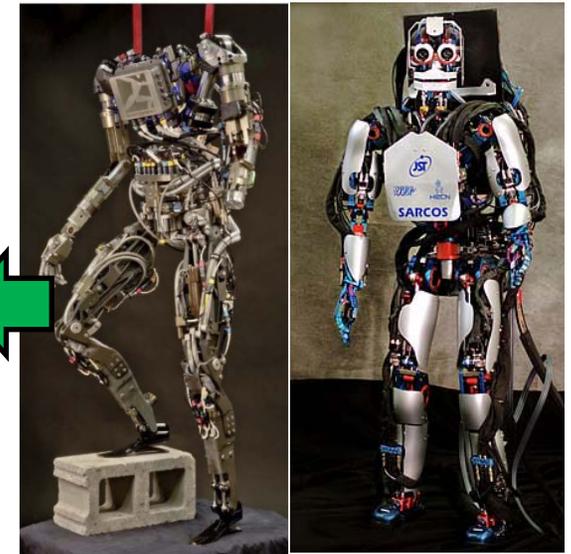
Humanoid actuation

Electrical



Stiff actuation for accuracy
+
Active compliance regulation

Hydraulic



The need of compliance

- Robots cooperating / interacting (purposely or accidentally) with their environment have different requirements than the current stiff robotic systems
 - Accuracy and repeatability are necessary but probably not the highest priorities
 - **Adaptability** to interaction (whole body level) , **safety** and **robustness** is at least of equal significance

• How to satisfy the new requirements ?

Stiff body/actuation for accuracy
+
Active/Controlled impedance
to satisfy new requirements

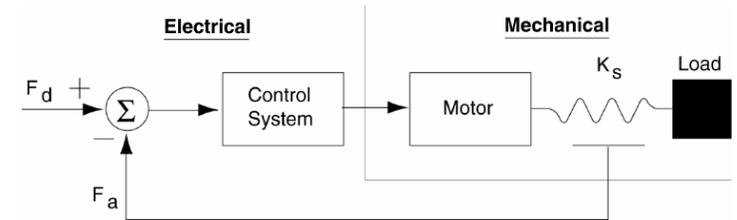
Intrinsic body compliance
+
Control to satisfy performance indexes

1. **lower impact forces, improves robustness**
2. **passive adaptability to interaction**
3. peak power generation
4. **energy efficiency**

Series elastic actuation (SEA)

- **Fixed series elasticity**

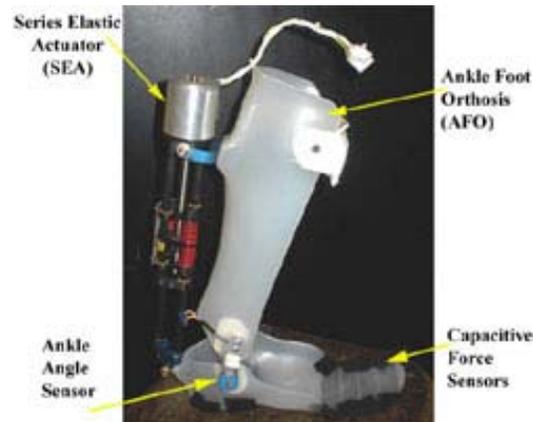
- passively adaptable
- lower impact forces
- inherently safer, more tolerant to disturbances
- can be combined with active stiffness regulation



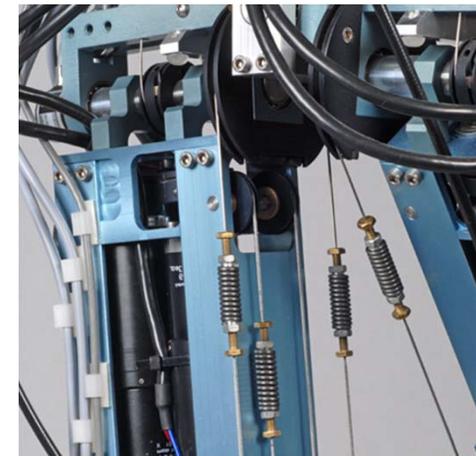
- preset passive mechanical compliance
- performance is compromised



Pratt et al, 1995

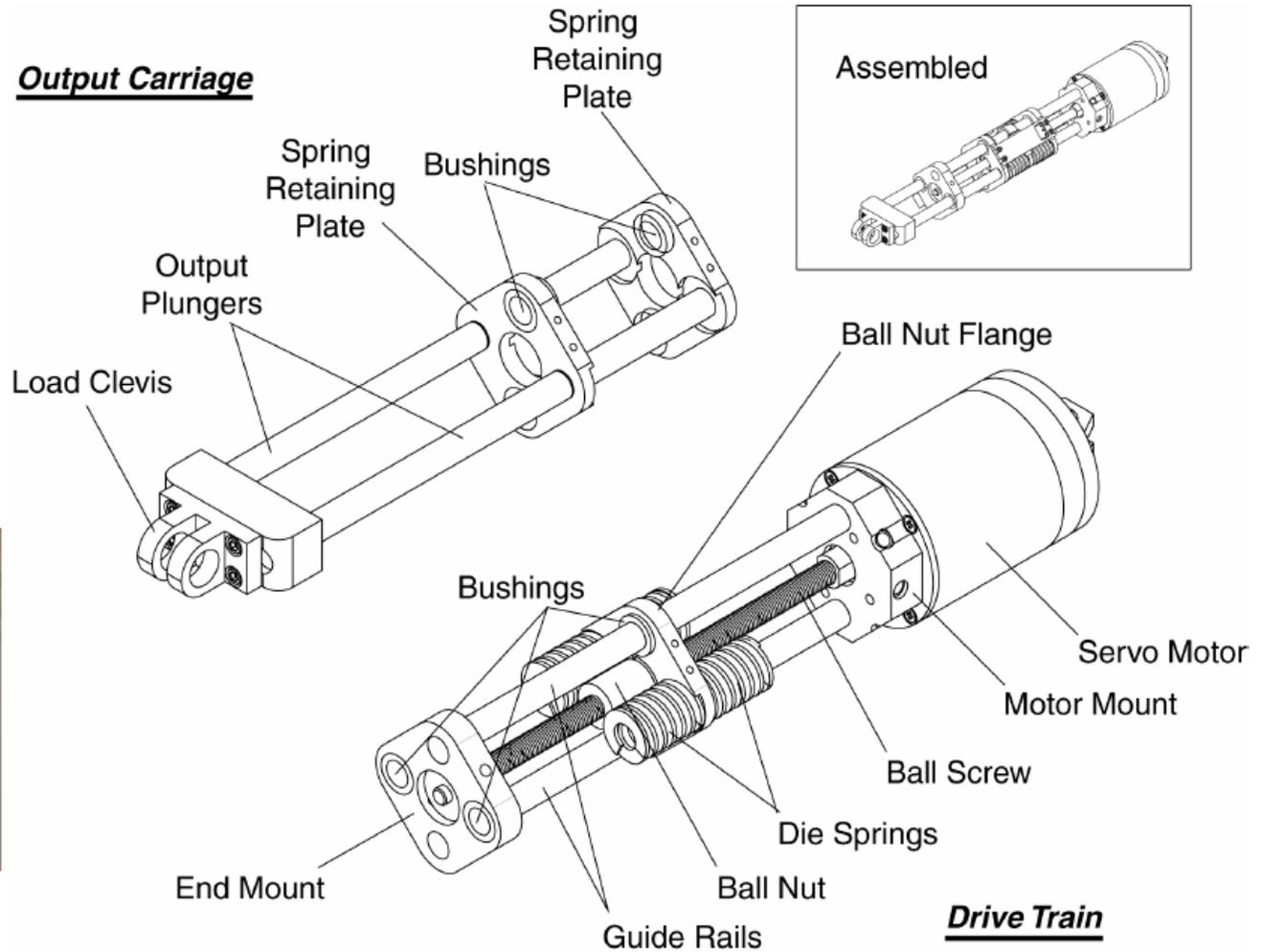


Herr et al, 2004



Wisse et al, 2007

Series elastic actuator



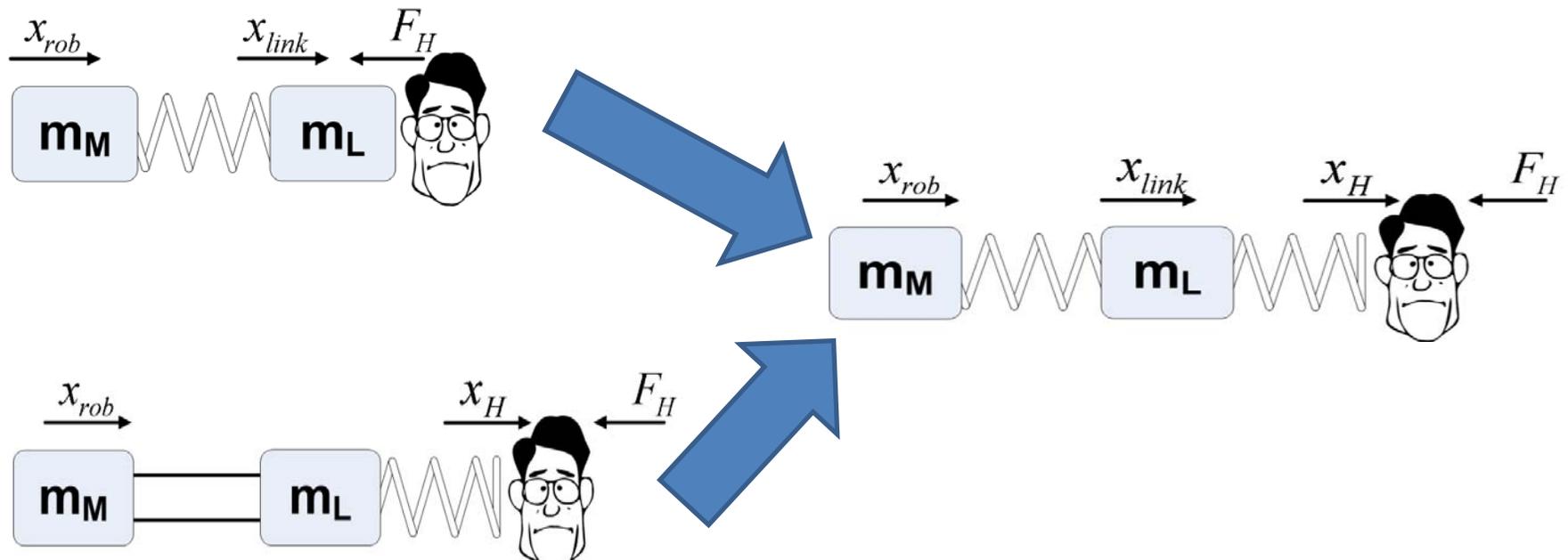
Pratt et al, 95

Intrinsic passive compliance

Effect on the impact forces

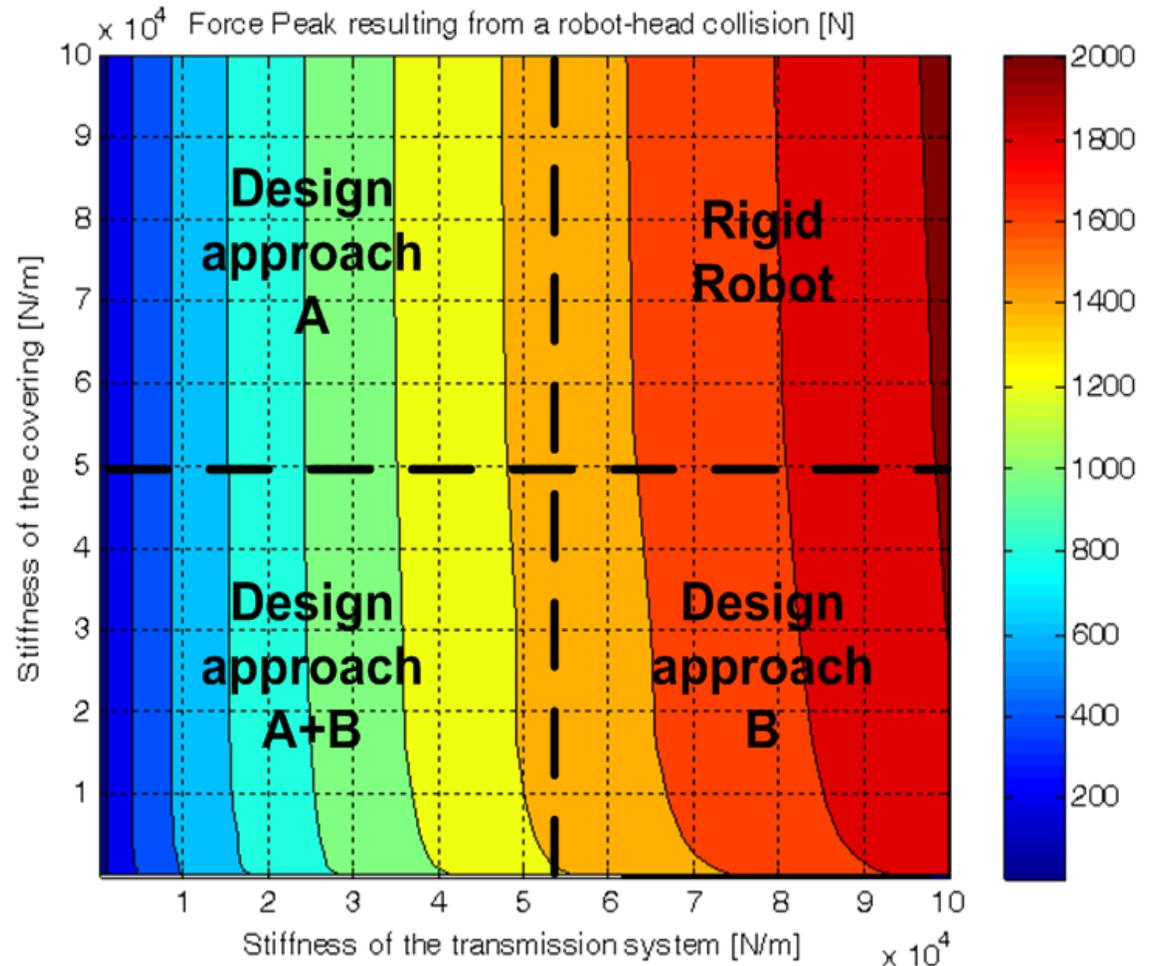
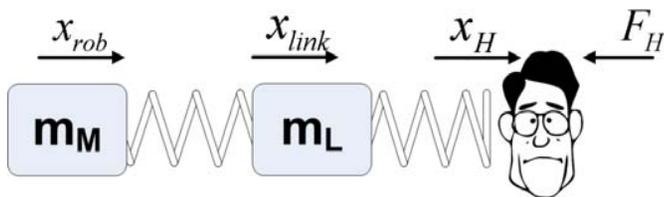
Compliance can be introduced:

- A: between the actuator and the link
- B: around the link/structure (soft cover)
- C: A and B



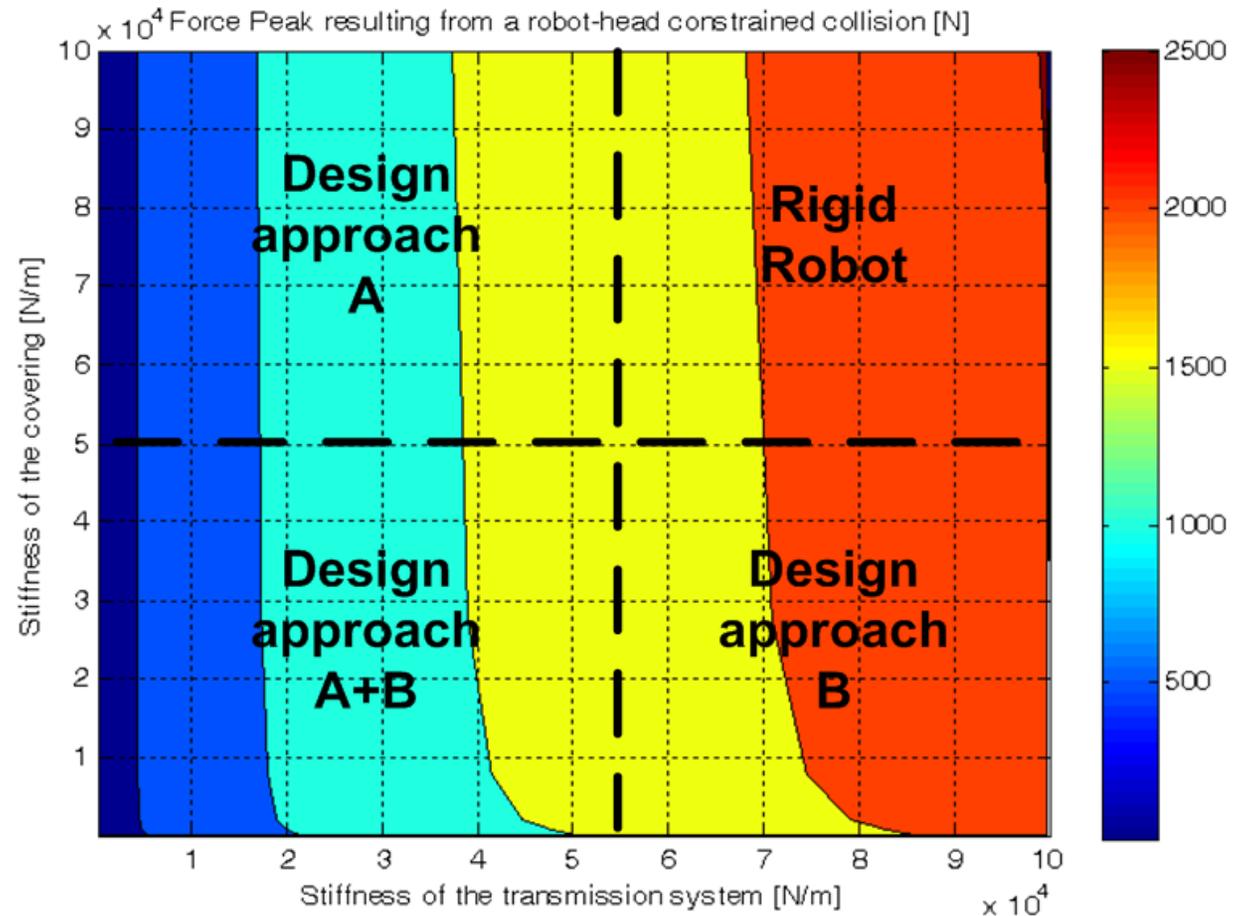
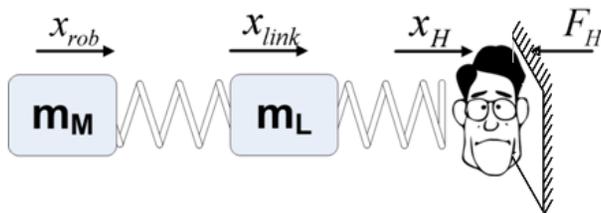
Effect of the stiffness to the impact forces: unconstrained case

Parameter	Value
Link reflected mass	1.85 kg
Rotor reflected mass	0.79 kg
External object mass	5 kg
Impact speed	3 m/s



Effect of the stiffness to the impact forces: constrained case

Parameter	Value
Link reflected mass	1.85 kg
Rotor reflected mass	0.79 kg
External object mass	5 kg
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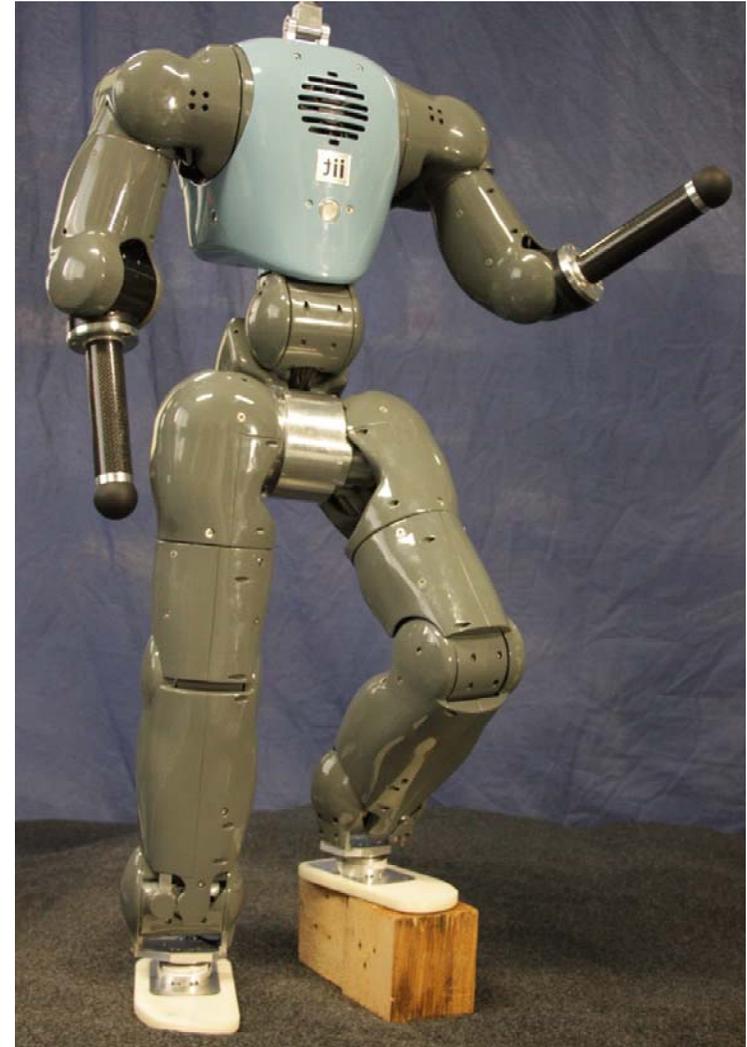
- ❑ The goal of AMARSi is to make a qualitative jump toward rich motor behaviour where novel mechanical, control and learning solutions are integrated with each other

AMARSI passive COMpliant huMANoid (COMAN)

- a full humanoid robot
- 25 major degrees of freedom (arms/legs and torso excluding hands and neck/head)
- **intrinsic passive** compliance
- joint **torque sensing/active compliance**

COMAN overview

- **Actuation**
 - moderate to high power
 - passive series compliance
 - legs (ankle/knee and hip sagittal joints)
 - torso (pitch and yaw)
 - arms: (shoulder and elbow)
 - no cable transmissions
- **Sensing**
 - joint torque sensing
 - 2 x 6 DOF F/T sensors
 - IMU
- **Power autonomy**
 - battery
 - power management system
- **On board computation power**
 - 2 x PC104 (1 inside the torso and one to be added in the head)
- **Body housing**
 - internal electrical wiring routing
 - full body covers (no exposed components/wires)

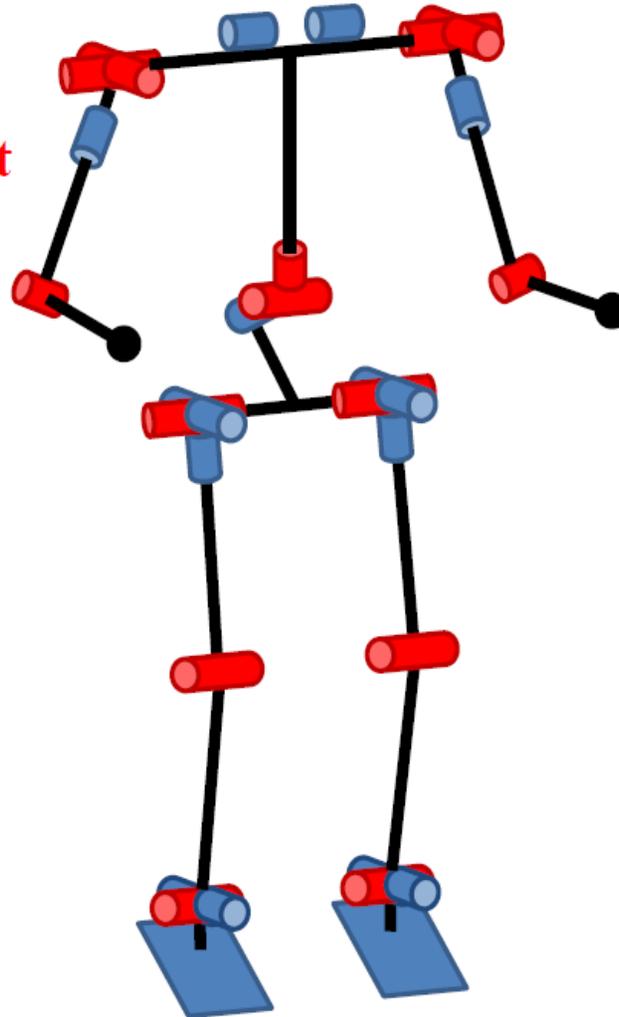


Tsagarakis et al, ICRA 2013

COMAN kinematics

 **Stiff Joint**

 **Compliant Joint**



Joint	Number of DOF
Ankle	2
Knee	1
Hip	3
Waist	3
Shoulder	3
Elbow	1
Neck	2

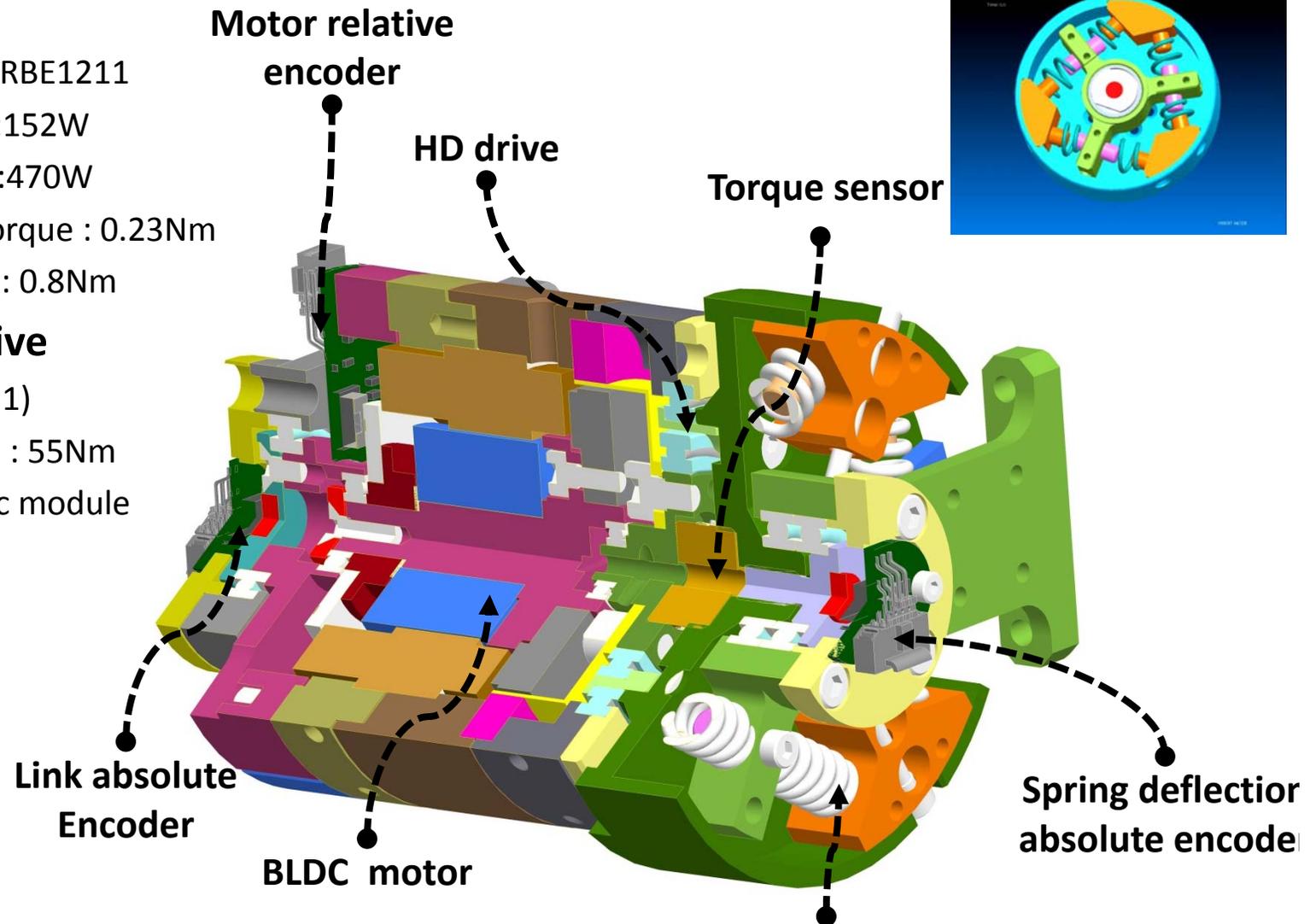
Compliant joint: CompAct unit

- **Motor**

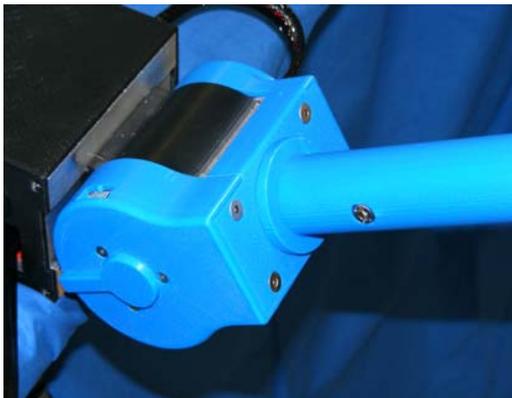
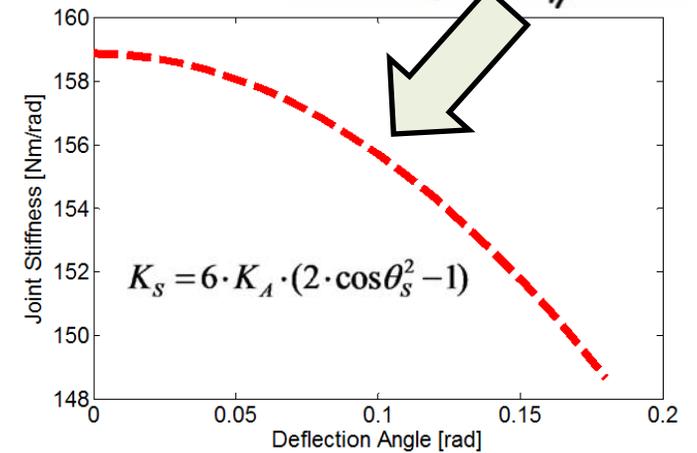
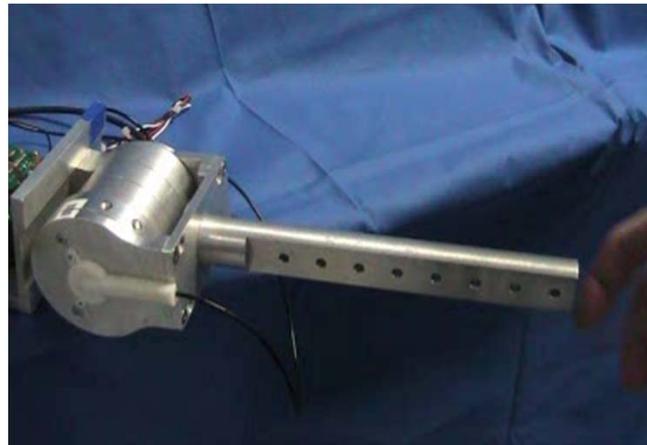
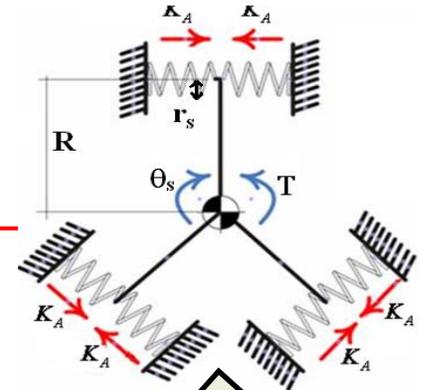
- Kollmorgen RBE1211
- rate power :152W
- peak power:470W
- continues torque : 0.23Nm
- peak torque: 0.8Nm

- **Reduction drive**

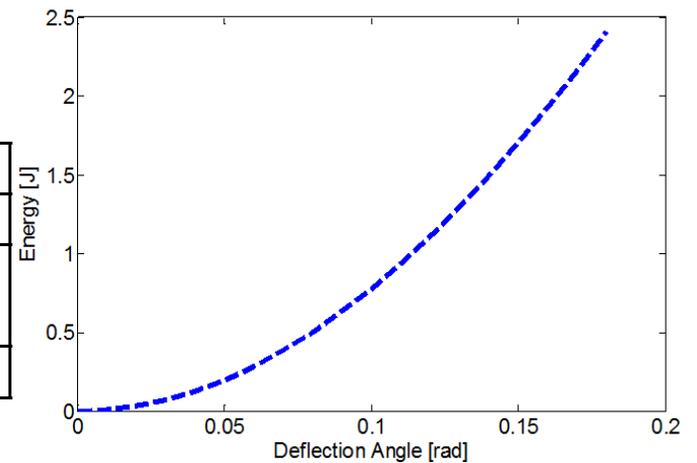
- CSD17 (100:1)
- peak torque : 55Nm
- series elastic module



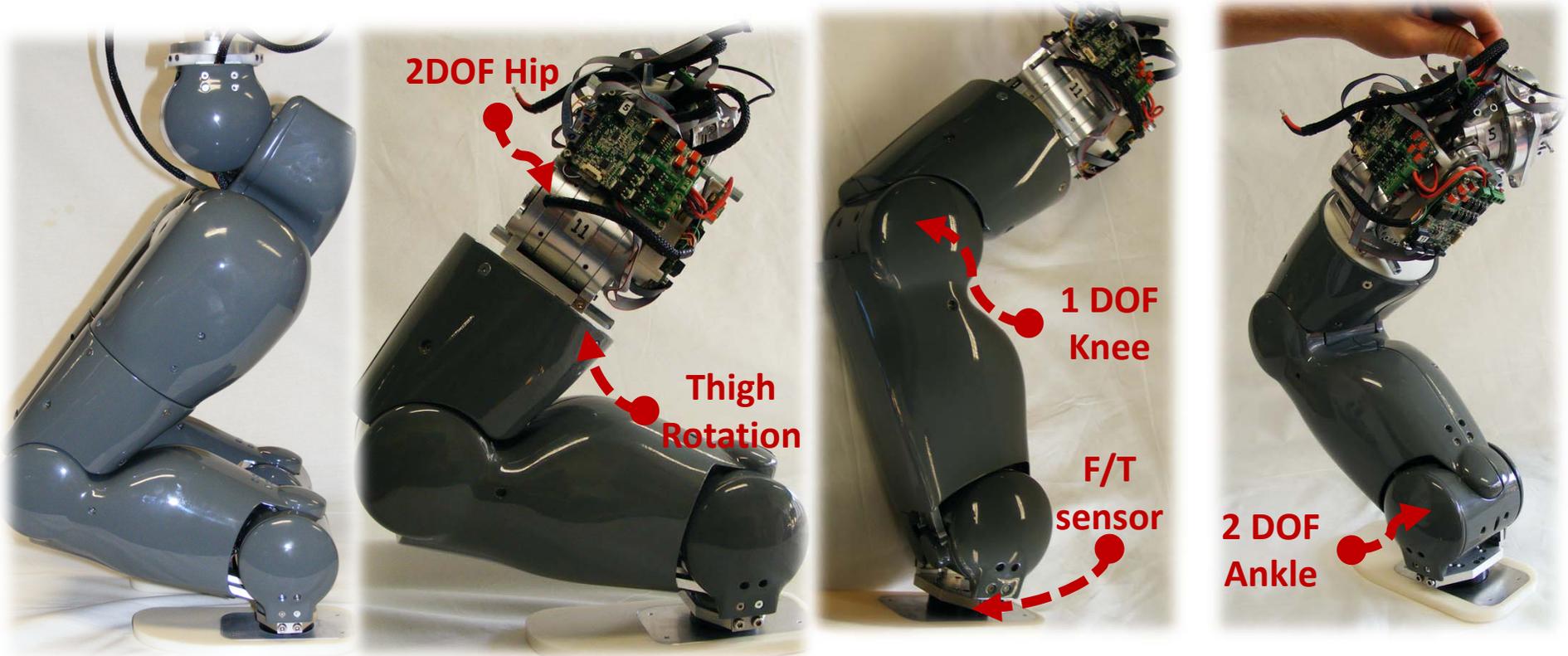
The CompAct actuator



Diameter	70mm
Length	80mm
Max rotary passive deflection	+/-0.2rad
Weight	0.52Kg

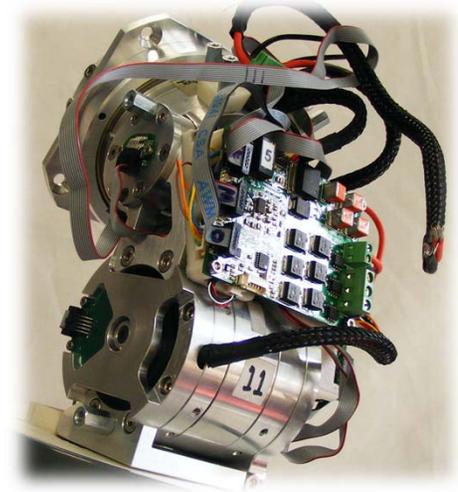
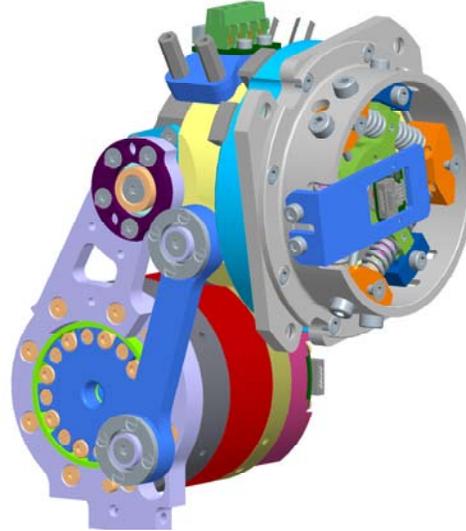


COMAN lower body



Hip design and specs

- serial mechanism
- passive compliance for hip pitch and roll
- gear ratio 100:1

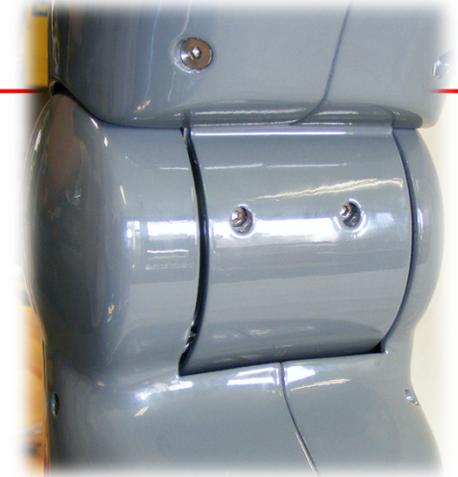
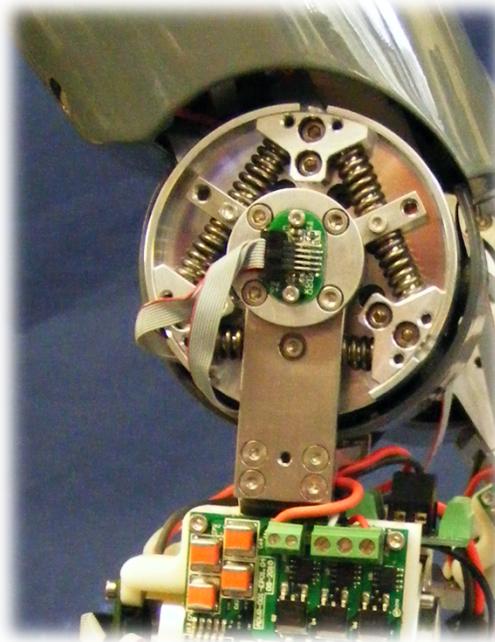


Joint	New Hip	
	Motion Range (°)	Peak Torque (Nm)
Flex/Ext	+110, -45	55 (6.2rad/s at 36V, 9.0rad/s at 48V)
Abd/Add	-60, +20	55 (6.2rad/s at 36V, 9.0rad/s at 48V)
Rotation	+50, -50	55 (6.2rad/s at 36V, 9.0rad/s at 48V)



Knee design and specs

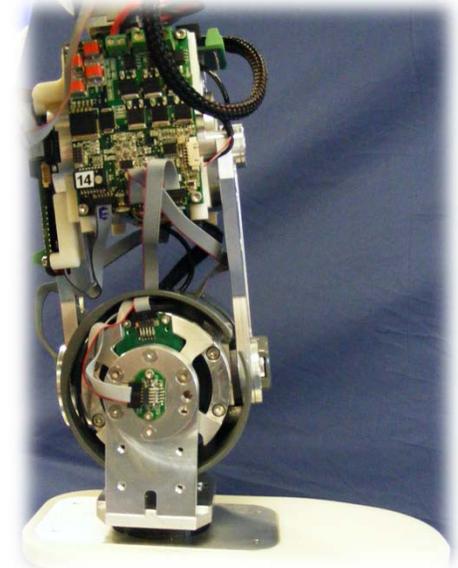
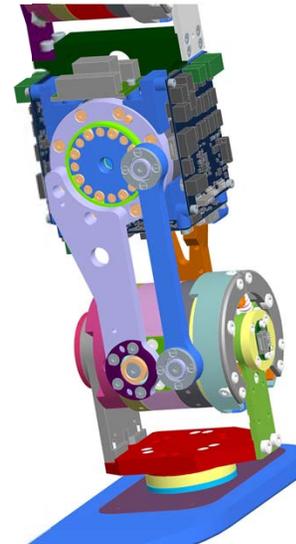
- series elastic actuated
- gear ratio 100:1



Joint	knee	
	Motion Range (°)	Torque (Nm)
Flex/Ext	-120, +10	55 (6.2rad/s at 36V, 9.0rad/s at 48V)

Ankle design and specs

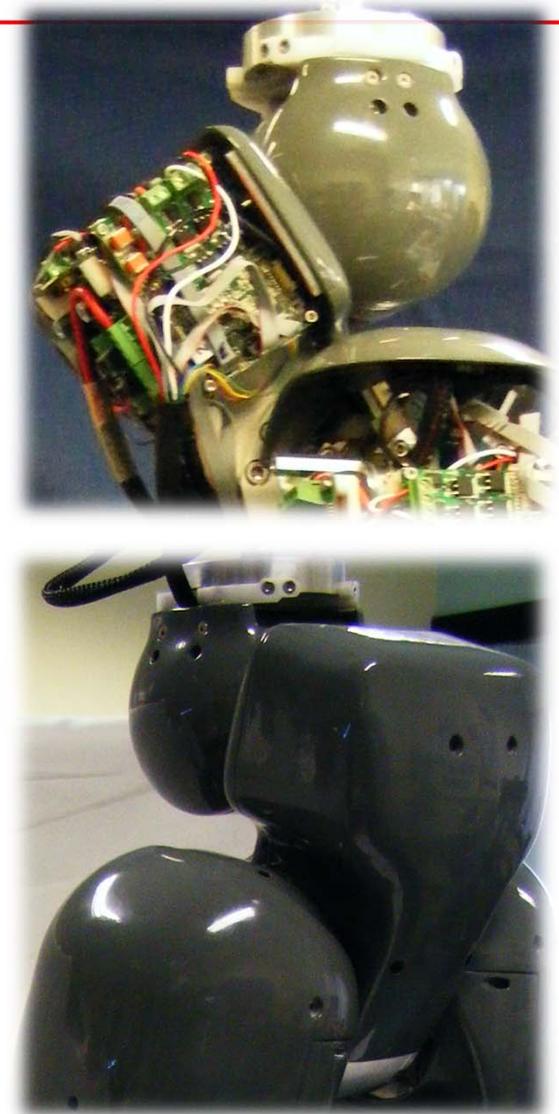
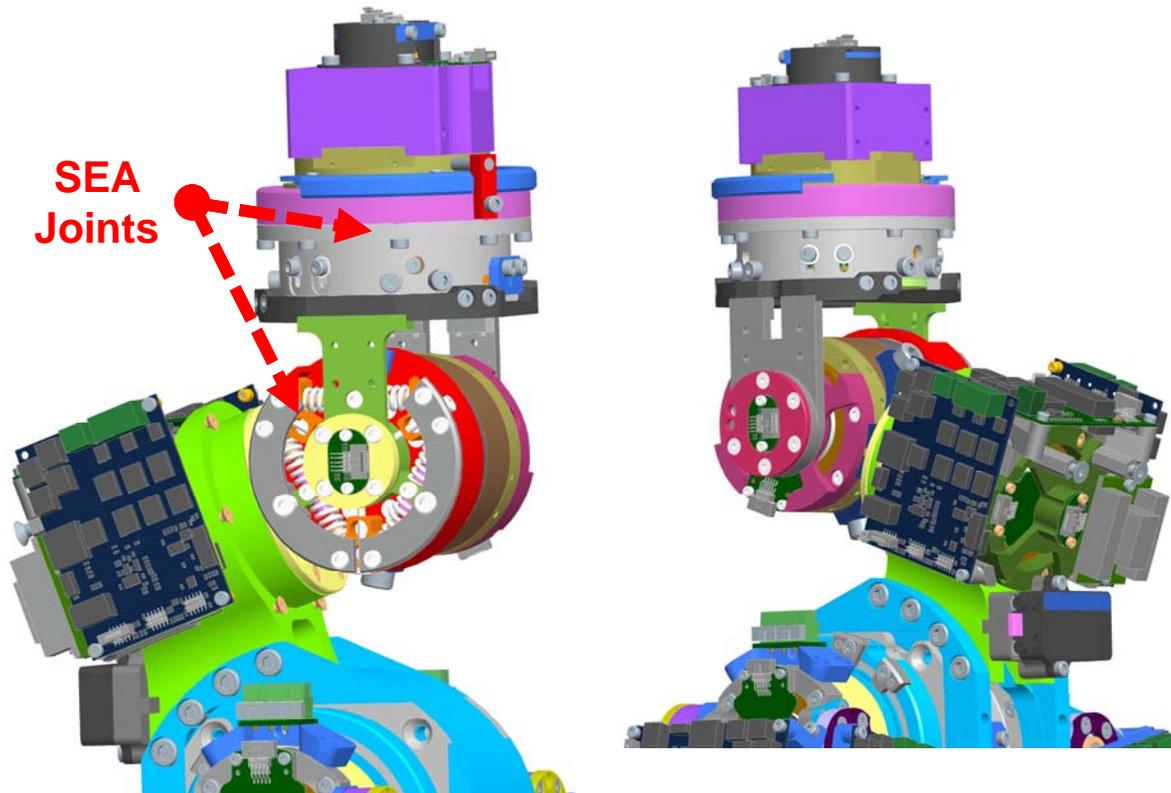
- serial mechanism
- passive compliance for hip pitch and roll
- gear ratio 100:1



Joint	Ankle	
	Motion Range (°)	Torque (Nm)
Flex/Ext	+70, +50	55 (6.2rad/s at 36V, 9.0rad/s at 48V)
Abd/Add	-35, +35	55 (6.2rad/s at 36V, 9.0rad/s at 48V)

COMAN torso joint

- 3DOF serial mechanism
- passive compliance for pitch and yaw motions



Upper torso and neck



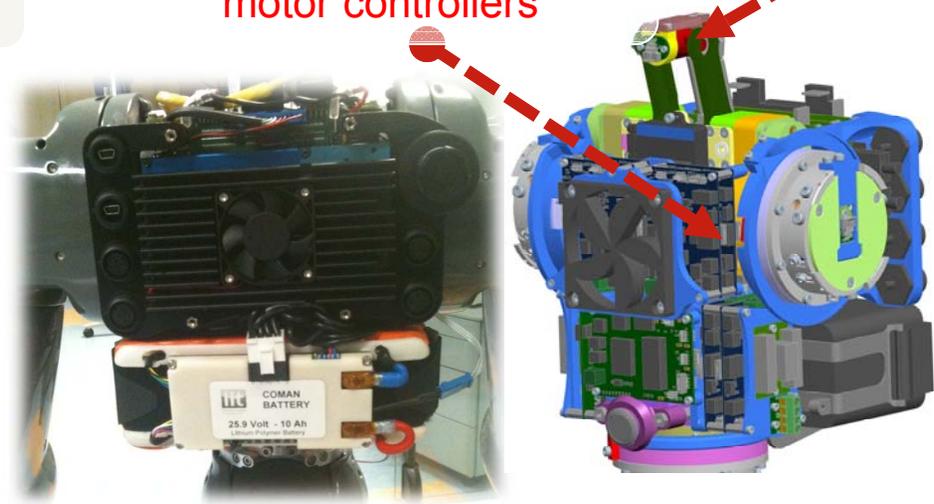
Compliant
Shoulder
flexion

PC104
controller

Shoulder and neck
motor controllers

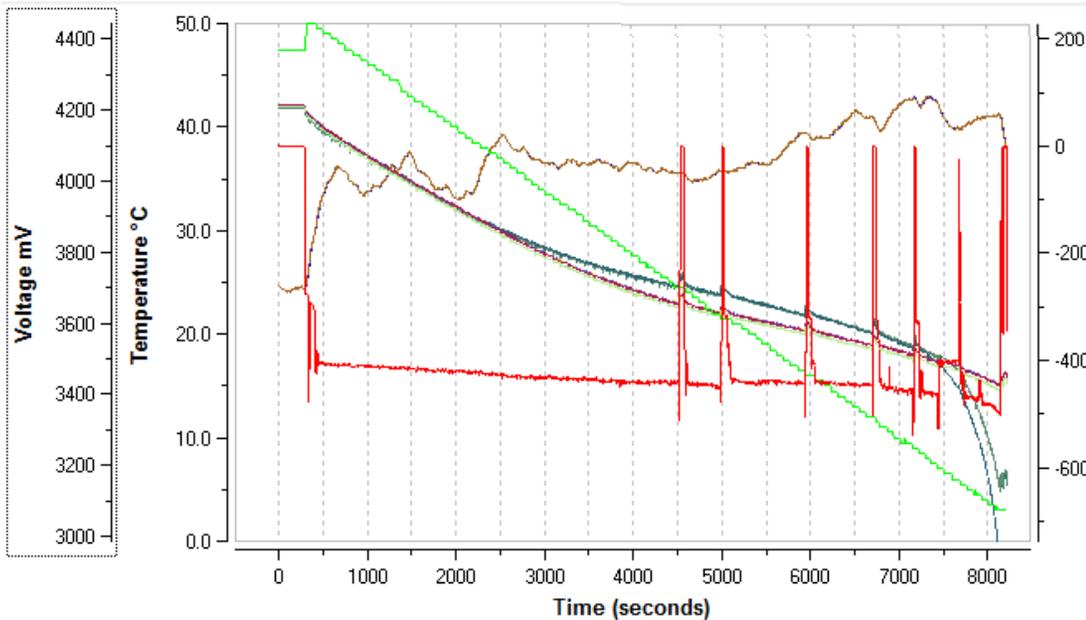
Neck module

Battery pack
and BMS
system



Battery pack and BMS system

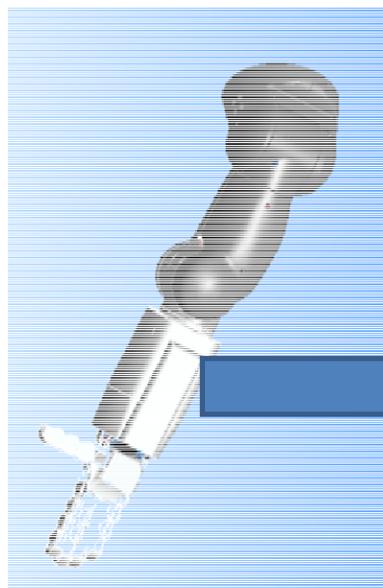
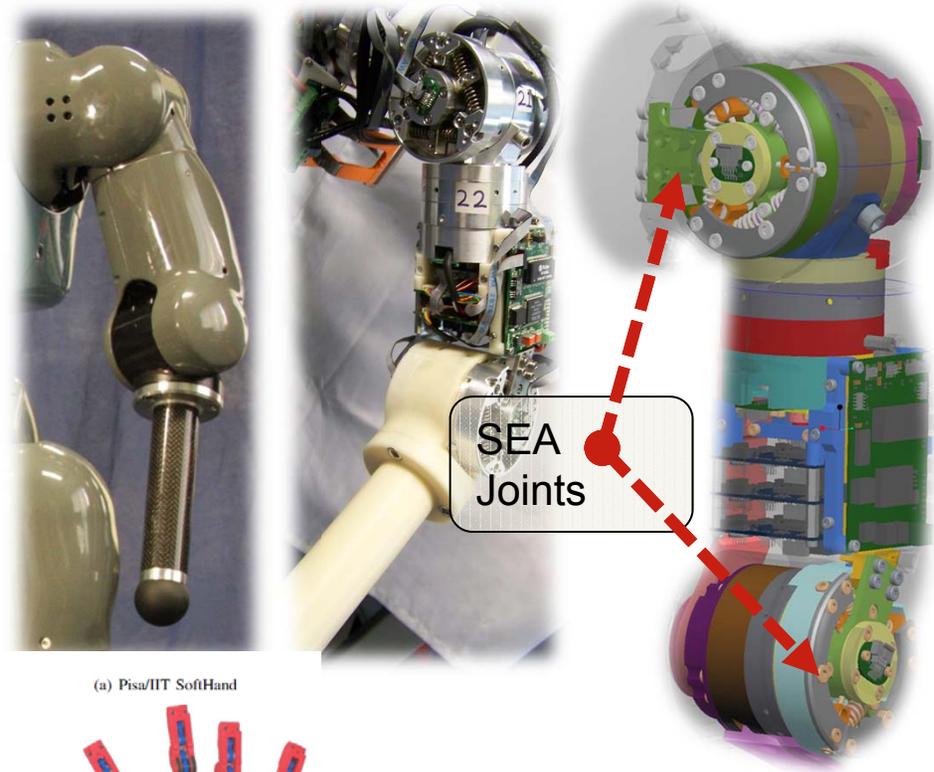
- Lithium polymer
- weight 1.7Kg
- nominal voltage 23-29V
- capacity 10Ah



..more than two hours of light-duty squatting

COMAN arm

- 3DOF serial shoulder mechanism
- 1DOF elbow
- passive compliance
 - shoulder (flex/ext and abd/add) motions
 - elbow flex/ext
- **Wrist/hand will be integrated soon**



(a) Pisa/IIT SoftHand

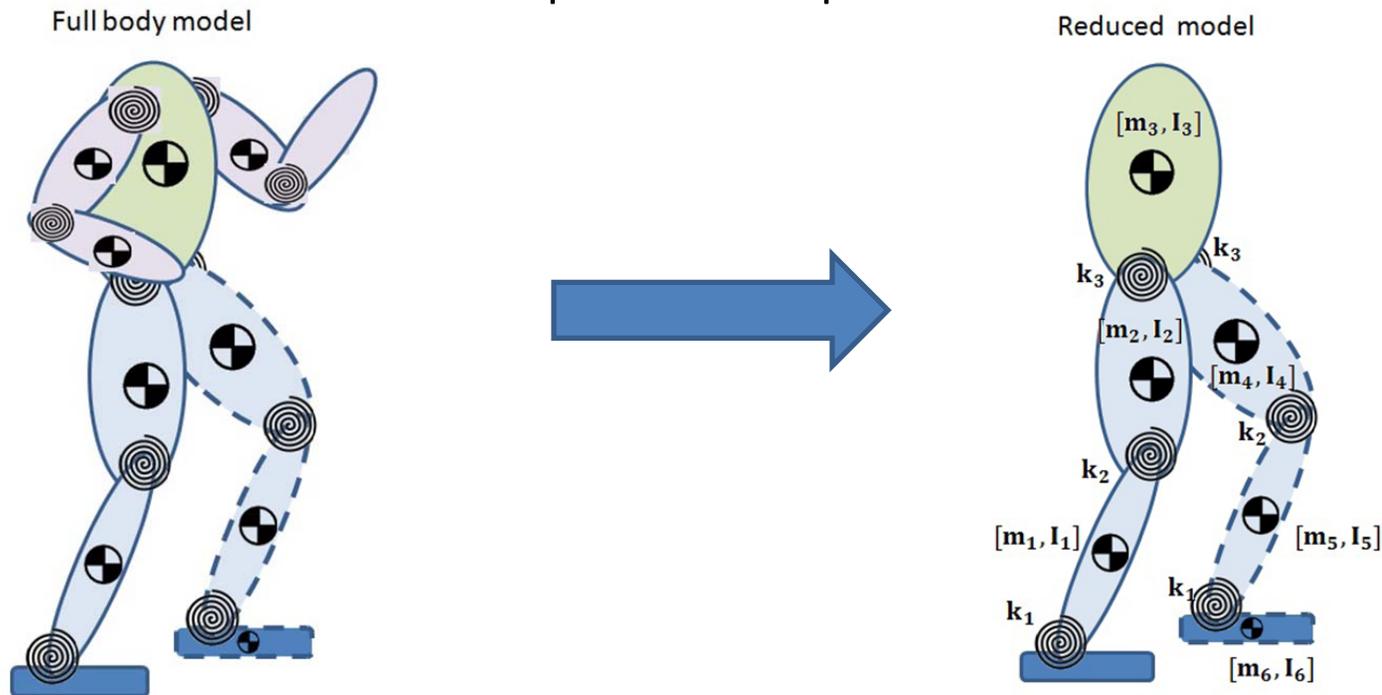
Catalano et al, 2012

How to tune the intrinsic elasticity?

- Where to place the compliance?
- How to select the joint compliance level?
- the tuning of the series passive elasticity still remains an experimental trial and error process and very little information on the methodologies used is available
- Can we tune compliance using a more systematic method?
 - optimise for bandwidth constraints

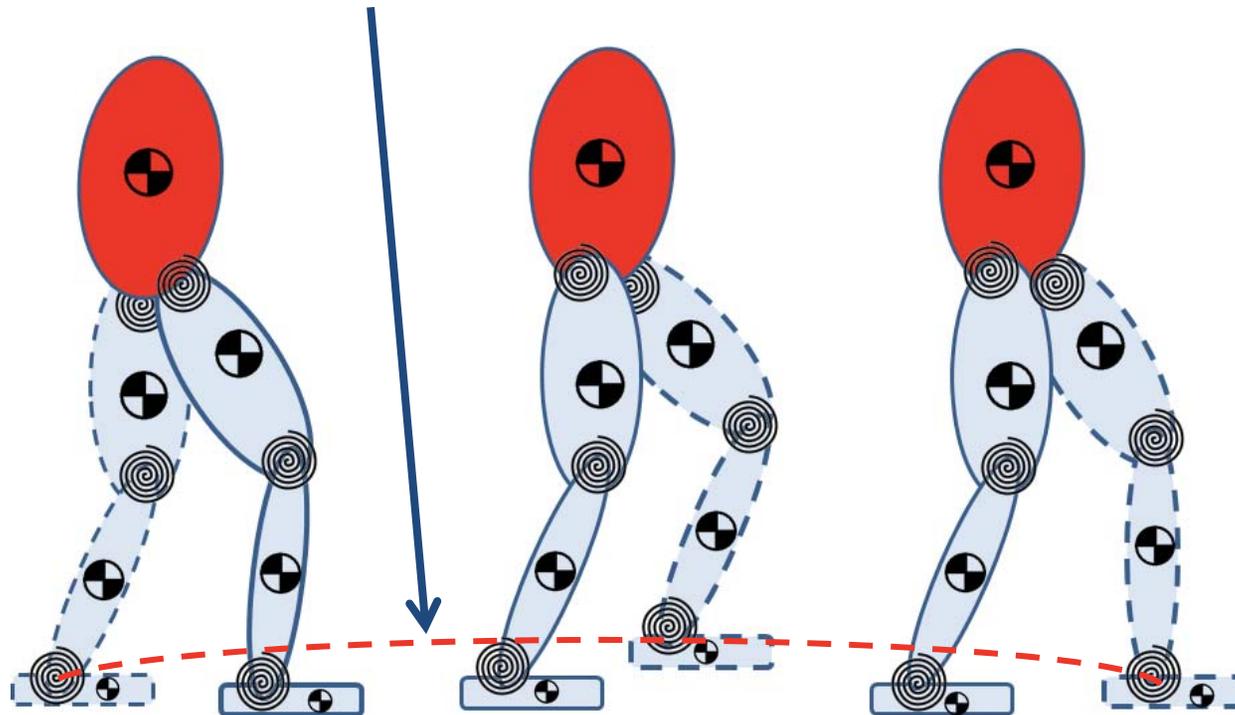
Selecting COMAN's leg compliance

- multi-dof mass-spring system
- highly nonlinear varying system
 - mass matrix changes
 - additional nonlinearities may exist in the drive elasticity
- resonances change and depend on the posture

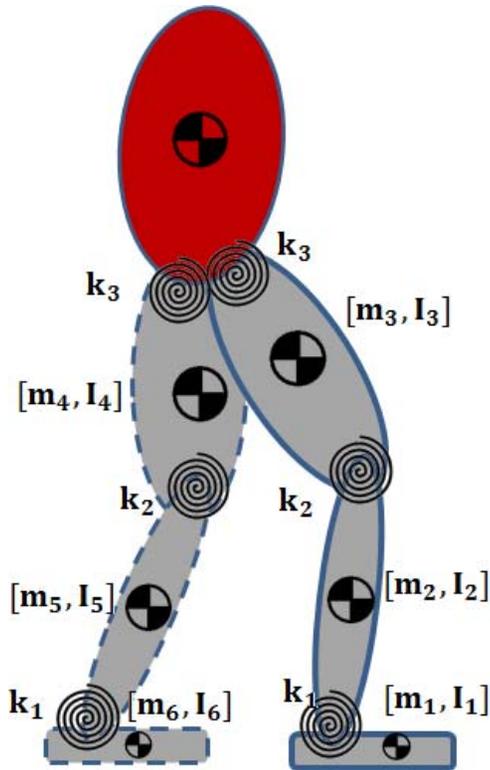


Selecting COMAN's leg compliance

Twenty posture configuration points of the single support phase were considered

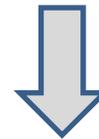


Selecting COMAN's leg compliance



$$\Delta(q) \begin{bmatrix} \ddot{q} \\ \ddot{\theta} \end{bmatrix} + \Gamma(q, \dot{q}) \begin{bmatrix} \dot{q} \\ \dot{\theta} \end{bmatrix} + \begin{bmatrix} g(q) - K(\theta - q) \\ K(\theta - q) \end{bmatrix} = \begin{bmatrix} \tau_e \\ \tau_m \end{bmatrix}$$

$$\Theta = [q^T \ \theta^T]^T \quad G(q) = [g(q)^T \ 0]^T$$



$$\Delta(q)\ddot{\Theta} + \Gamma(q, \dot{q})\dot{\Theta} + S\Theta + G(q) = \tau \quad S = \begin{bmatrix} K & -K \\ -K & K \end{bmatrix}$$

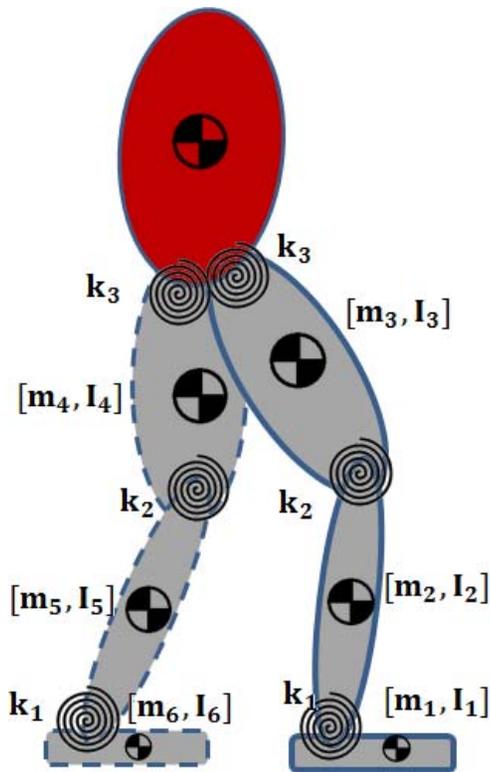
$$\phi = \Theta - \Theta_e$$

$$\Delta(q_e)\ddot{\phi} + S_g\phi = \tau$$

$$S_g = \begin{bmatrix} K & -K \\ -K & K \end{bmatrix} + \nabla G(q_e)$$

$$\nabla G(q_e) = \begin{bmatrix} \nabla g(q_e) & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix}$$

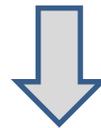
Selecting COMAN's leg compliance



$$S_{gm} = \begin{bmatrix} K + \nabla g(q_e) & -K \\ -K & K + K_m \end{bmatrix}$$

$$\Delta(q_e)\ddot{\phi} + S_{gm}\phi = \tau$$

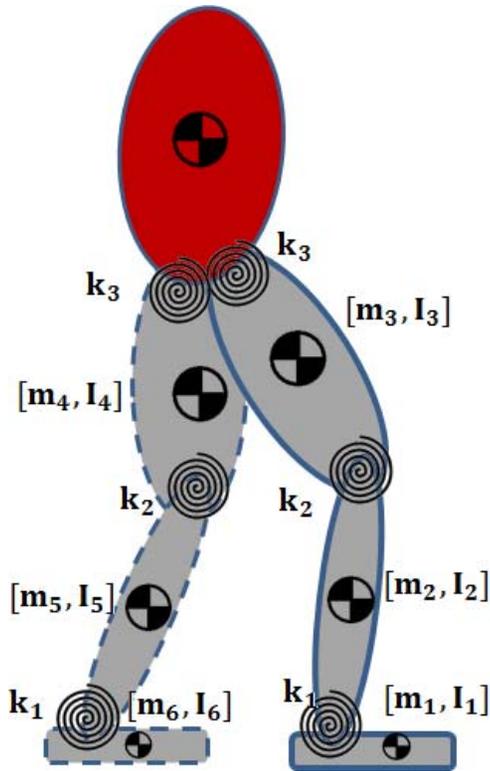
$$M\ddot{x} + Kx = f$$



$$A = \Delta(q_e)^{-1} S_{gm}$$

$$f_i = \frac{1}{2\pi} \sqrt{\lambda_i}, i = 1, 2 \dots N$$

Optimal joint stiffness selection



constrained optimization problem

- maximize the joint passive deflection for a given joint torque vector
- subject to constraints
 - natural frequencies constraints
 - stiffness constraints

$$\min\left(\frac{2}{\tau_i^2\left(\frac{1}{k_a} + \frac{1}{k_k} + \frac{1}{k_h}\right)}\right)$$

$$f_{ir} : |f_{ir}| > \frac{\alpha_i}{2\pi} \omega_b, \alpha_i > 1, i = 1, 2, \dots, n$$

$$k_{min} = \frac{\tau_{max}}{\theta_{smax}}$$

$$k_{min} < k_i < k_{max}$$

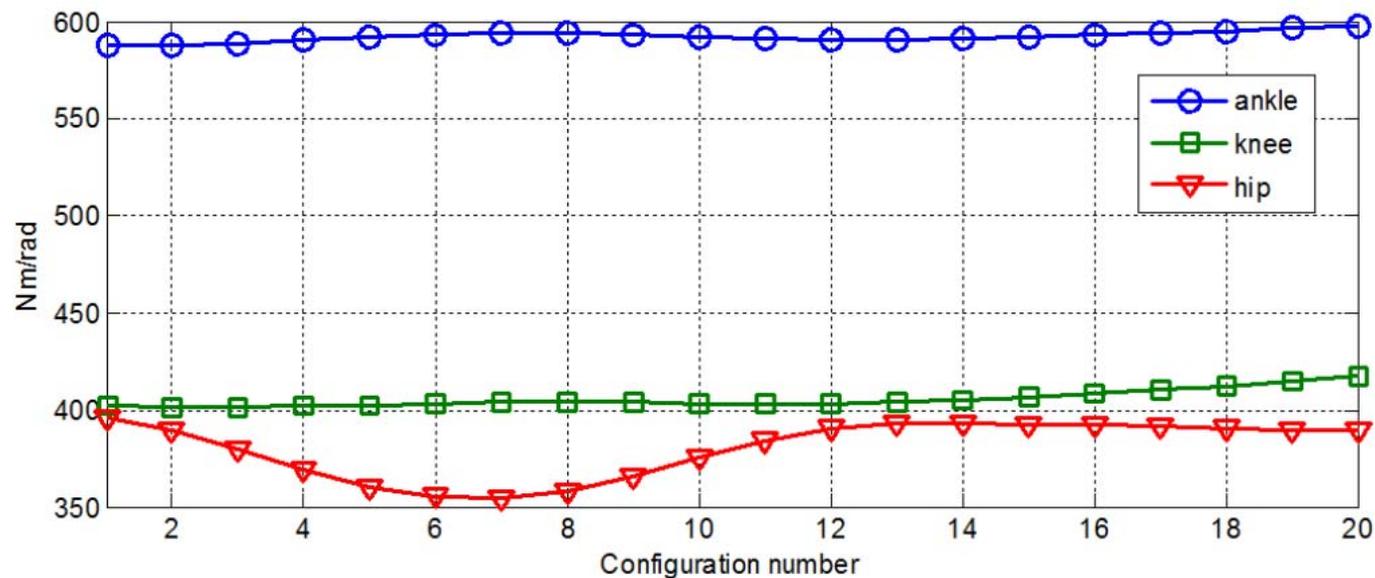
$$k_{max} = 800 \frac{Nm}{rad}$$

Tsagarakis et al, ICRA 2013

Optimal joint stiffness selection

- constraints were chosen for two lowest resonant frequencies
- first and second natural frequencies inequalities constraints:

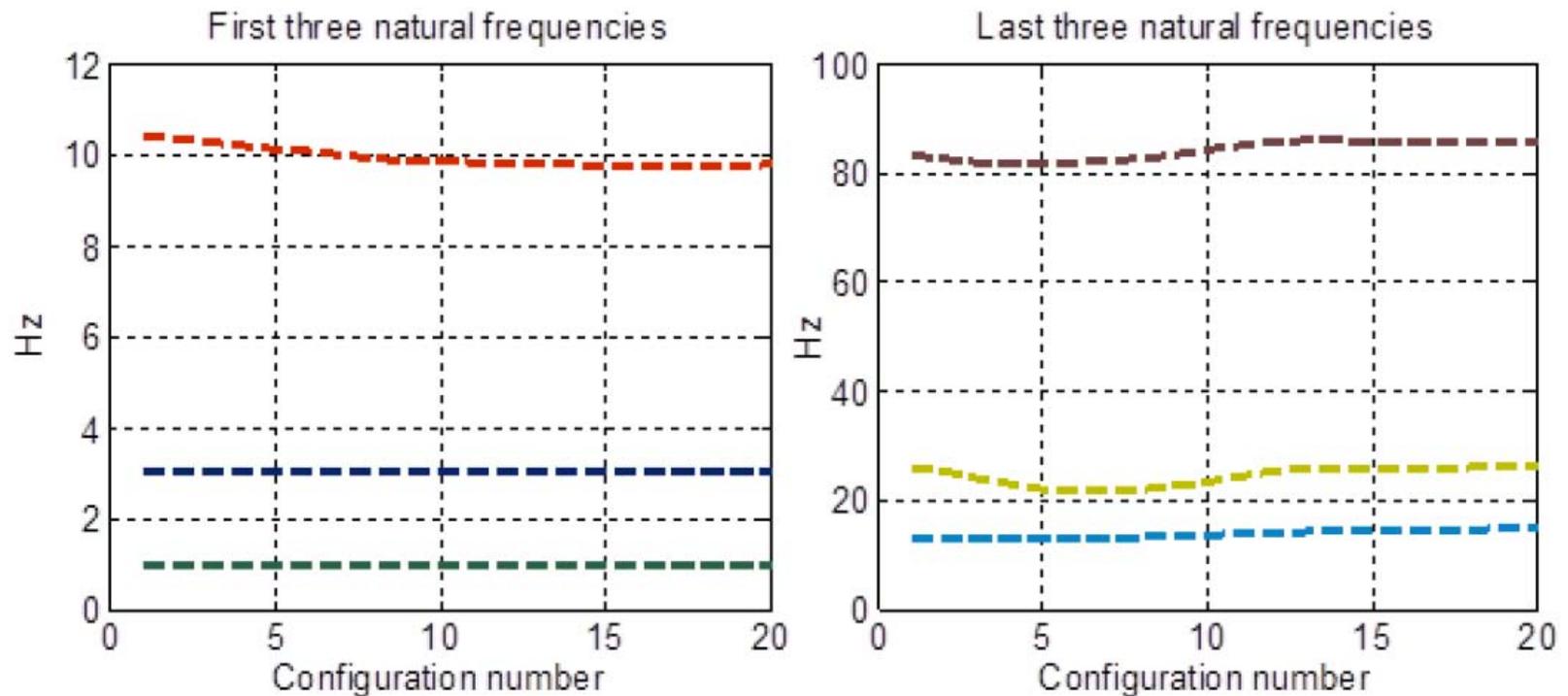
$$(f_1 > 1.0Hz) (f_2 > 3.0Hz)$$



$$(k_a, k_k, k_h) = (597, 417, 396)Nm/rad.$$

Optimal joint stiffness selection

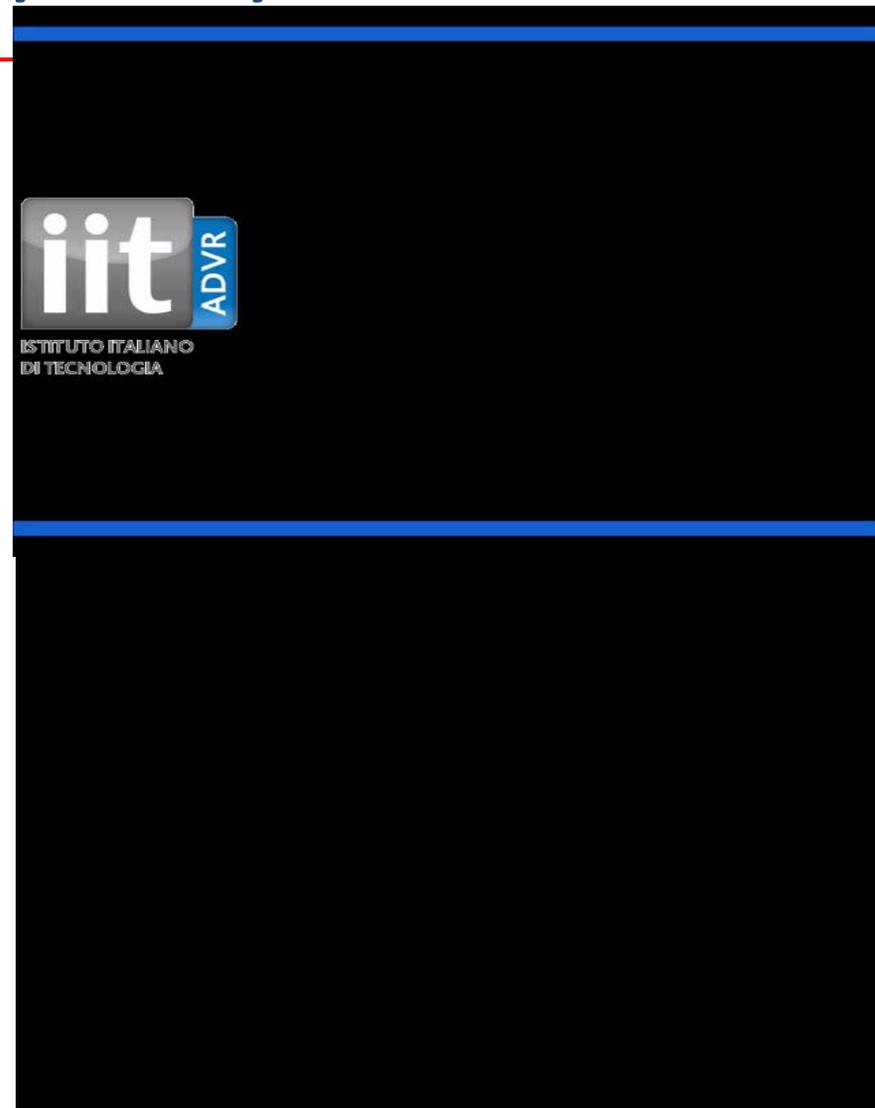
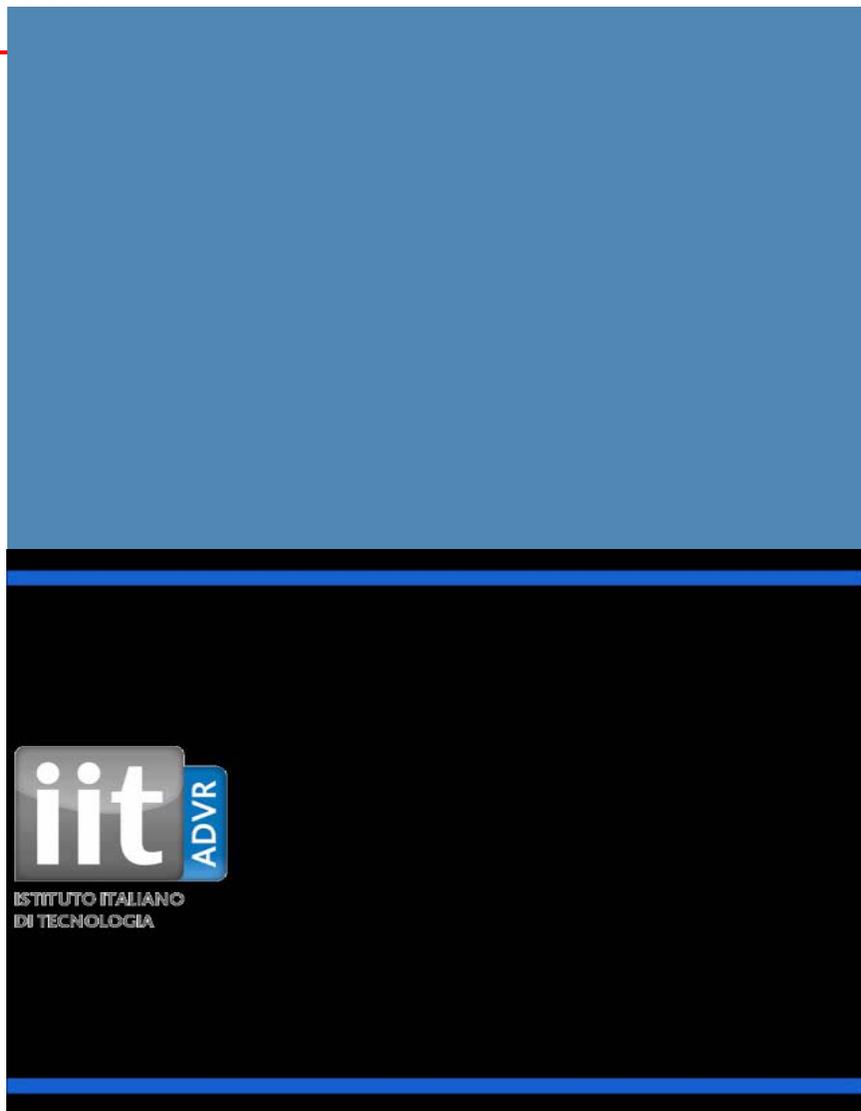
- the resultant natural frequencies given a configuration and the selected optimal joint stiffness matrix



Whole body torque/impedance regulation



COMAN lower body early tests

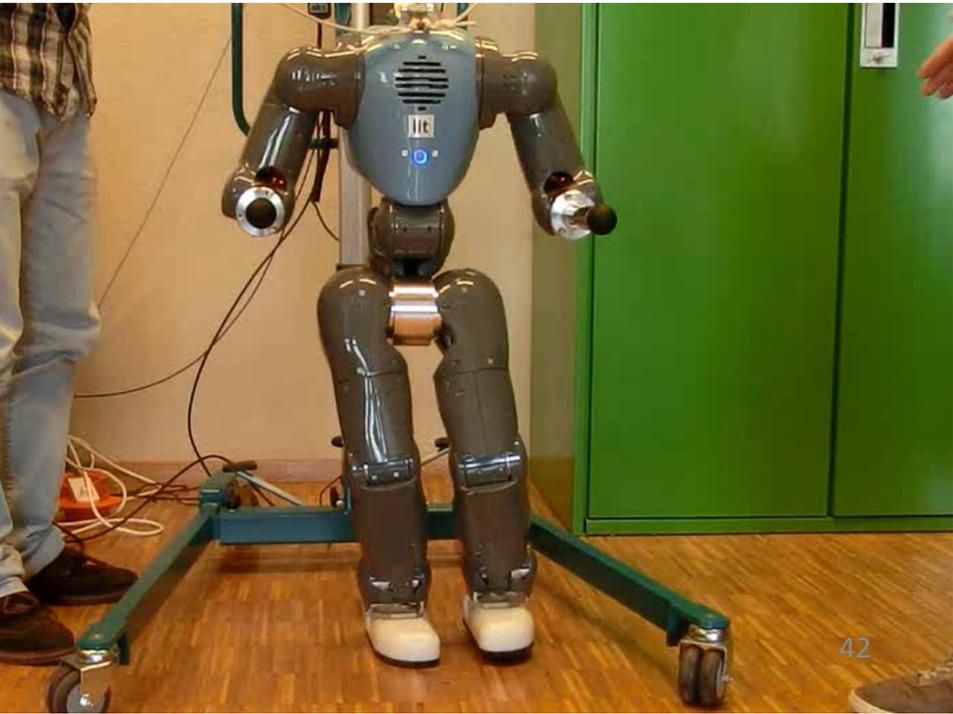
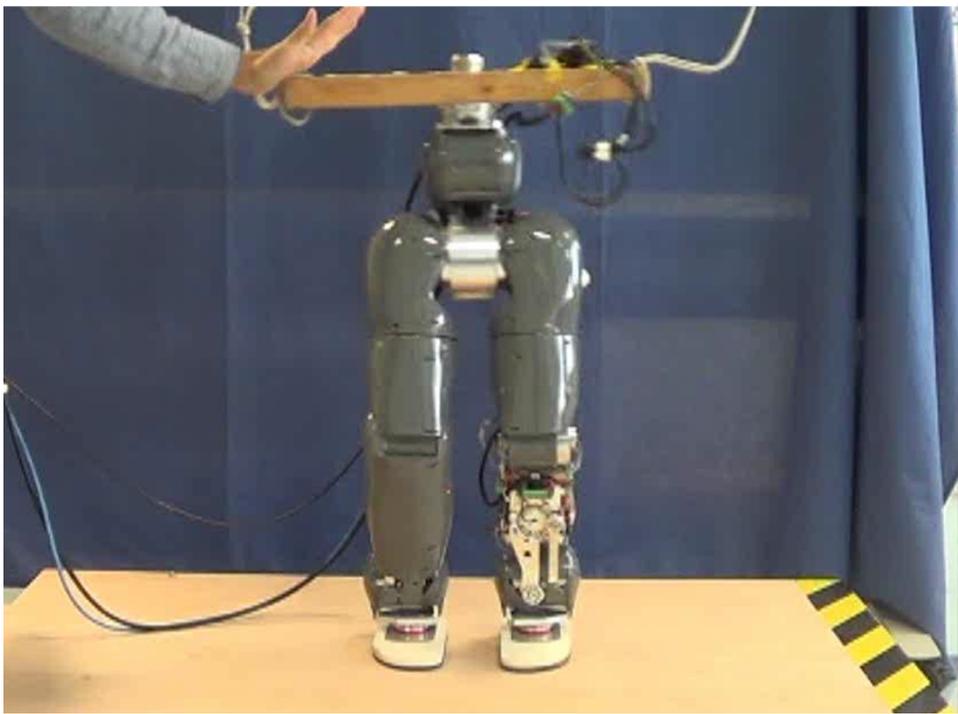
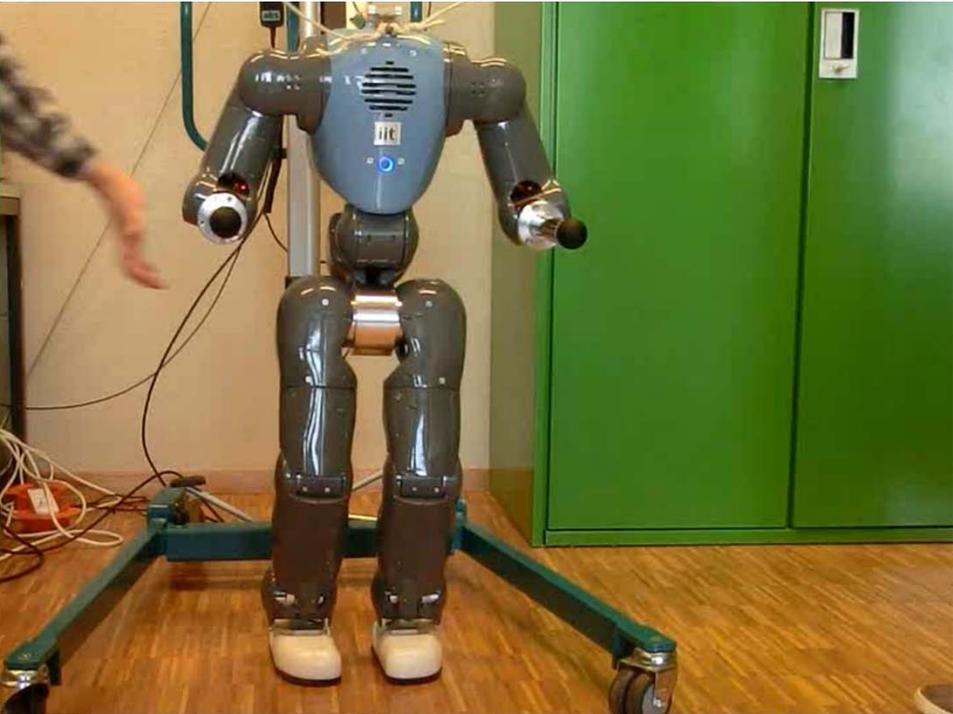
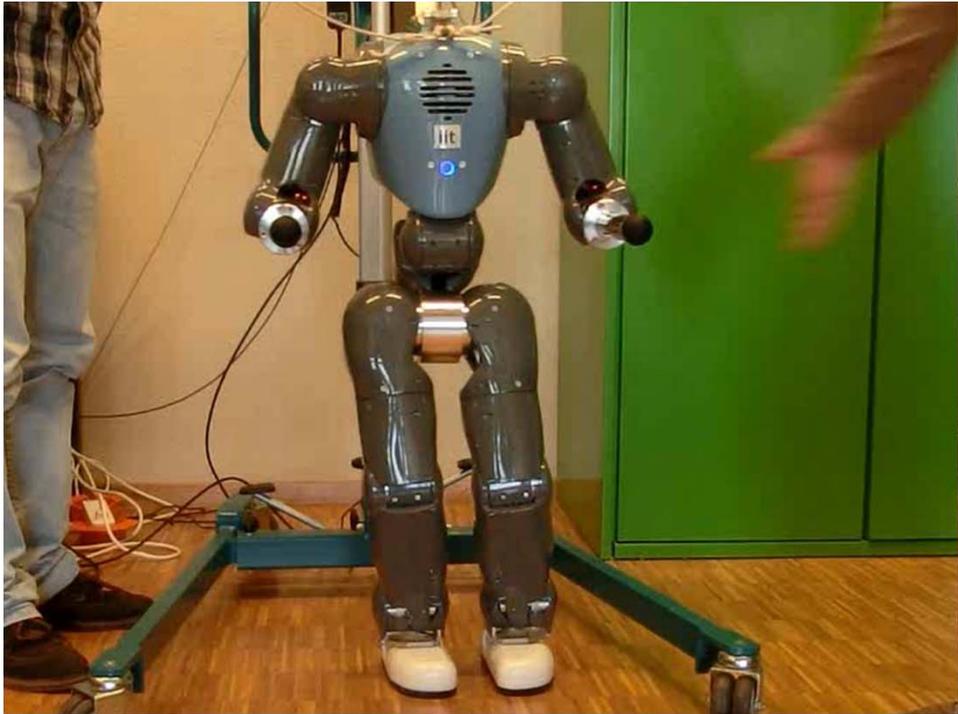


Zhibin Li et al, ICRA 2012

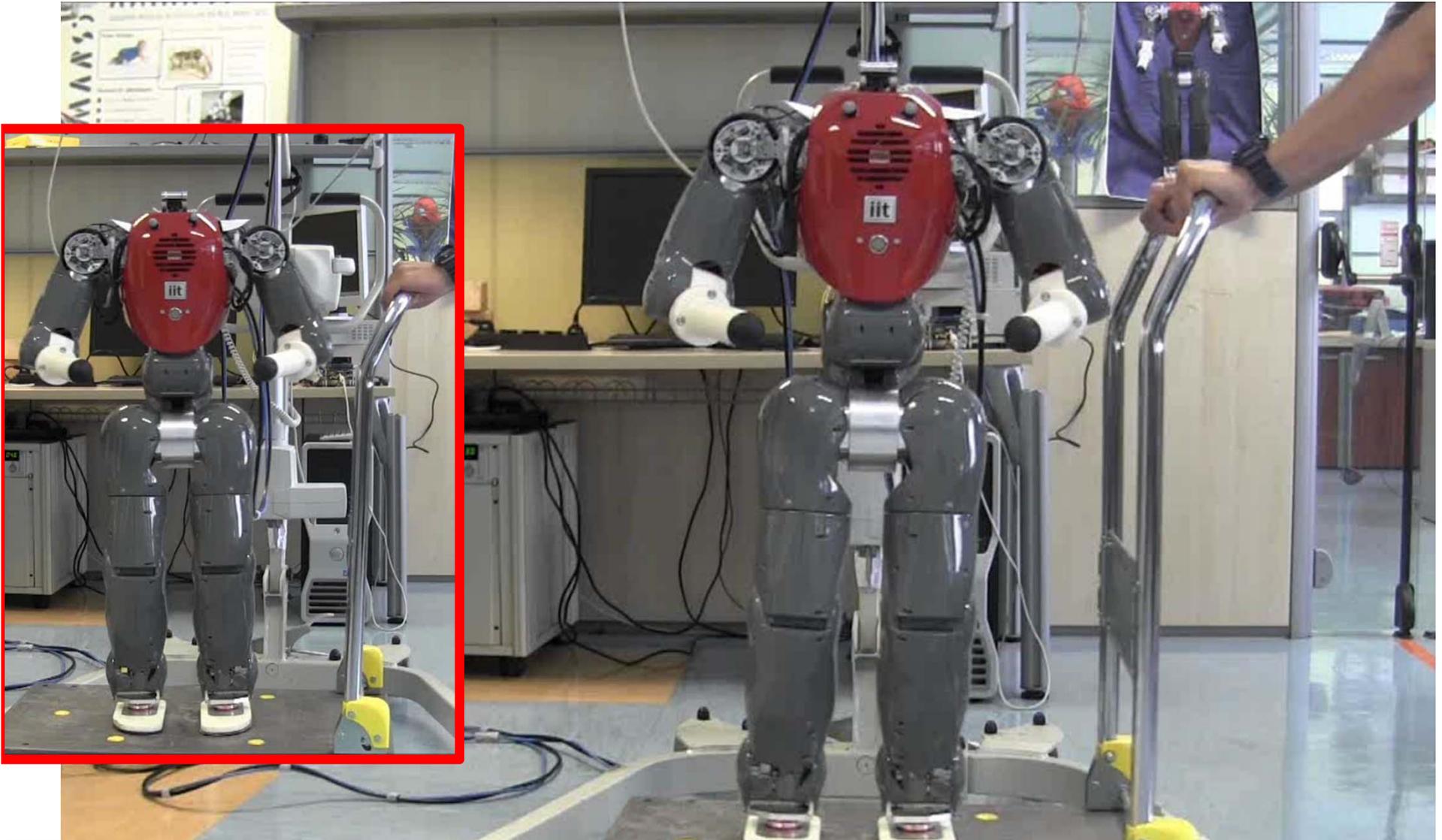


ISTITUTO ITALIANO
DI TECNOLOGIA

Zhibin Li et al, Humanoids 2012



Stabilization on mobile platform



Stabilizing Humanoids on Cross Slopes
Using Terrain Inclination Estimation

Zhibin Li, Nikos Tsagarakis, and Darwin
Caldwell

Department of Advanced Robotics
Italian Institute of Technology

Zhibin Li et al, IROS 2013

Fixed and variable compliance

- **Fixed series elasticity (SEA)**

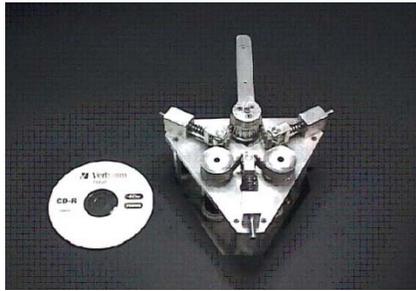
- passively adaptable
- inherently safer
- makes the robot more tolerant to impacts
- does not need additional actuation
- can be combined with active stiffness regulation

- preset passive mechanical compliance
- performance is compromised

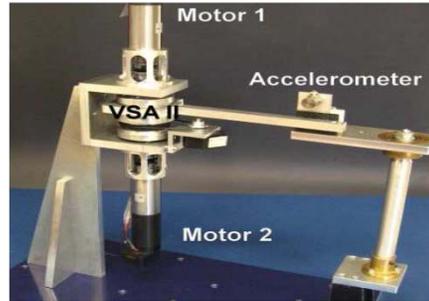
- **Variable impedance actuators**

- passively adaptable
- inherently safer
- makes the robot more tolerant to impacts
- compliance can be regulated according to task needs
 - accuracy, efficiency or safety
- performance can be maintained
- complex, requires additional actuators for the impedance tuning
- application to MDOF systems is not trivial

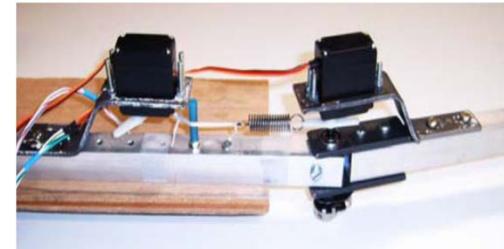
VSAs prototypes



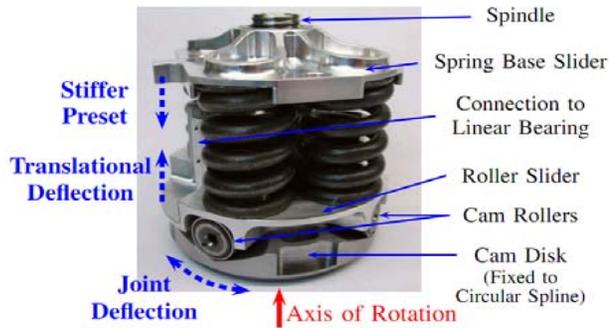
VSA: G. Tonietti *et al.* (2005)



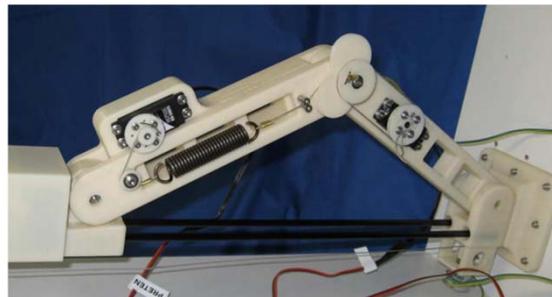
VSA-II: R. Schiavi *et al.* (2008)



MACCEPA: R. Van Ham *et al.* (2007)



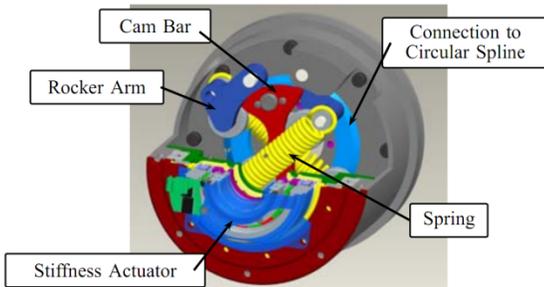
VS-Joint: S. Wolf *et al.* (2008)



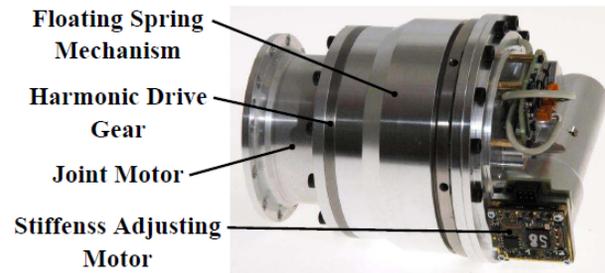
MACCEPA 2.0: B. Vanderborgh *et al.* (2009)



Hybrid VSA:
Byeong-Sang Kim *et al.* (2010)



QA-Joint: O. Eiberger *et al.* (2010)



FSJ: Wolf *et al.* ICRA 2011

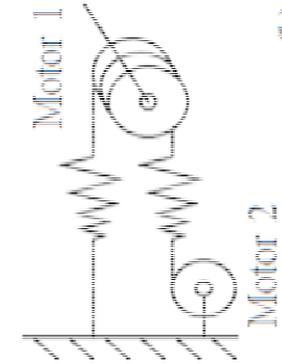
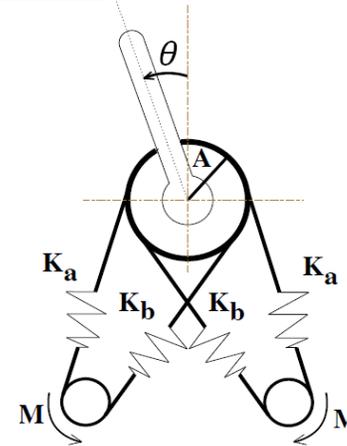
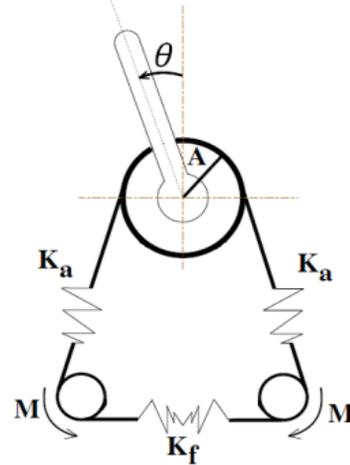
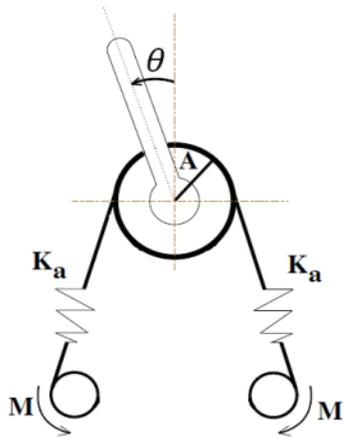


VSA Cube: Catalano *et al.* ICRA

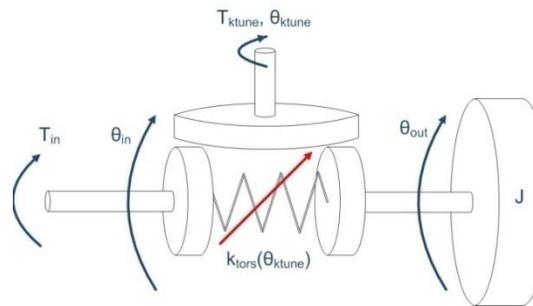
Variable Stiffness Actuators (VSAs)

Main configurations

Antagonistic



Serial

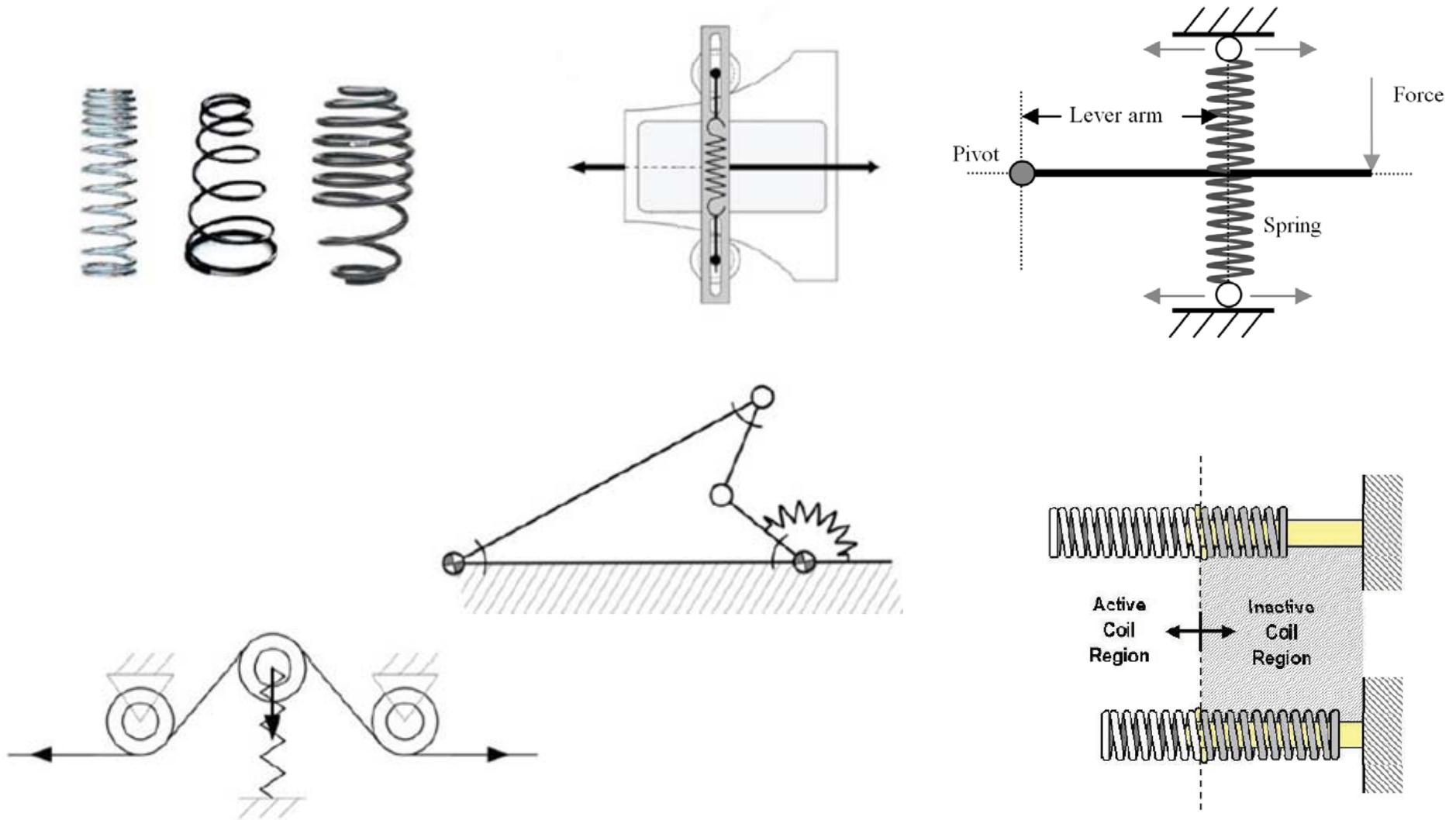


Variable Stiffness Actuators (VSAs)

Stiffness regulation principles

- Spring preloading
 - Stiffness is altered by changing the pretension of the nonlinear spring.
- Variable transmission
 - Stiffness regulation is achieved by changing the transmission ratio between the output link
- Modification of spring properties
 - The physical structure of the spring is mechanically modified

Mechanisms for generating nonlinear spring forces

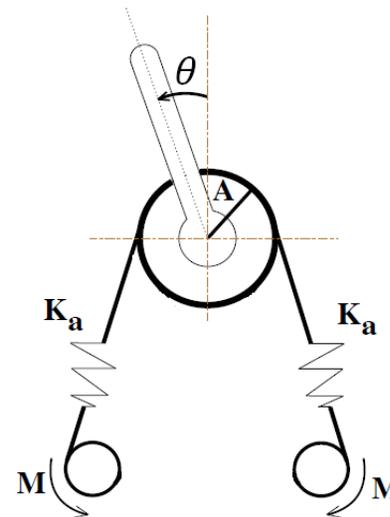
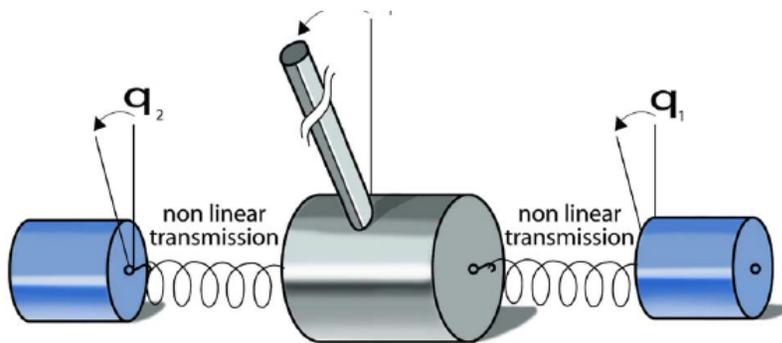
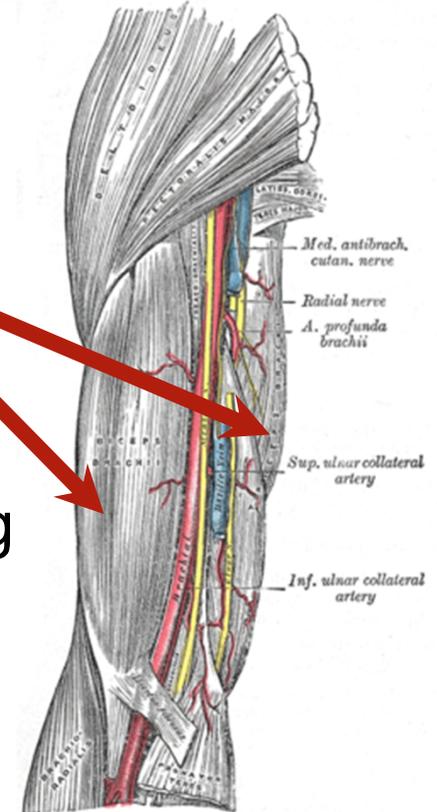


Simple antagonistic arrangement

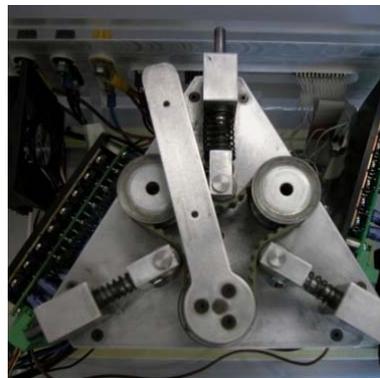
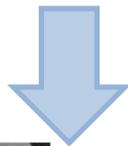
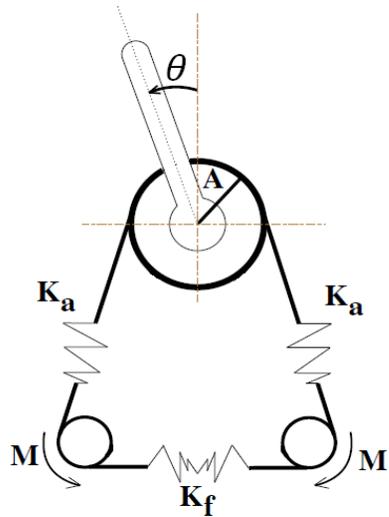
- Bio-inspired configuration
- In the human body, each joint is actuated by - *at least* – two muscles

Conventional mechatronic realization

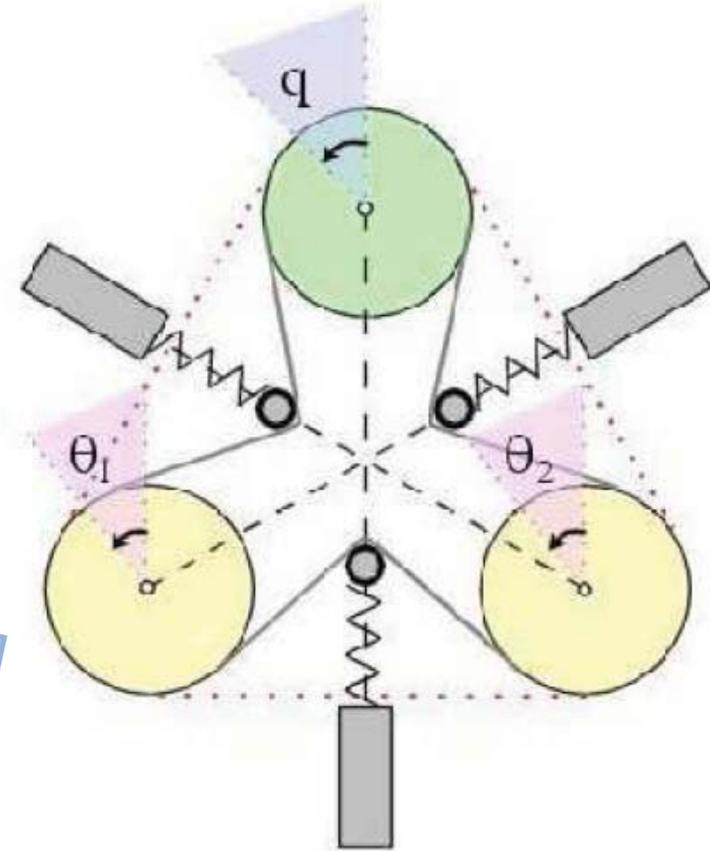
- Two actuators with a single direction coupling
- A pair of elastic elements



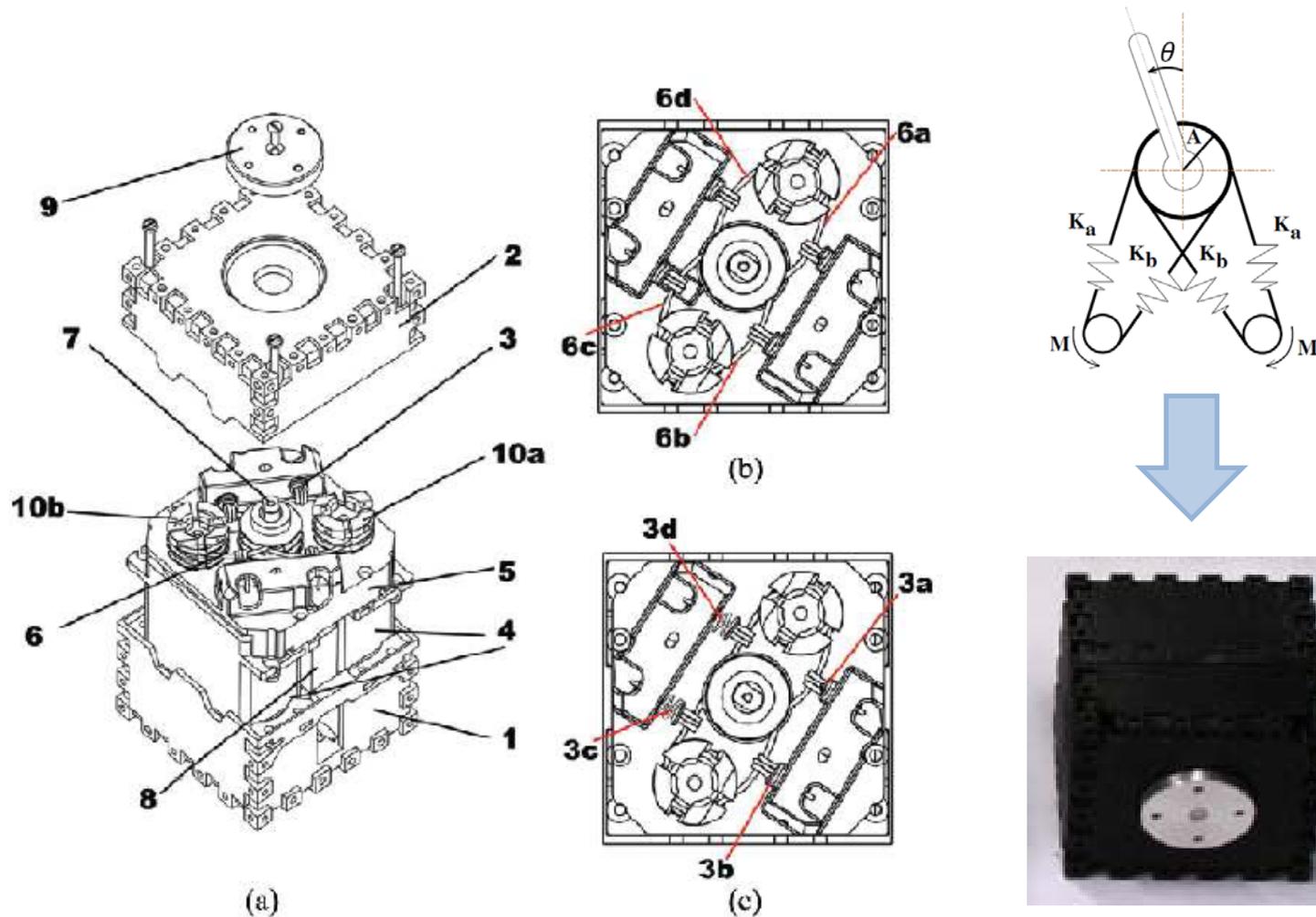
Cross – coupled antagonistic scheme



Tonietti, Bicchi, ICRA 2005

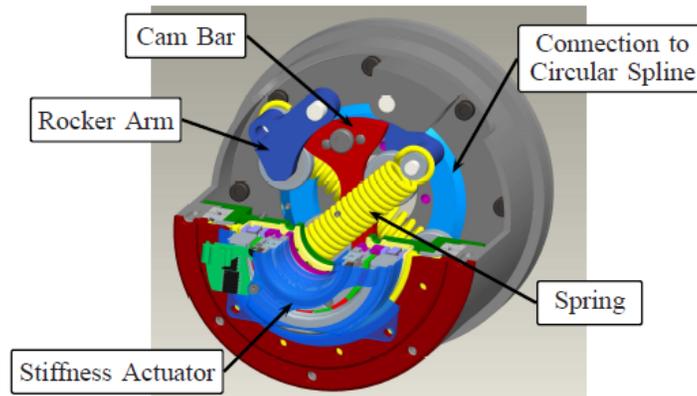
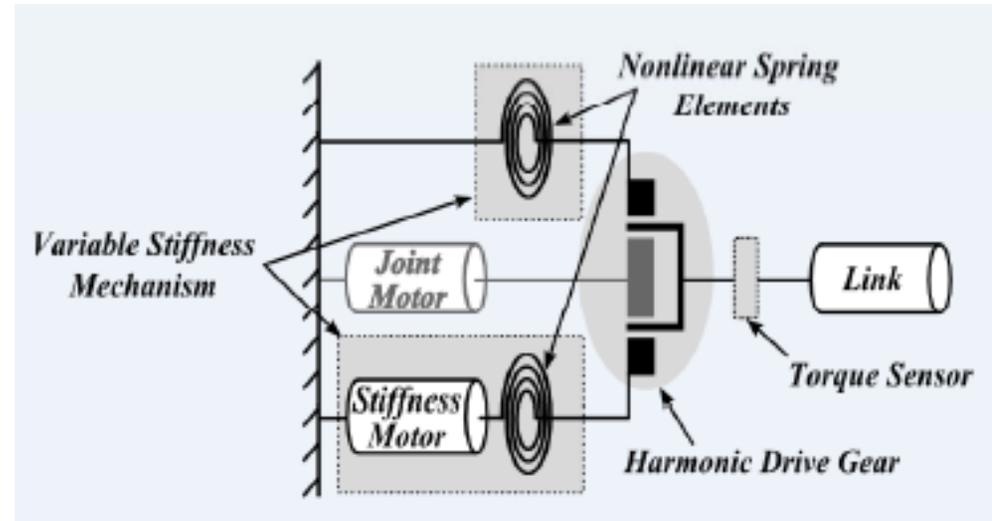
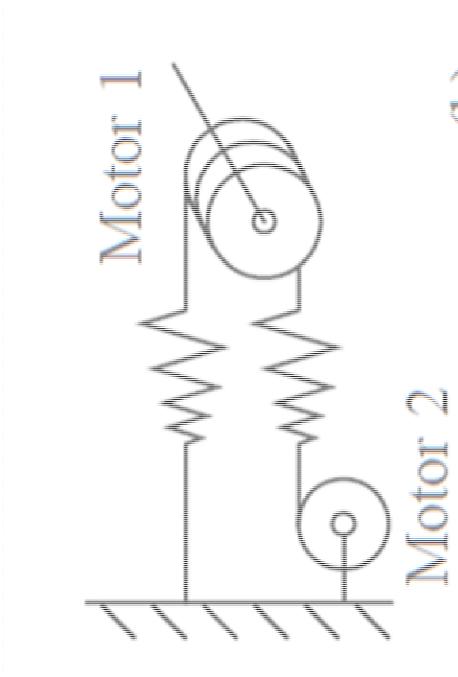


Cross – coupled and bilateral antagonistic schemes



VSA Cube: Catalano et al. ICRA 2011

Quasi Antagonistic Joint Mechanism



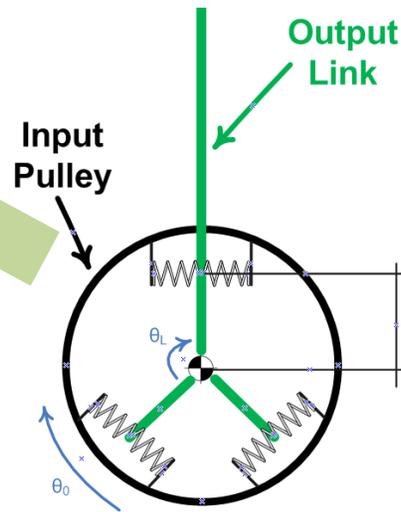
O. Eiberger et al. ICRA 2010

Alin Albu-Schäffer et al, RA Mag., 2008

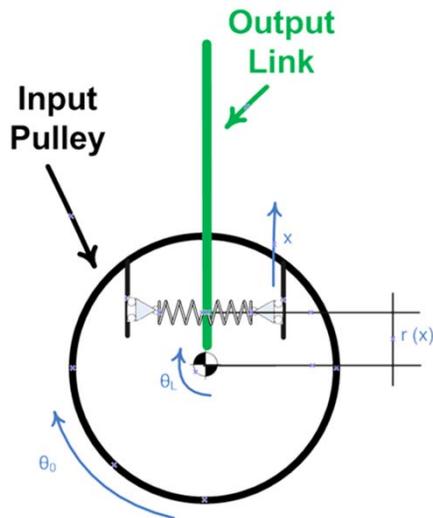
From CompAct to CompAct-VSA



Fixed stiffness joint



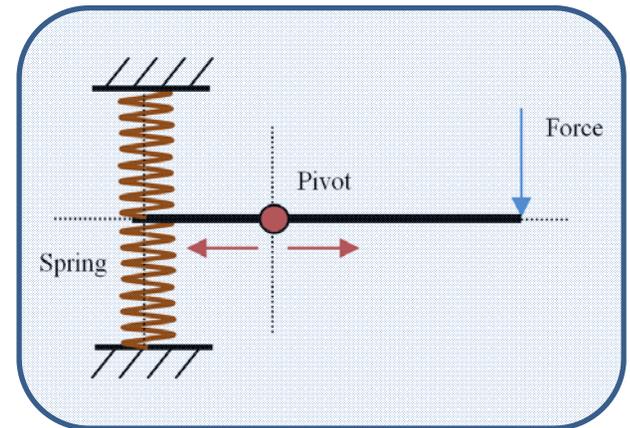
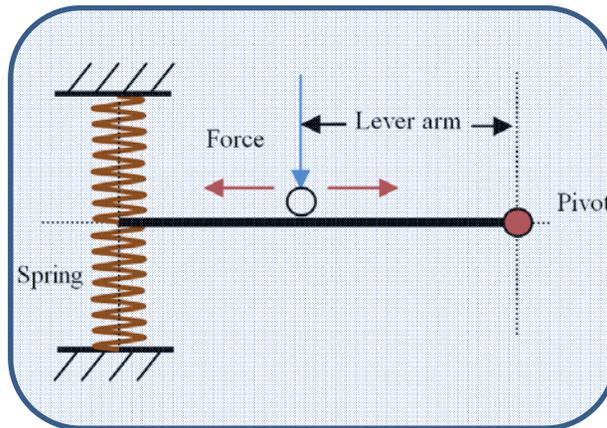
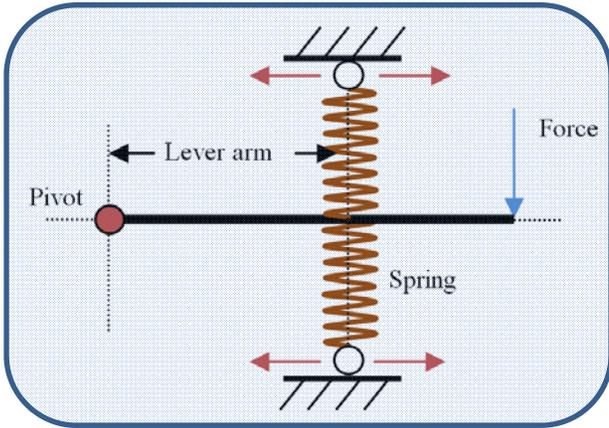
Variable stiffness joint



$$K_T = 6 \cdot K_S \cdot f(r^2)$$

Lever arm principle

Variable spring position



- Positions of the pivot and force point are fixed. Position of the spring is adjustable.
- The bigger is the lever arm, the stiffer is the link.
- The minimum stiffness is zero
- The maximum stiffness depends on the length of the lever and the stiffness of the



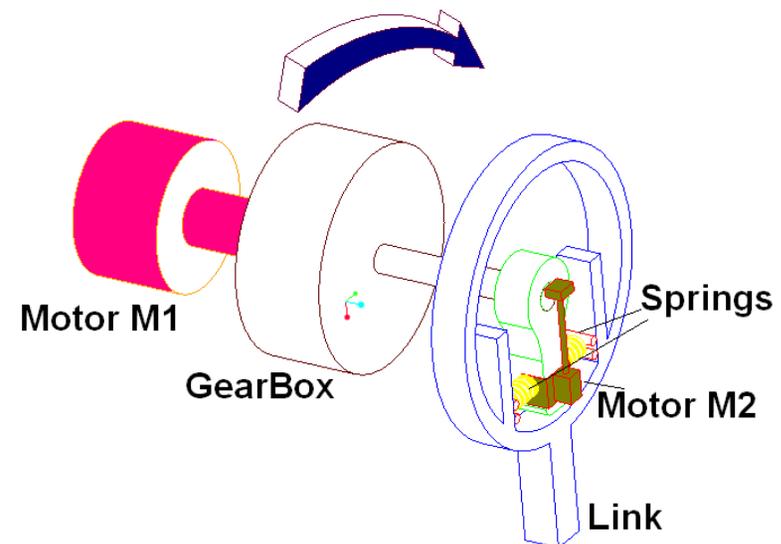
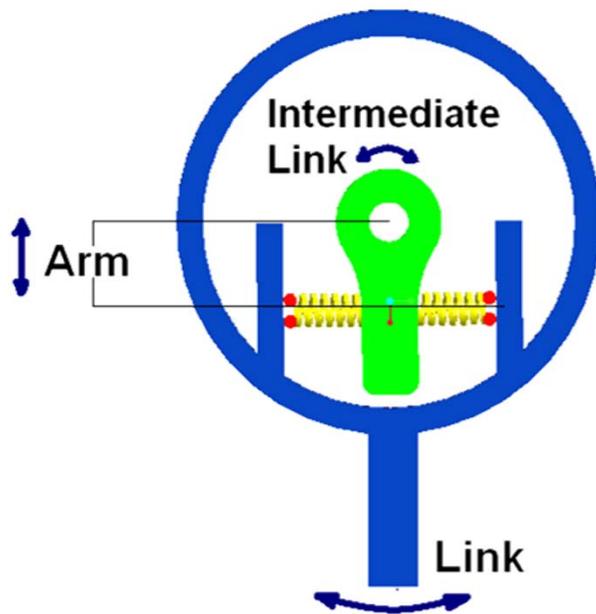
Hybrid actuator: Byeong-Sang Kim et al., ICRA 2010



AwAS: A. Jafari et al., IROS 2010

AwAS: Principle of operation

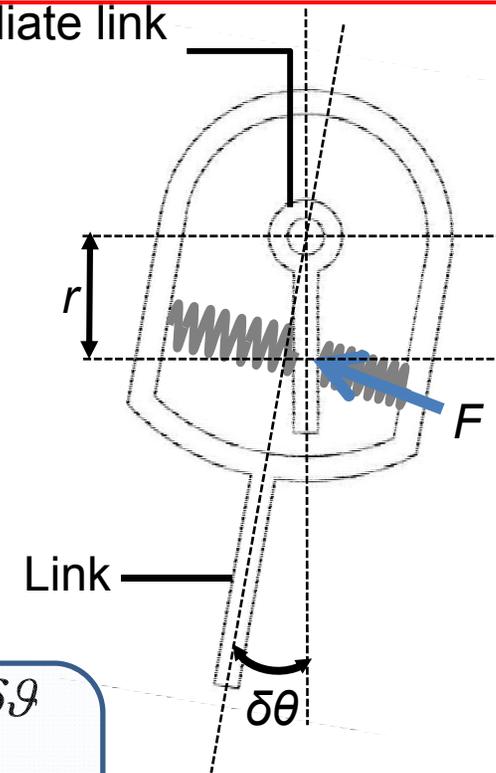
- Intermediate link is connected the motor M1;
- Springs are located between intermediate link and the link;
- Arm (variable) is the distance from the center of rotation to the attachment point of springs



(AwAS)-Principle of operation

Parameter	Description
r	Arm
$\delta\vartheta$	Angular deflection
K_s	Spring's rate
F	Resultant force of spring
p	Spring's pretension
δX	Spring's deflection
K	Stiffness
T	Overall torque

Intermediate link



$$F = K_s (p + \delta x) - K_s (p - \delta x) = 2K_s \delta x = 2K_s r \sin \delta\vartheta$$

$$T = F \cdot r \cdot \cos \delta\vartheta = 2 \cdot K_s \cdot r^2 \cdot \sin \delta\vartheta \cdot \cos \delta\vartheta$$

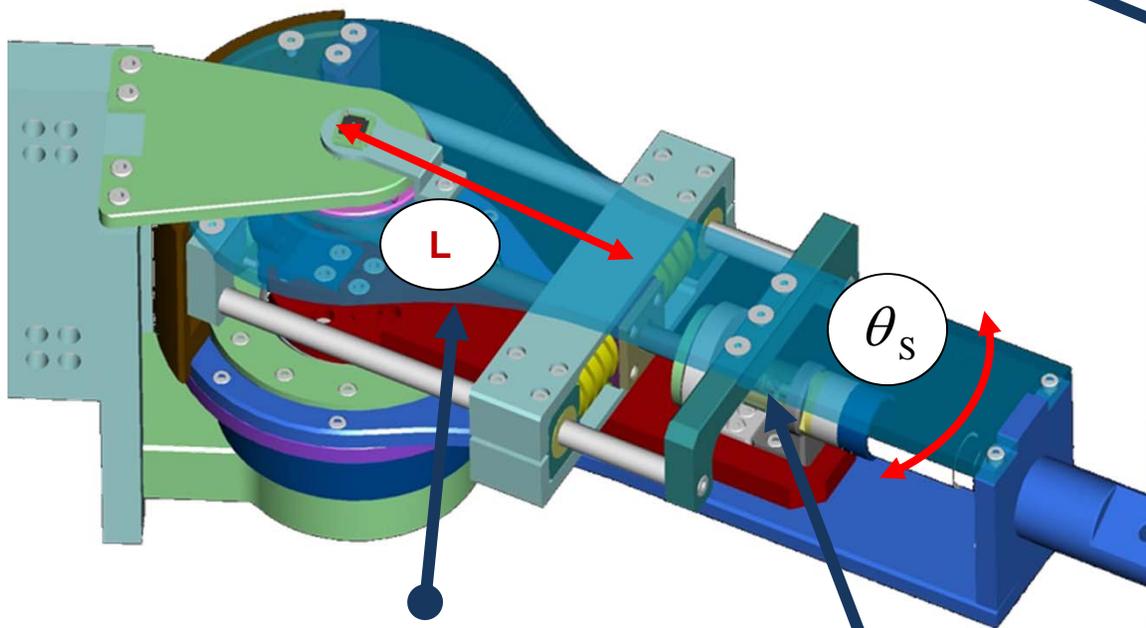
$$K = \frac{dT}{d\theta} = 2 \cdot K_s \cdot r^2 \cdot (2 \cdot \cos^2 \delta\vartheta - 1)$$

At equilibrium position, force F generated by the springs is perpendicular to the displacement needed to change the stiffness.

AwAS:Assembly

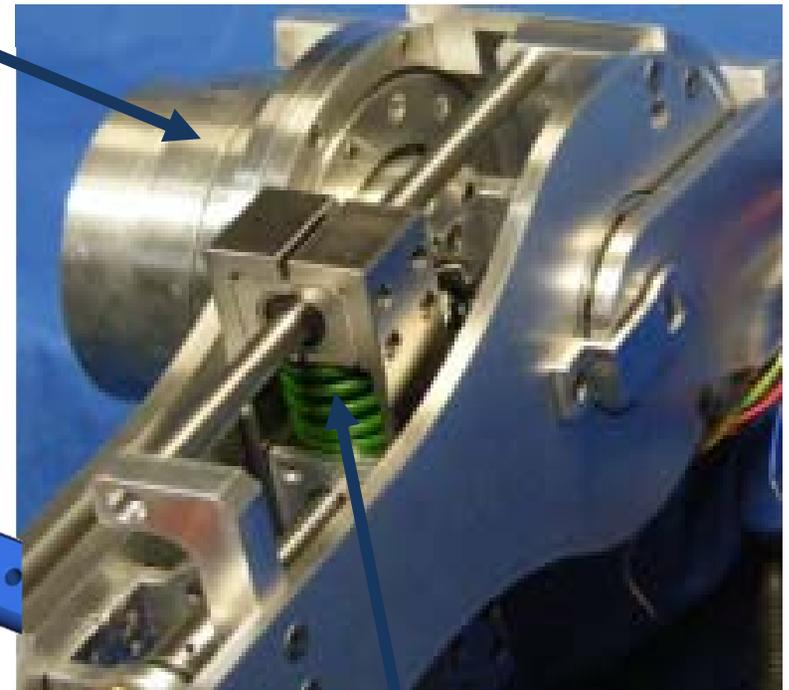
$$K = 2 \cdot K_s \cdot L^2 \cdot f(\theta_s)$$

Main actuator



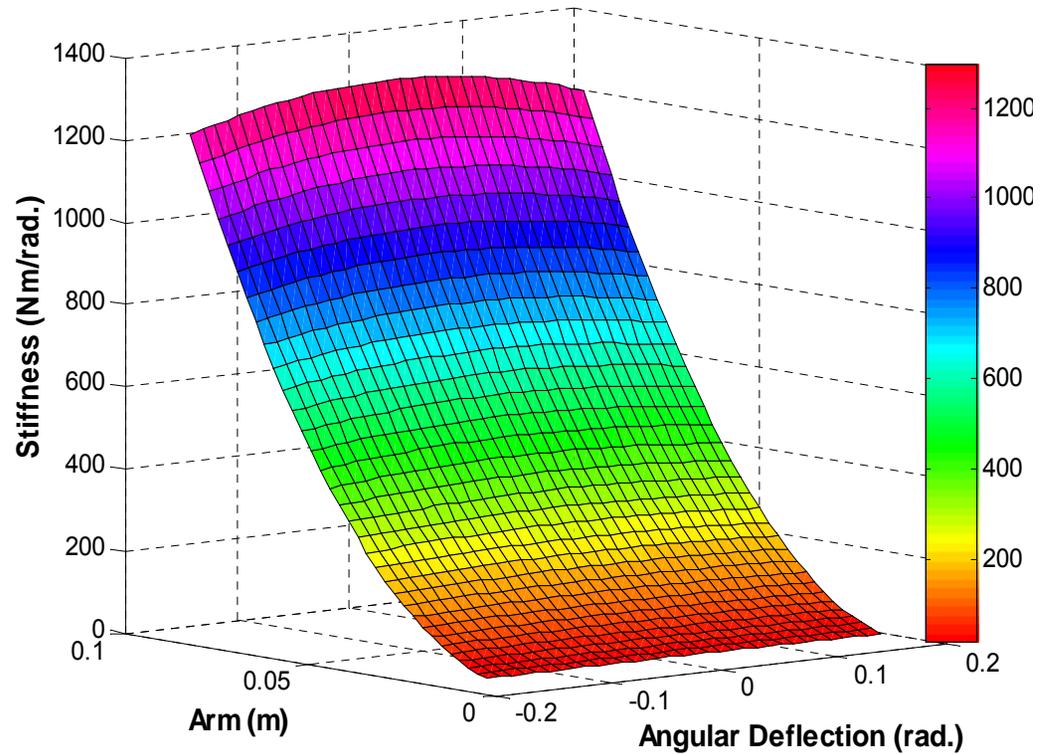
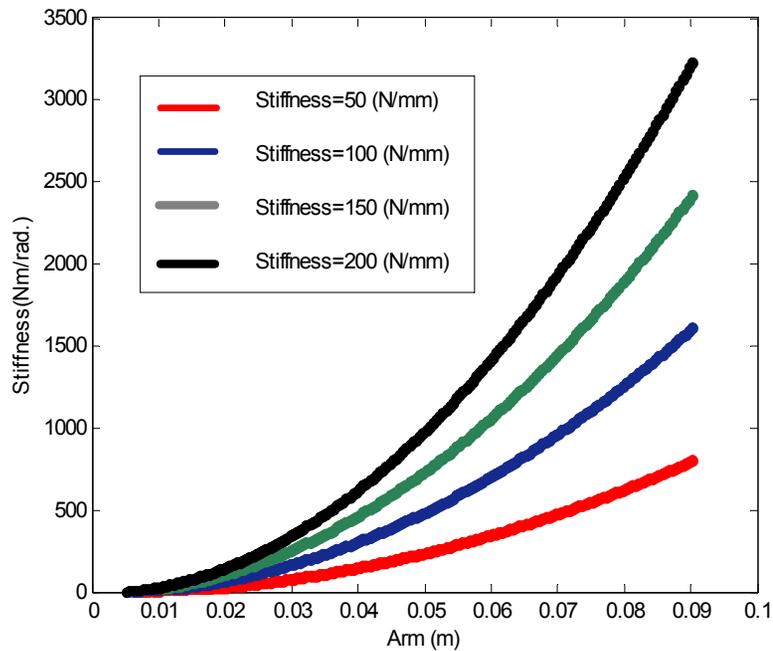
Intermediate link

Lever arm drive
(stiffness adjuster)



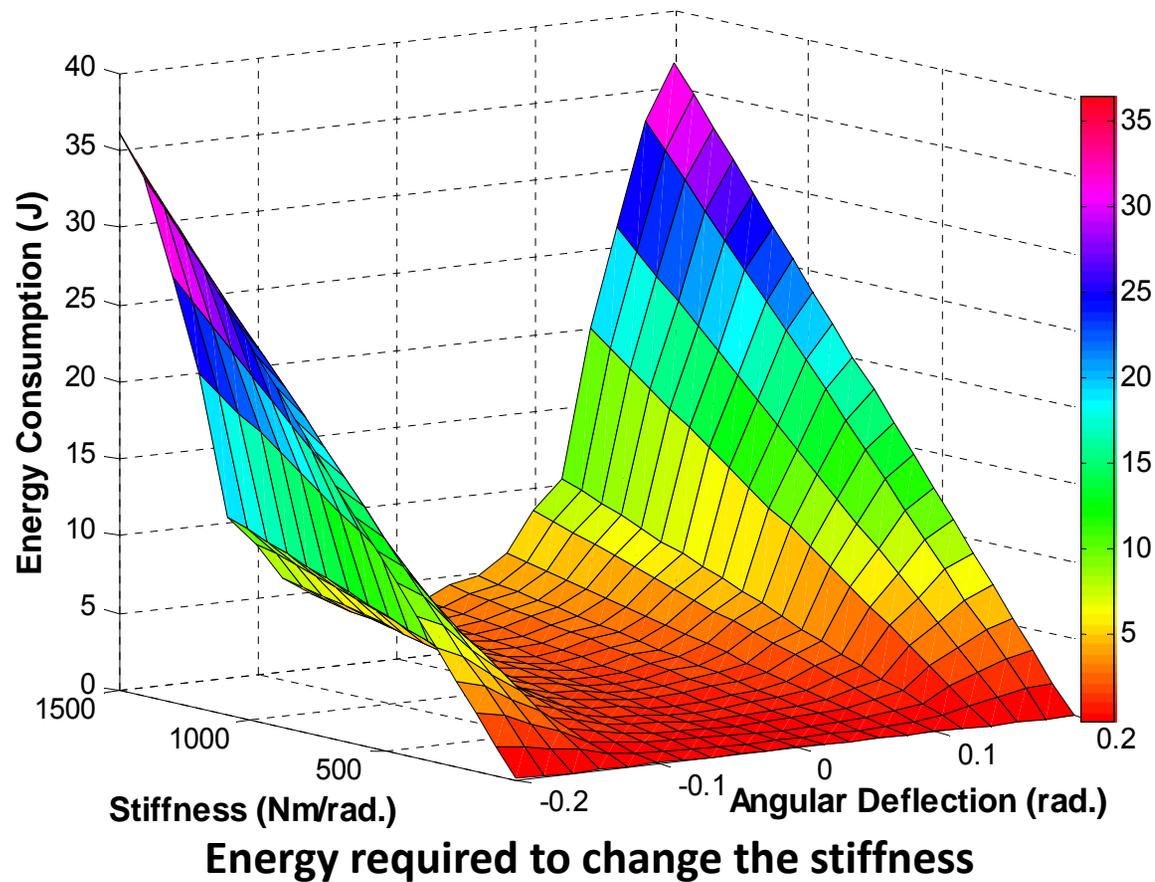
Spring coupling

Stiffness regulation

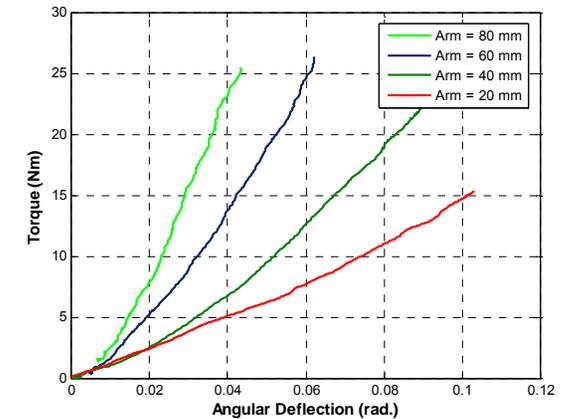
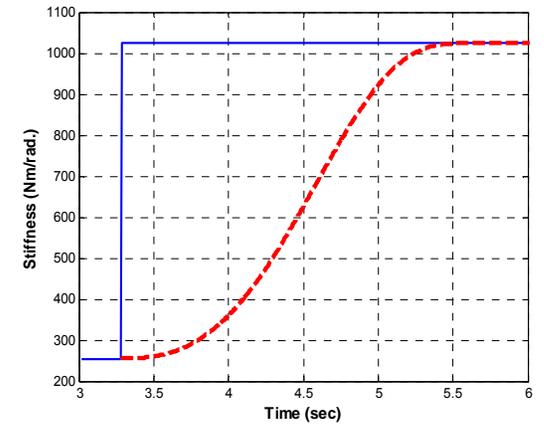
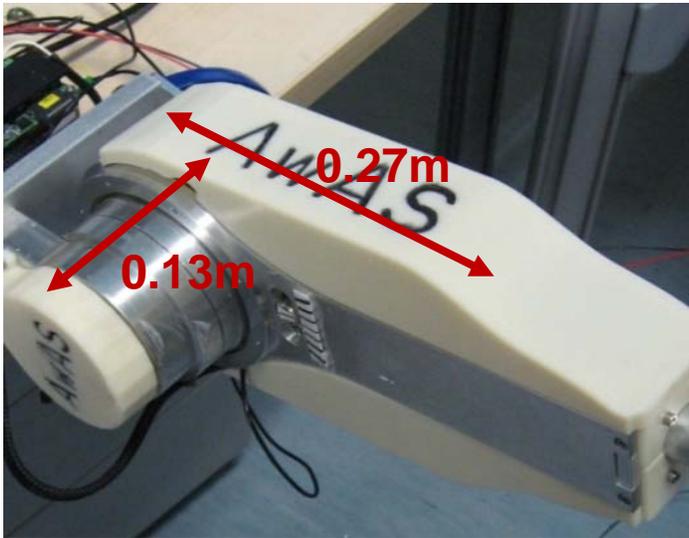


Stiffness of the springs and maximum arm length are 80N/mm and 0.09m, respectively

Experimental measures of energy

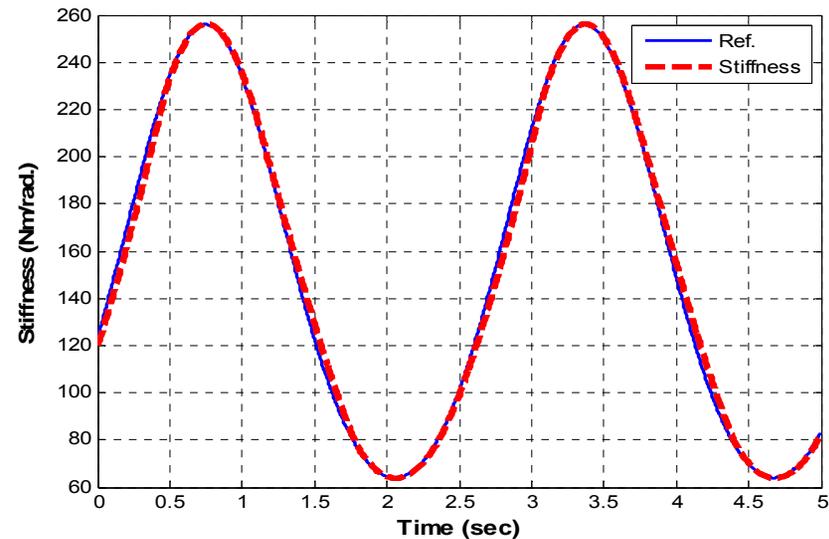
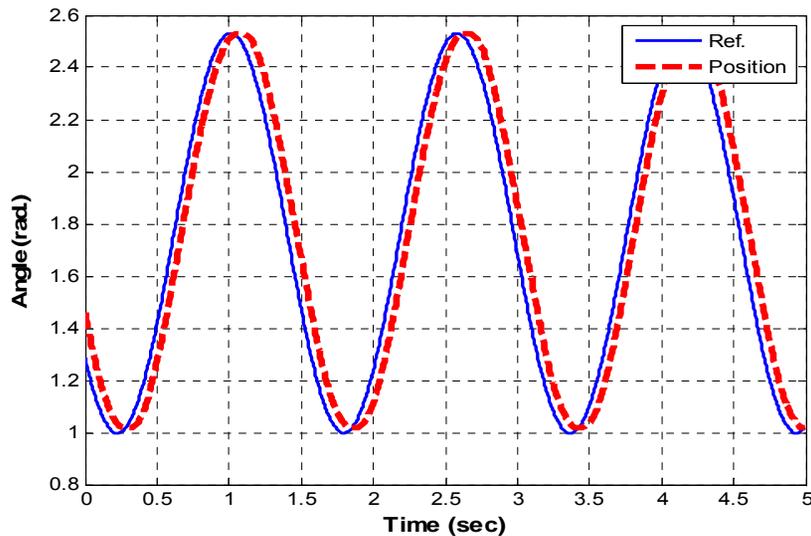


AwAS: Specifications



Range of Motion (rad)	Range of Stiffness (Nm/rad)	Passive Angular Deflection (rad)	Max Stiffness regulation speed (Nm/rad sec)	Energy Storage (J)	Output Torque (Nm)	Weight (Kg)
-2,+2	30,1800	-0.2,+0.2 at 640Nm/rad	800	3.5	80	1.4

Tracking position and stiffness



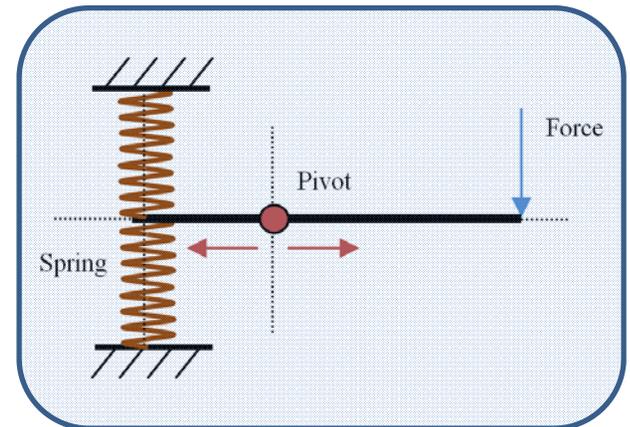
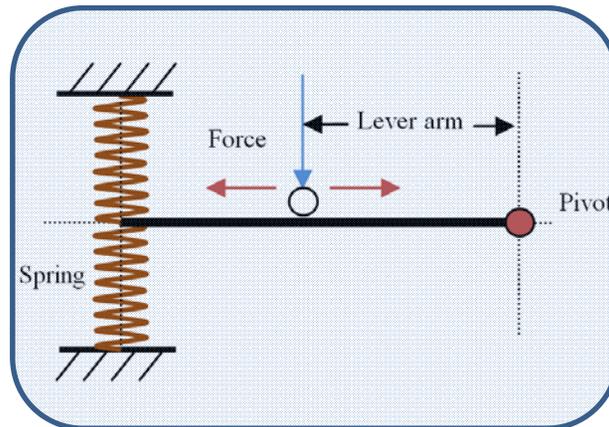
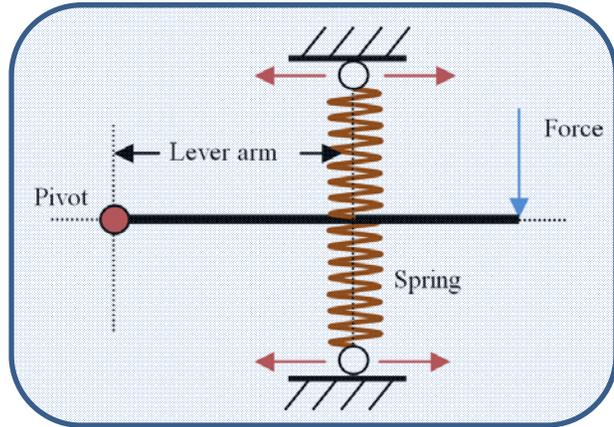
Both motors M1 for position and M2 for stiffness were simultaneously controlled to follow sinusoidal position and stiffness trajectories of different frequencies

AwAS prototype

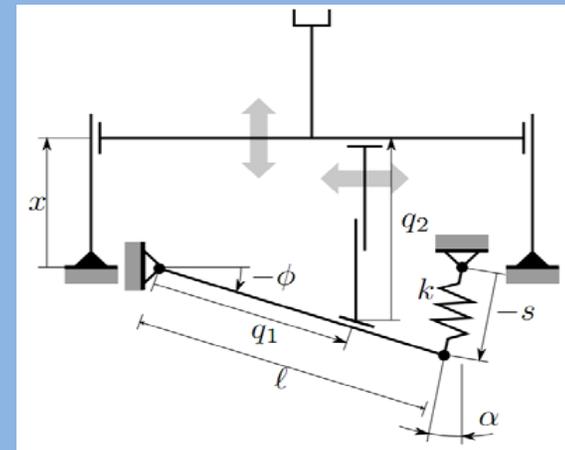


Lever arm principle

Variable force application point



- Positions of the pivot and spring are fixed.
- Position of the force point is adjustable.
- The shorter is the lever arm, the stiffer is the link.
- The maximum stiffness is infinite. The minimum stiffness depends on the length of the lever and the stiffness of the springs.

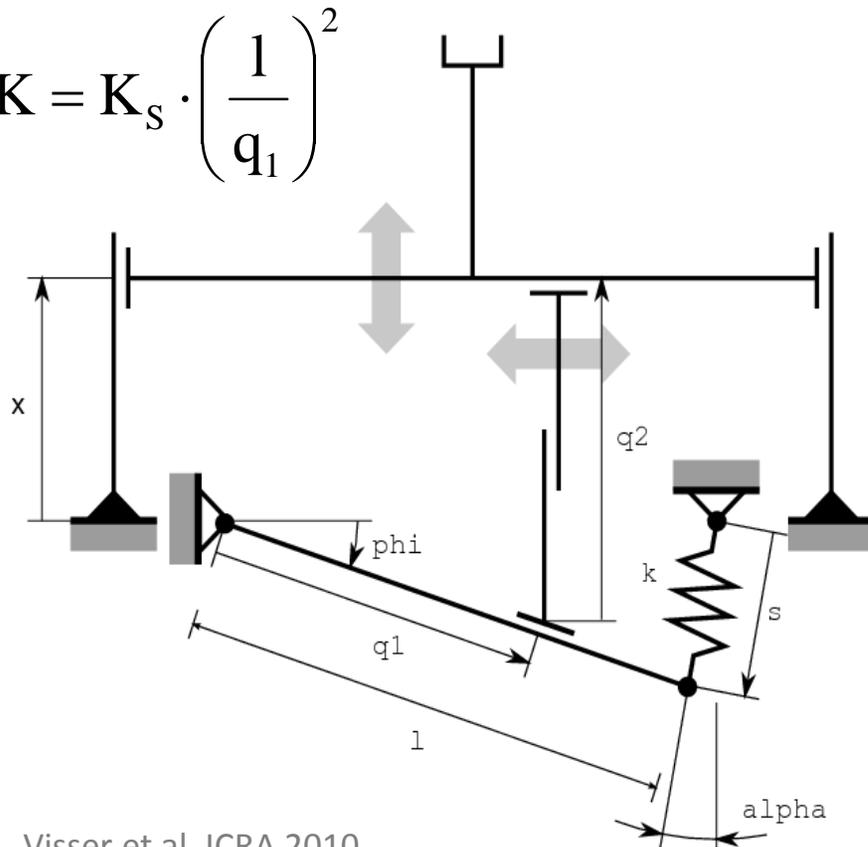


Energy Efficient VSA:
L.C. Visser *et al.*, ICRA 2010

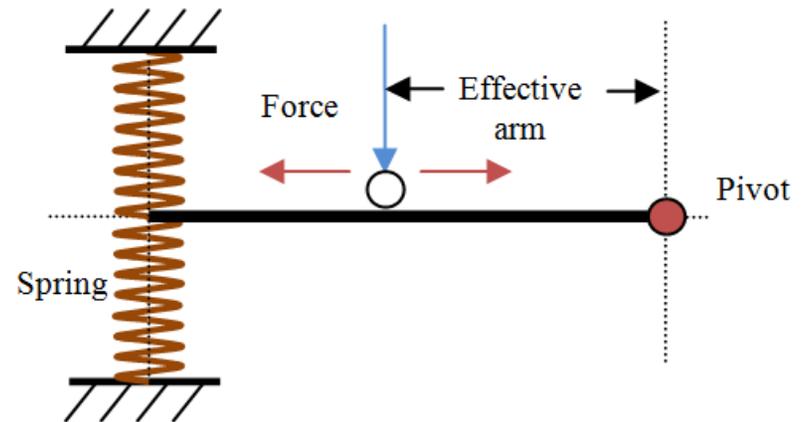
Lever arm principle

Variable force application point

$$K = K_s \cdot \left(\frac{1}{q_1} \right)^2$$

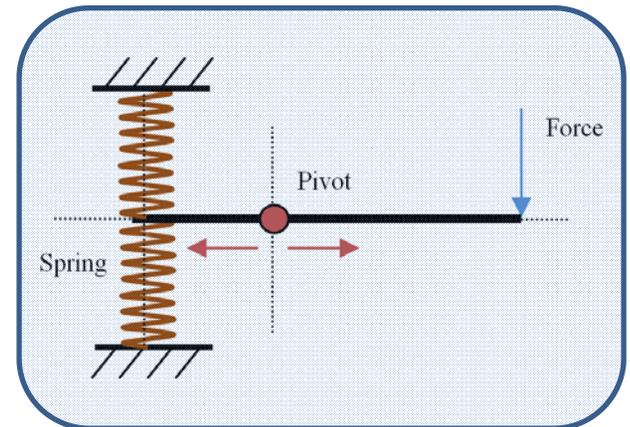
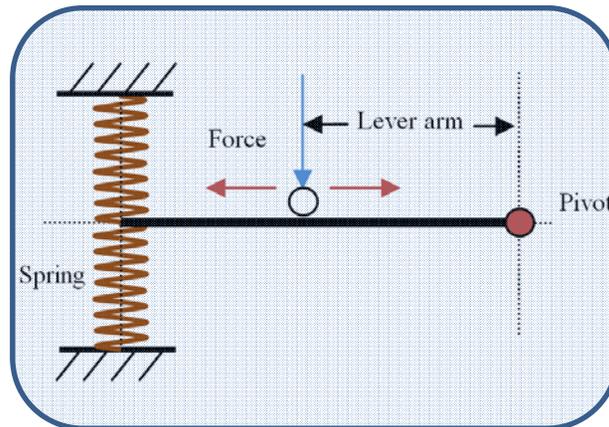
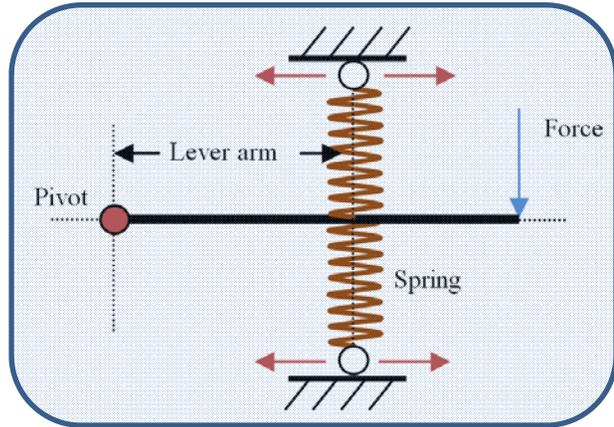


Visser et al, ICRA 2010

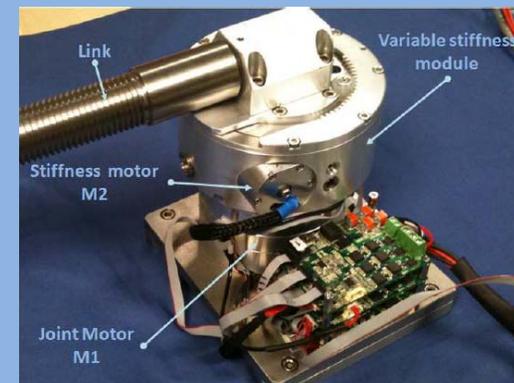


Lever arm principle

Variable pivot position

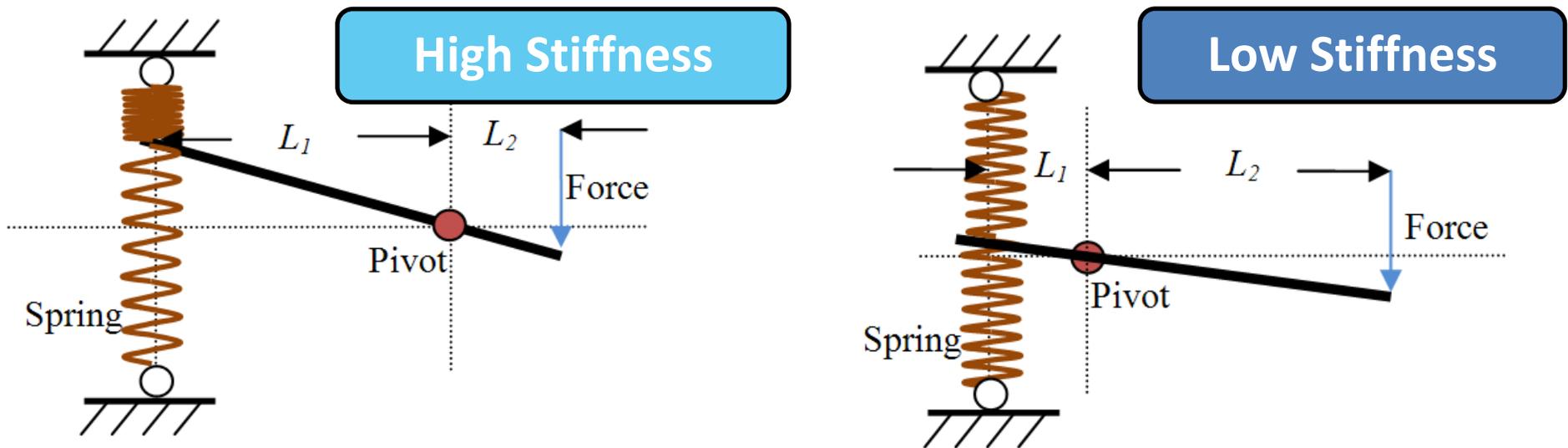


- Positions of the spring and force point are fixed. Position of the pivot is adjustable.
- The closer is the pivot to the force point, the stiffer is the link.
- The minimum stiffness is zero. The maximum stiffness is infinite. This range does not depend on the length of the lever and the stiffness of the springs.



CompAct VSA
Tsagarakis *et al.*, IROS 2011

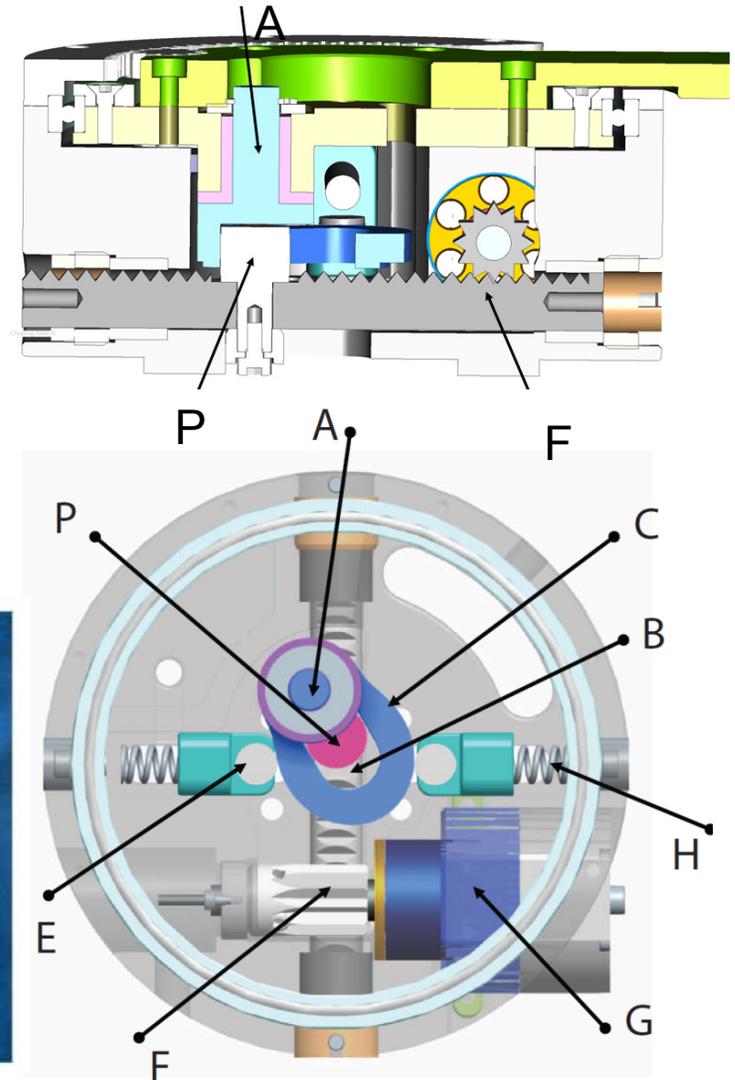
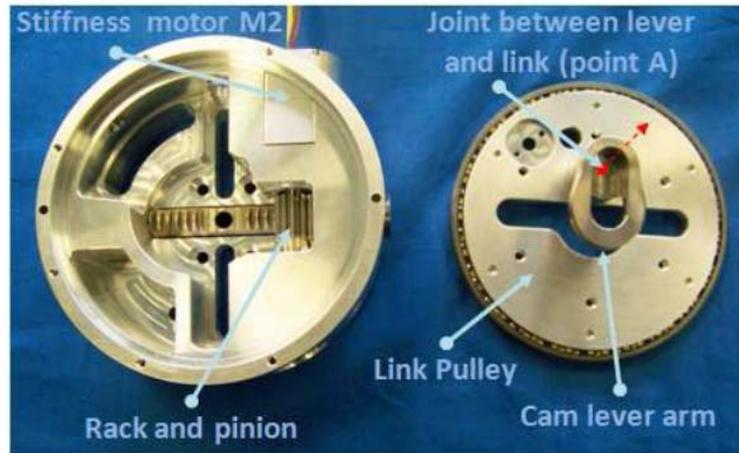
CompAct-VSA: Lever arm with variable pivot point principle



CompAct-VSA: Realization

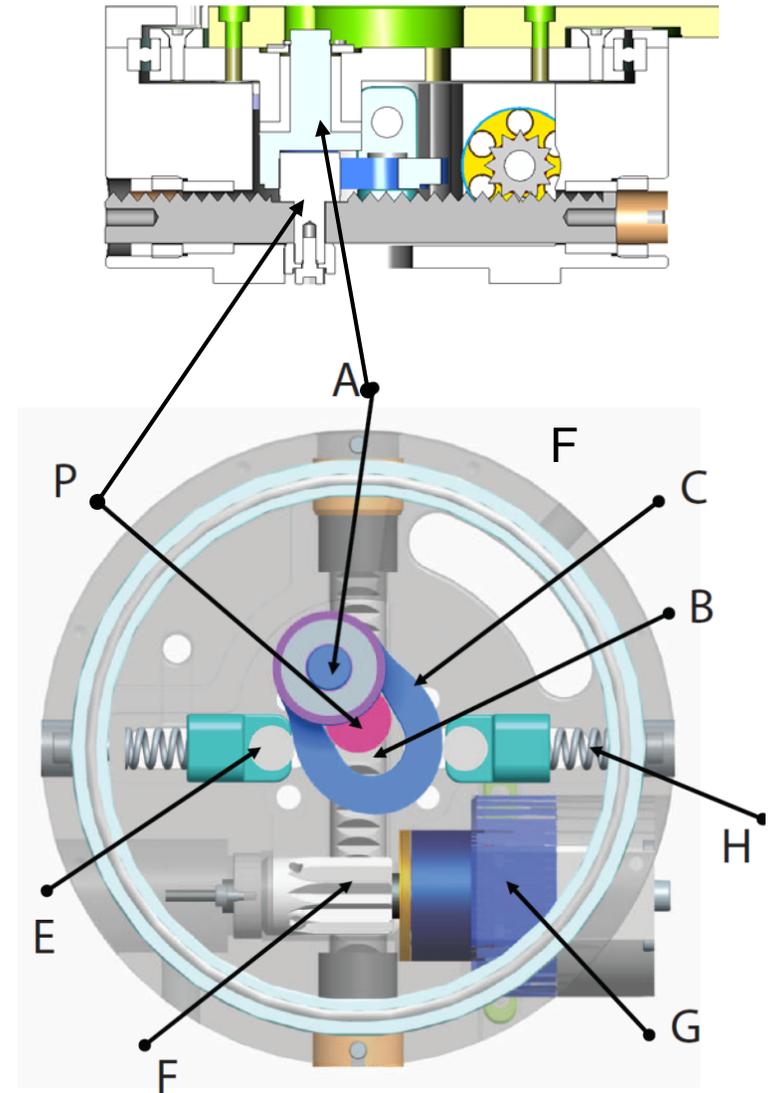
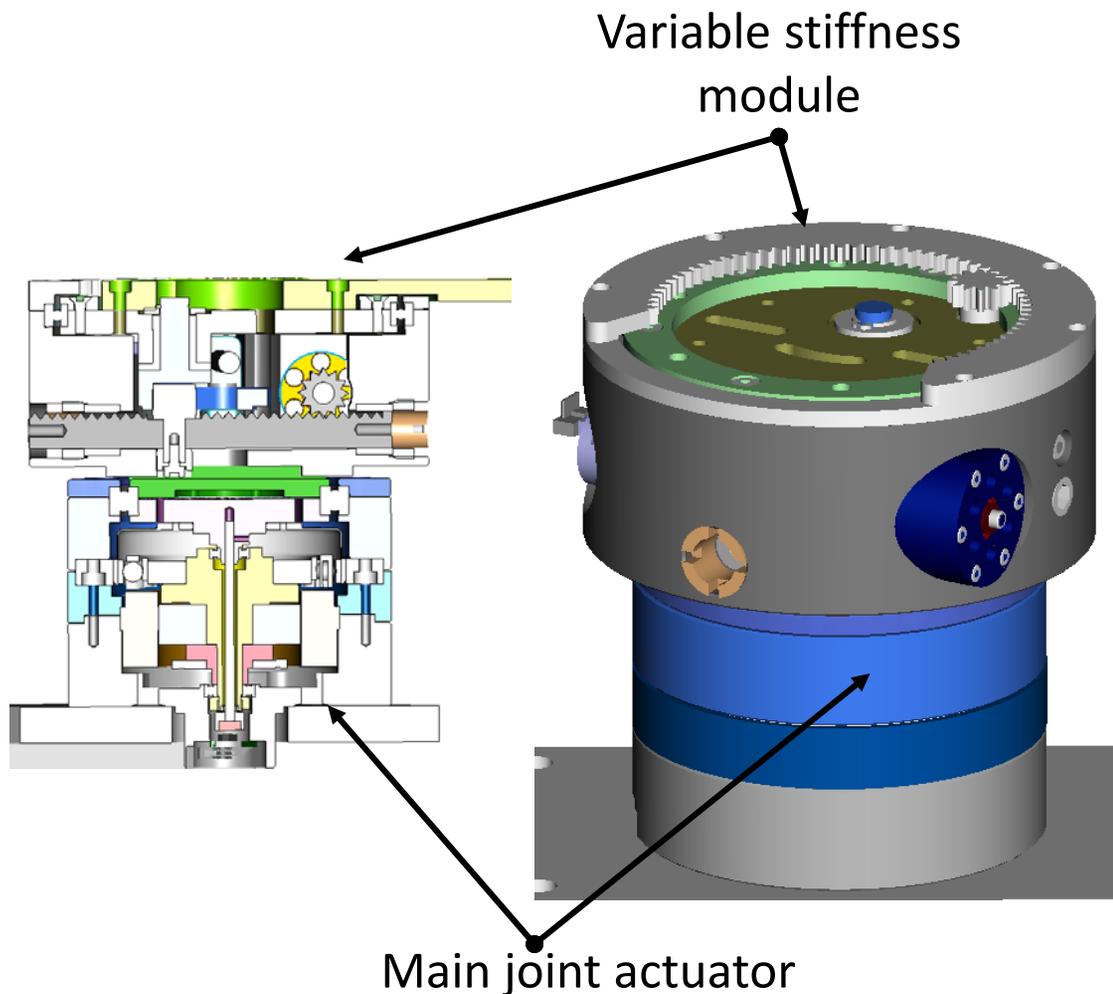
Variable Stiffness Module

- A) Link/Cam Connection
- B) Joint Axis
- C) Cam Shaped Lever Arm
- E) Cam Roller
- F) Rack/Pinion
- G) Stiffness Motor
- H) Springs
- P) Pivot Point



CompAct-VSA: Realization

Full Assembly



CompAct-VSA: Stiffness model

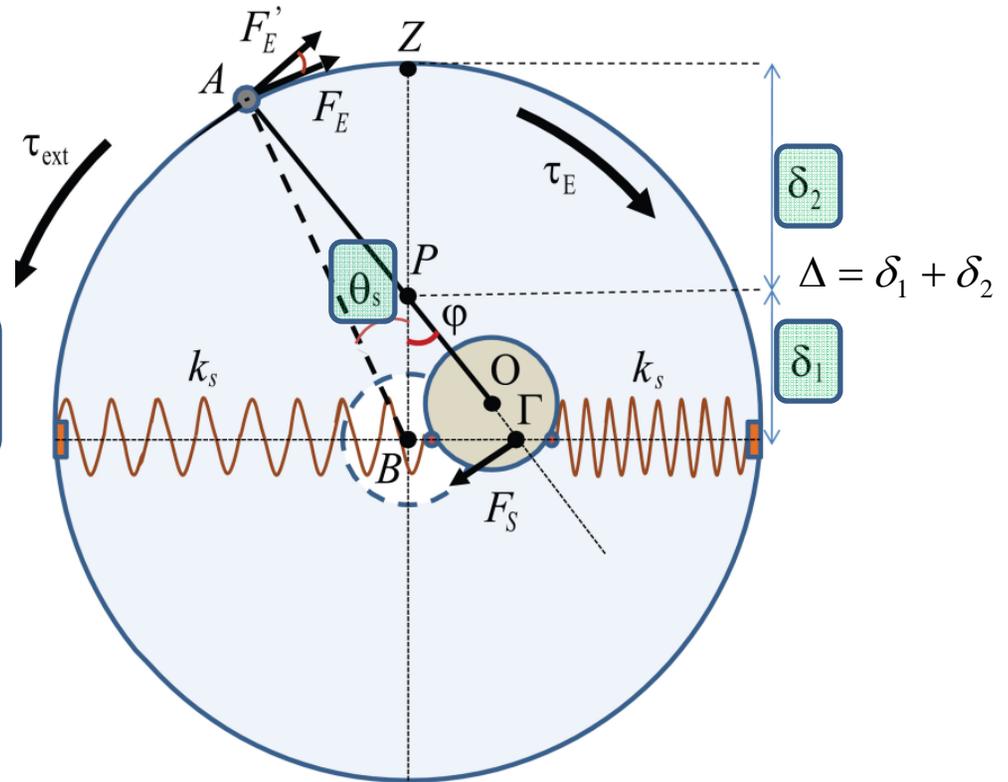
- Elastic torque $\tau_E = \frac{2k_s \delta_1^2 \Delta^2 \theta_s}{(\Delta - \delta_1)^2}$



- Stiffness $K = \frac{2k_s \delta_1^2 \Delta^2}{(\Delta - \delta_1)^2}$

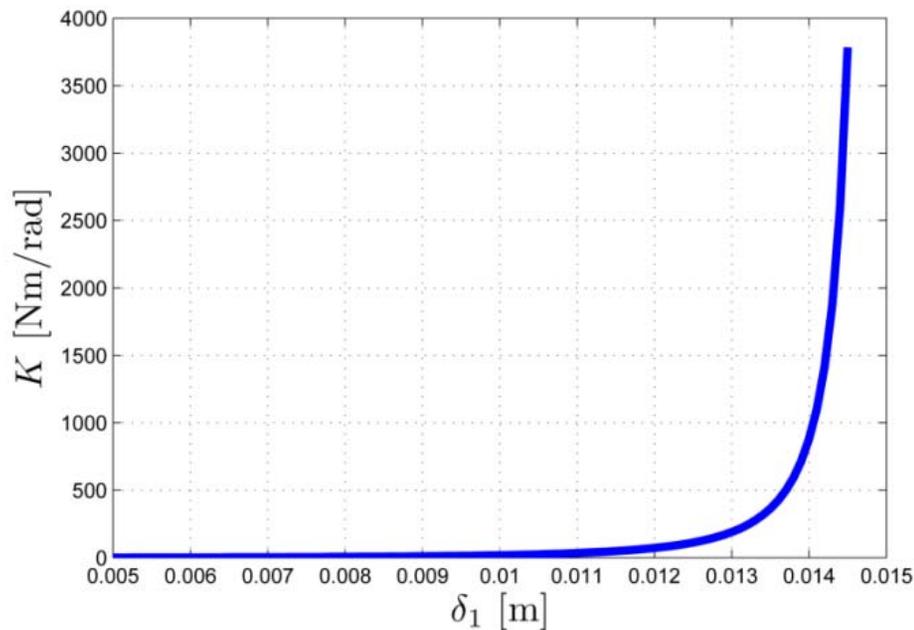
- Torque of the pivot motor

$$|\tau_R = \frac{2k_s n^2 \theta_2 \theta_s^2 \Delta^3}{(\Delta - n\theta_2)^3}$$

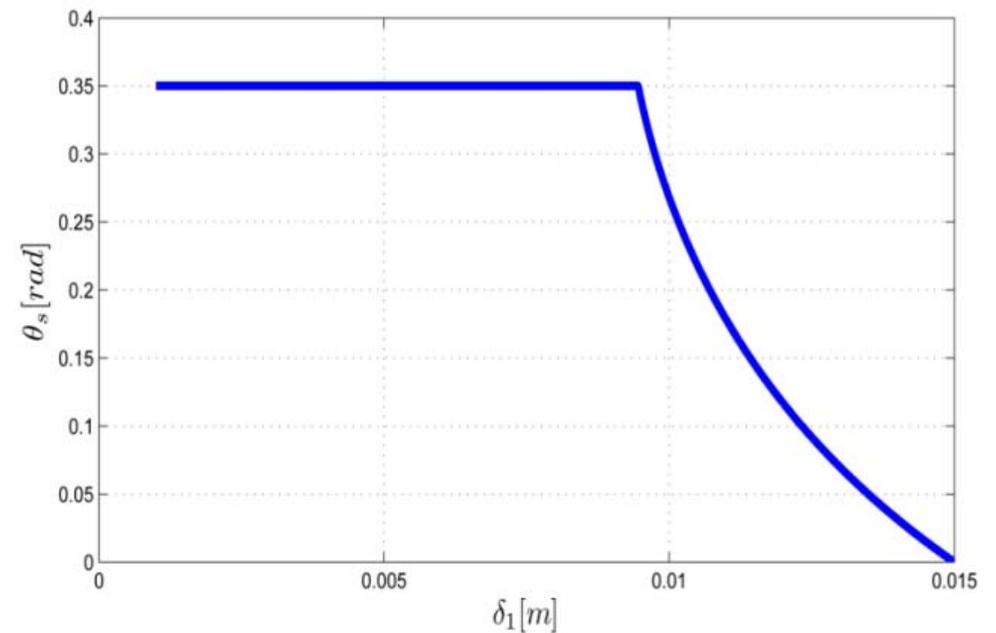


Stiffness & Passive deflection profiles

Stiffness
$$K = \frac{2k_s \delta_1^2 \Delta^2}{(\Delta - \delta_1)^2}$$



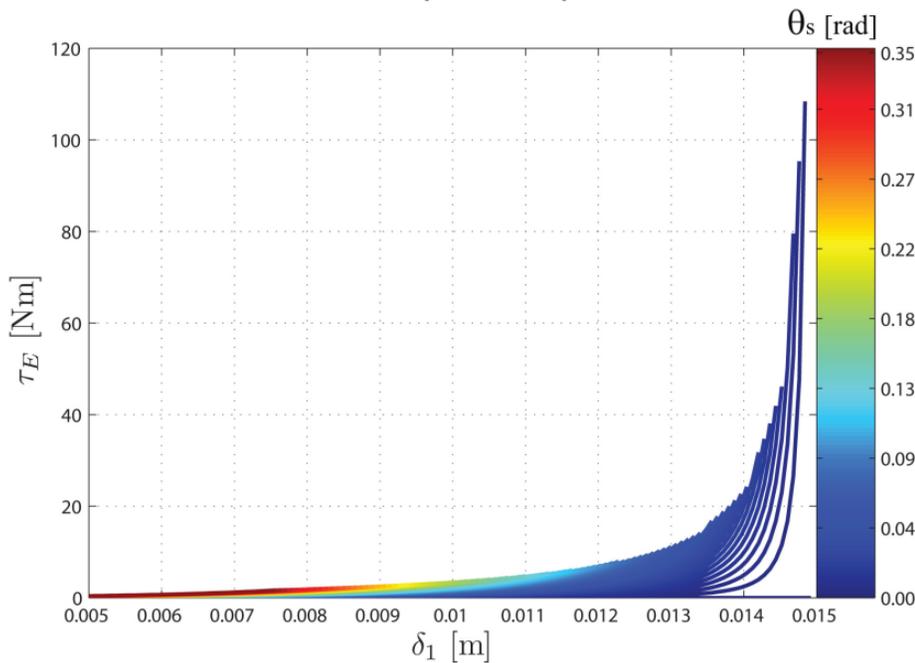
Passive deflection angle range



Elastic and pivot motor torques

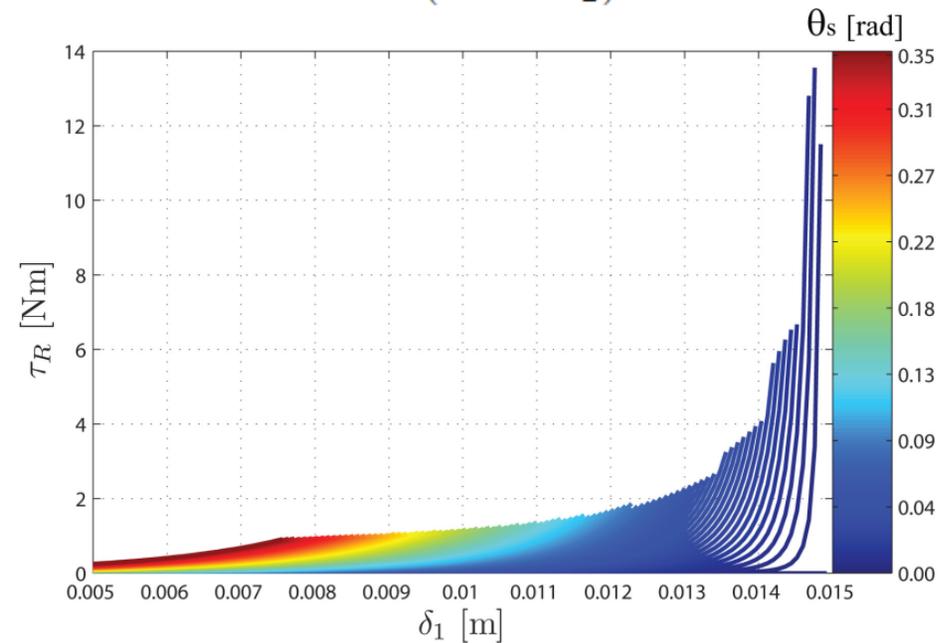
Elastic torque

$$\tau_E = \frac{2k_s \delta_1^2 \Delta^2 \theta_s}{(\Delta - \delta_1)^2}$$



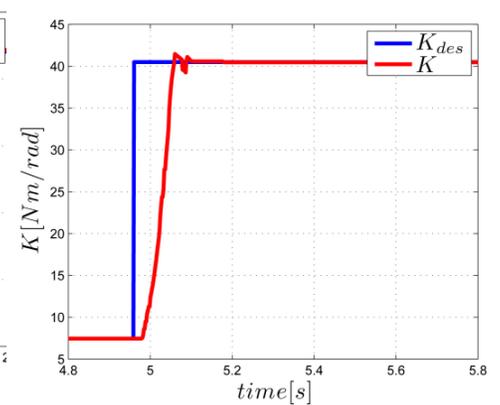
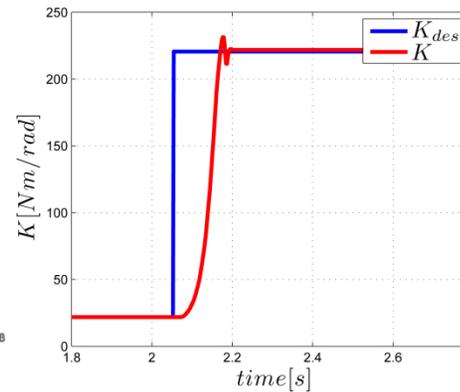
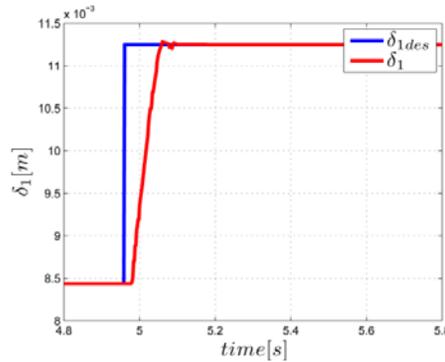
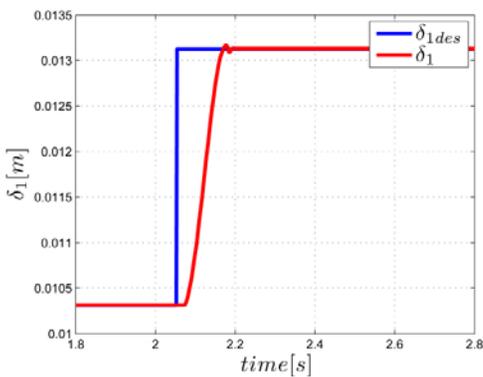
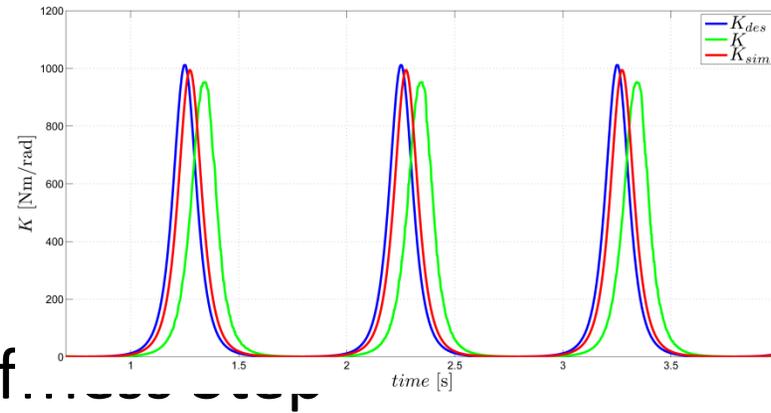
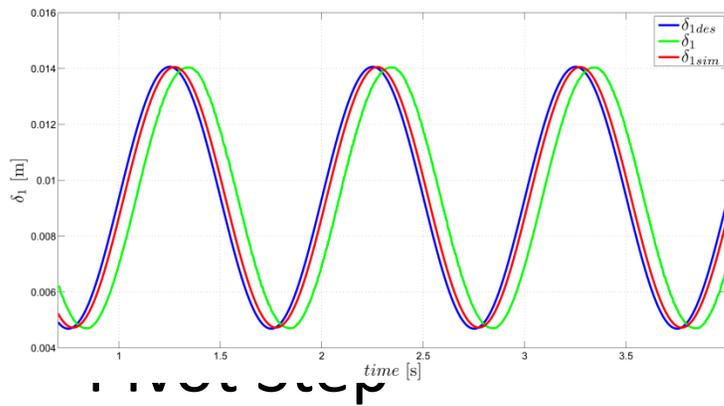
Resistant torque of the pivot motor

$$|\tau_R| = \frac{2k_s n^2 \theta_2 \theta_s^2 \Delta^3}{(\Delta - n\theta_2)^3}$$

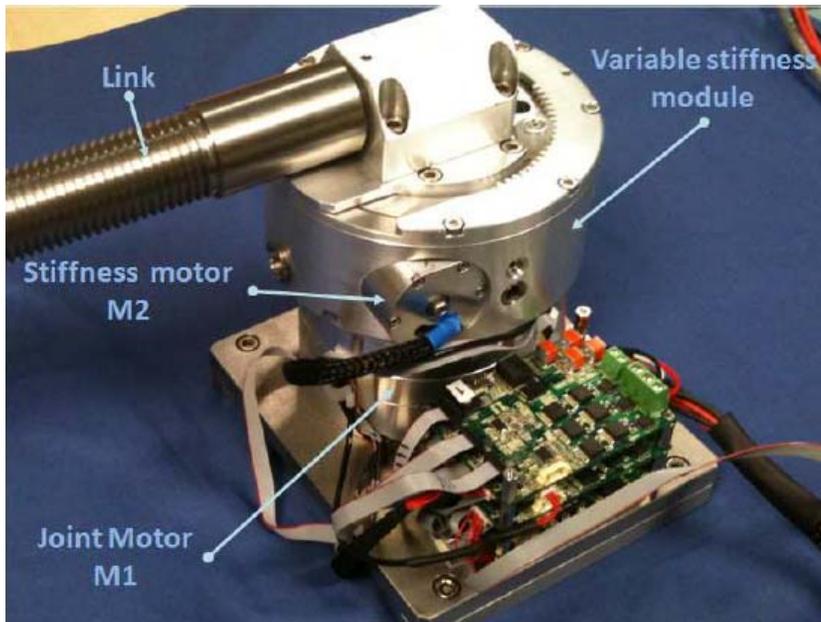


- Pivot Tracking

Stiffness Tracking



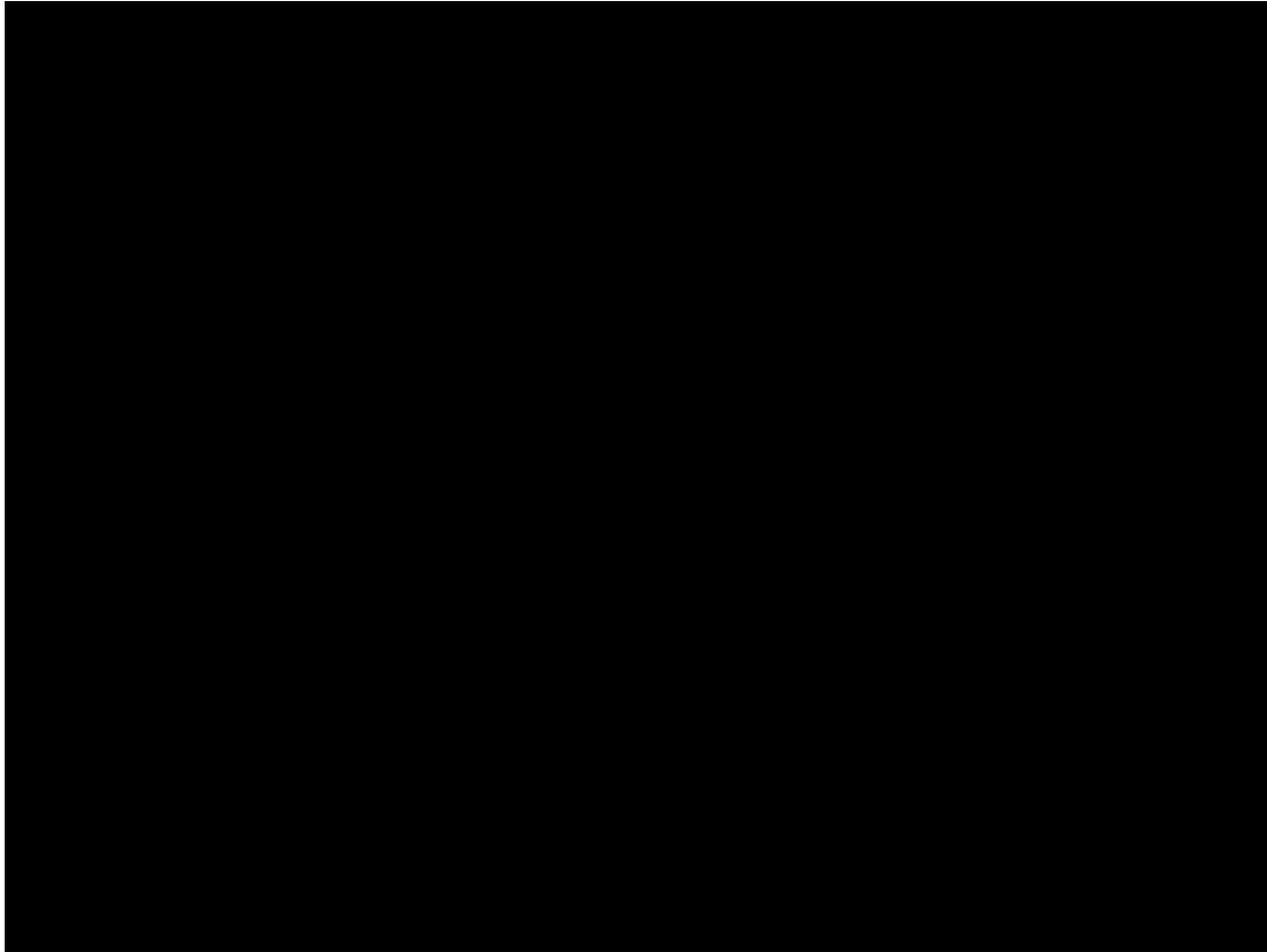
CompAct-VSA: Prototype



Tsagarakis *et al.*, IROS 2011

	CompAct-VSA	AwAS-II	AwAS
Range of Motion (deg)	+/-150°	+/-150°	+/-120°
Range of Stiffness (Nm/rad)	0 ~ rigid	0 ~ rigid	30~130 0
Time to change the stiffness (s)	~0.2sec	~1	3.5
Energy storage (J)	0.35	3.3	3.2
Peak Output Torque (Nm)	117	80	80
Length (m)	0.10	0.18	0.27
Width (m)	0.11	0.14	0.13
Overall Weight (Kg)	1.1	1.4	1.8

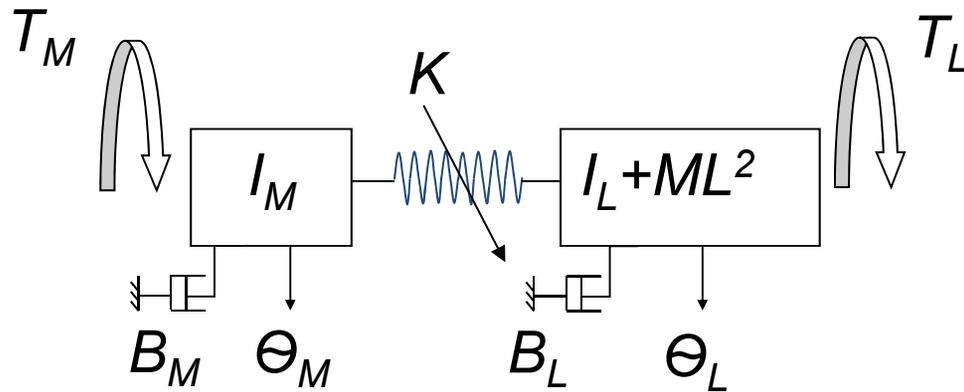
CompAct-VSA prototype



Compliance actuation benefits and challenges

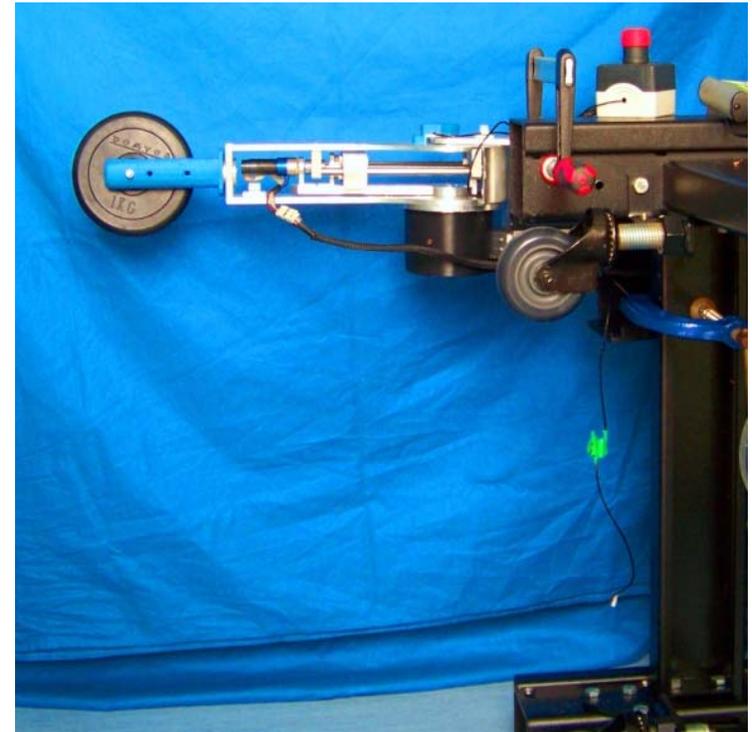
- intrinsic robustness against impacts
- passive adaptability to interaction
- high fidelity force/torque control
- peak power generation
- energy efficiency

Exploiting natural dynamics with AwAS



$$\begin{cases} (I_L + ML^2)\ddot{\theta}_L + B_L\dot{\theta}_L + K(\theta_L - \theta_M) = T_L \\ I_M\ddot{\theta}_M + B_M\dot{\theta}_M + K(\theta_M - \theta_L) = T_M \end{cases}$$

$$f_n = \frac{1}{2\pi} \sqrt{\frac{K}{(I_L + ML^2)}}$$

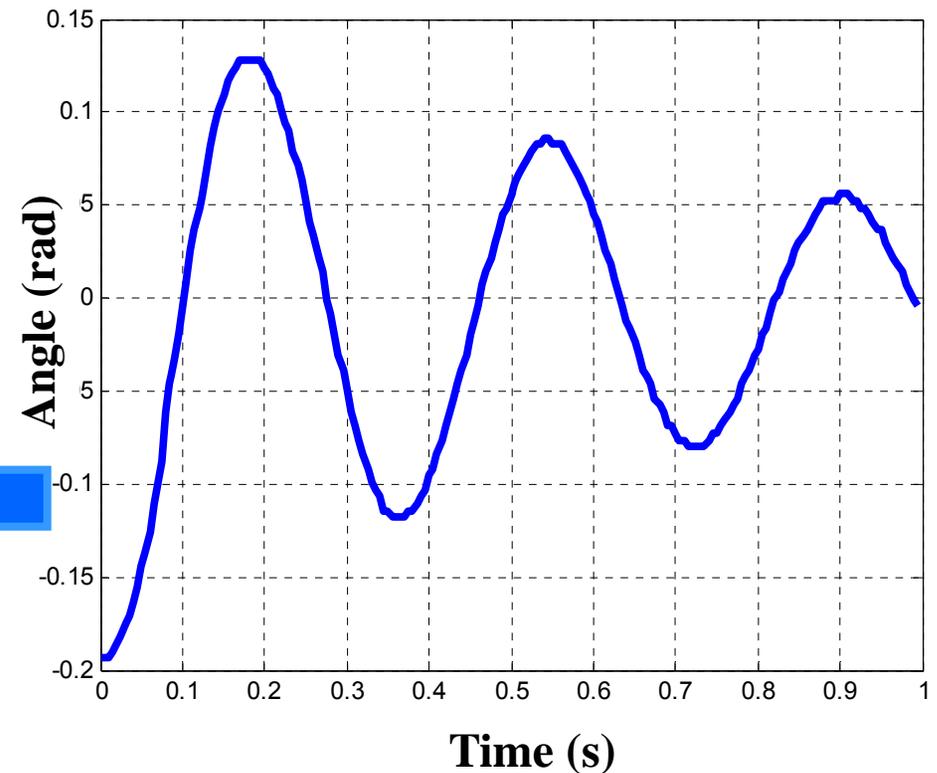


Fixed frequency sinusoidal reference

Desired link trajectory: $\theta_L = A \sin(2\pi f t)$ [fixed frequency]

Parameter	Value
I_M	0.35 (Kgm ²)
I_L	0.1 (Kgm ²)
M	1 (Kg)
L	0.34 (m)
f	2.5 (Hz)
A	0.2 (rad)

$$K = 4\pi^2 f_n^2 (I_L + ML^2) = 51.8 \text{ Nm/rad}$$

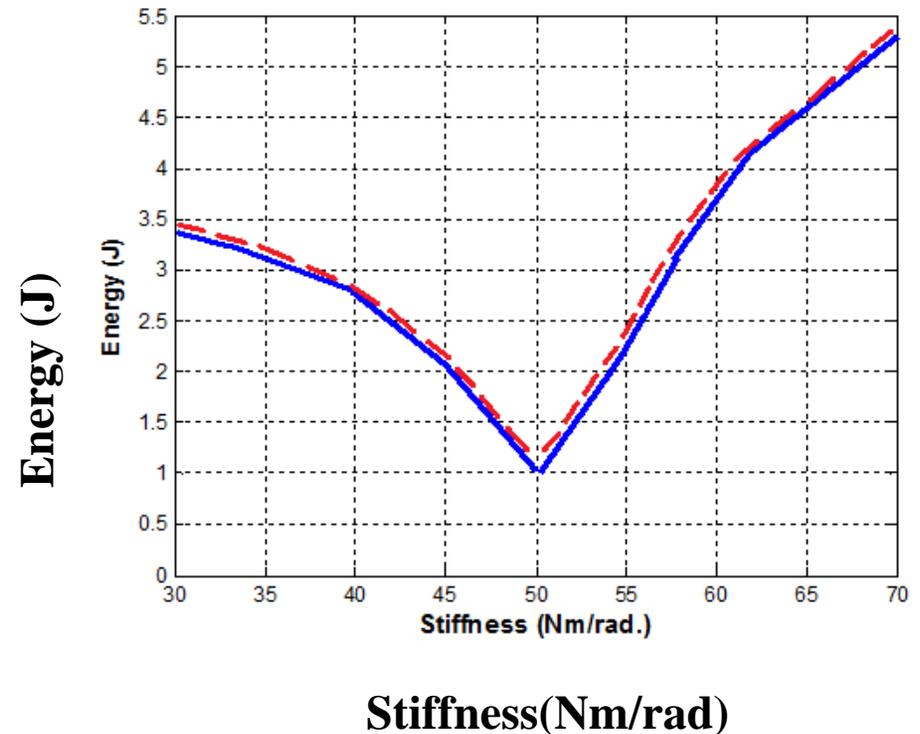


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f	2.5 (Hz)
A	0.2 (rad)

$$K = 4\pi^2 f_n^2 (I_L + ML^2) = 51.8 \text{ Nm/rad}$$



Fixed frequency sinusoidal reference



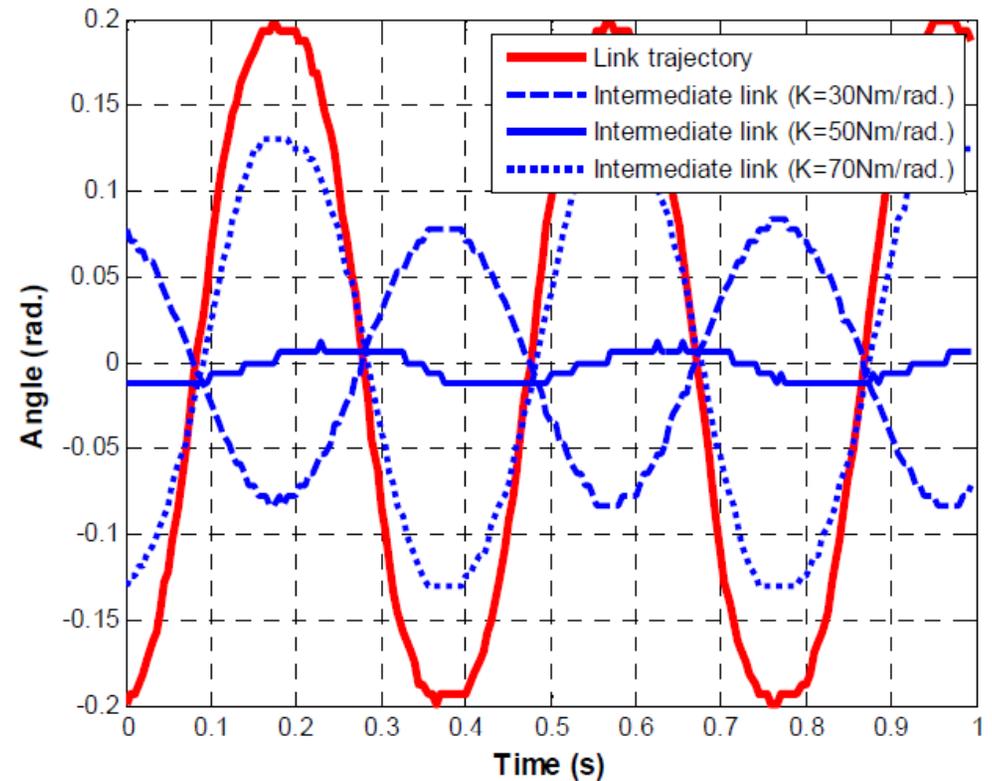
K=30 [Nm/rad]



K=50 [Nm/rad]



K=70 [Nm/rad]



Varying frequency sinusoidal reference

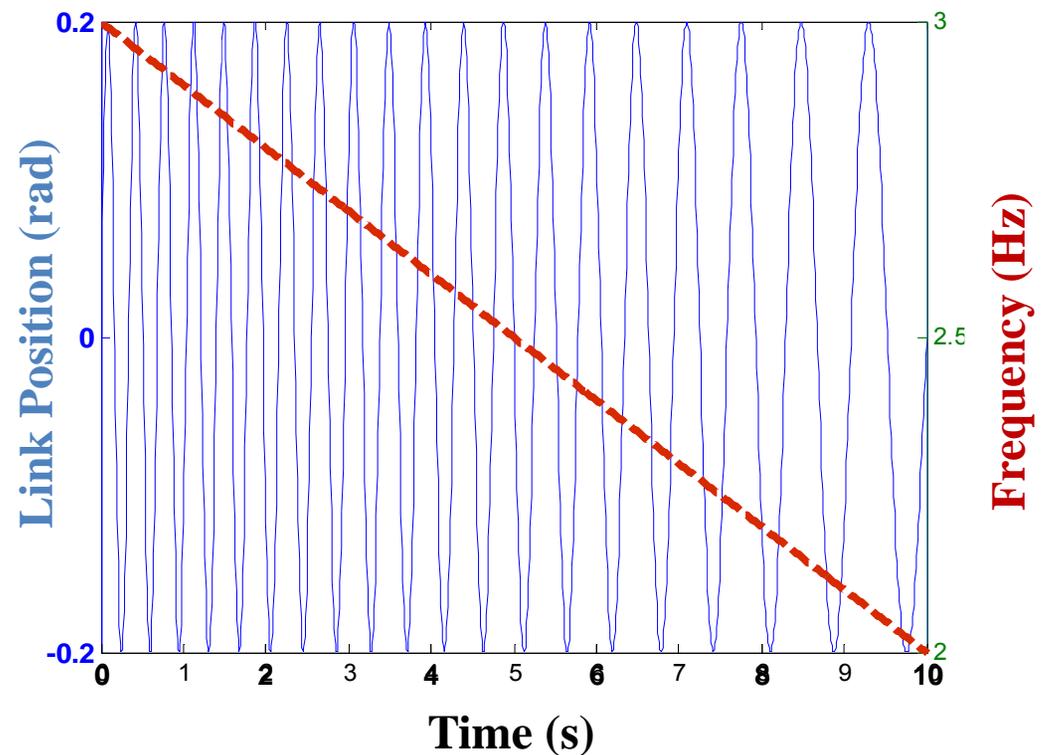
Desired link trajectory: $\theta_L = A \sin(2\pi ft)$ [Variable frequency]

Strategy 1:

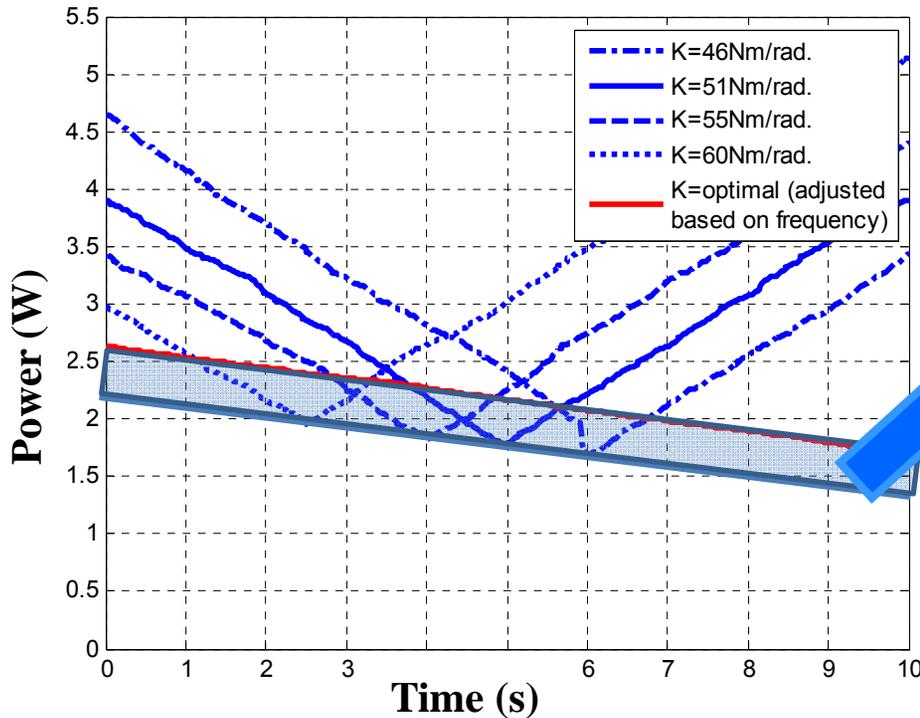
Set the stiffness to a fixed optimum value

Strategy 2:

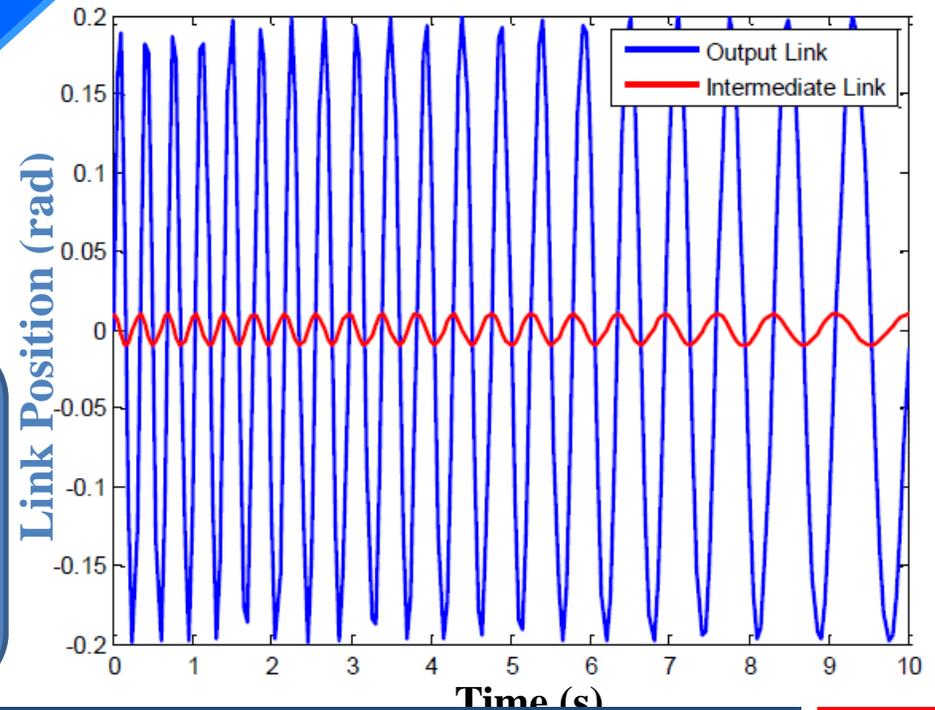
Tune the stiffness based on the frequency in real time



Varying frequency sinusoidal reference

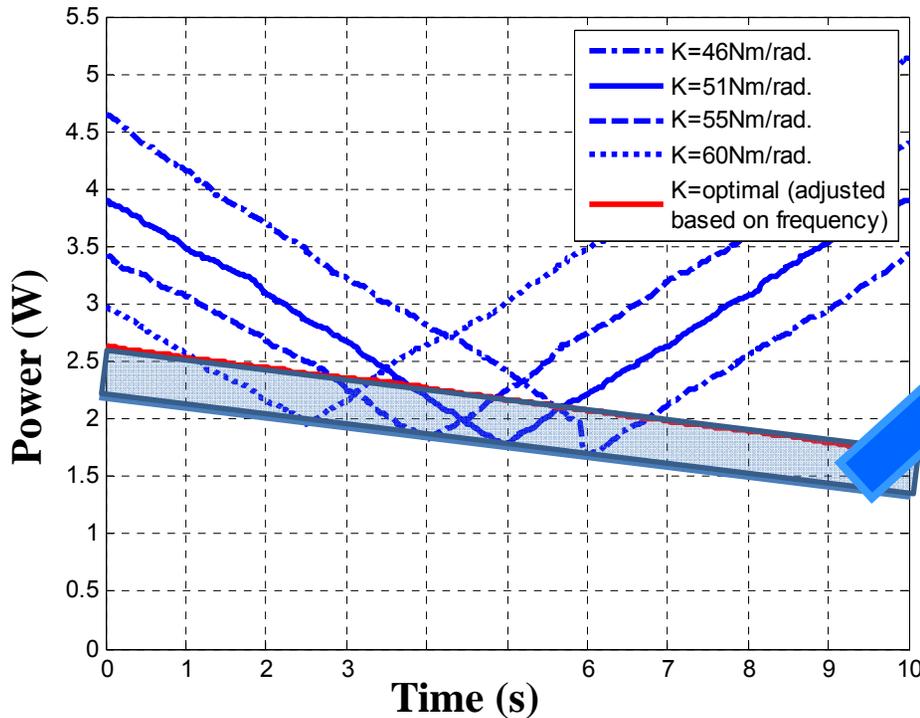


Energy consumption of the stiffness motor



Energy Consumption:
1st Strategy: 28.6J
2nd Strategy: 21.3J
[25% less than first strategy]

Varying frequency sinusoidal reference



Energy consumption of the stiffness motor

Jafari et al., ICRA 2011

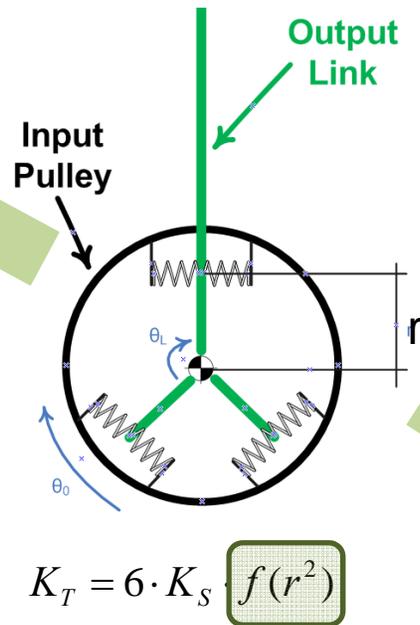
Energy Consumption:
1st Strategy: **28.6J**
2nd Strategy: **21.3J**
[25% less than first strategy]



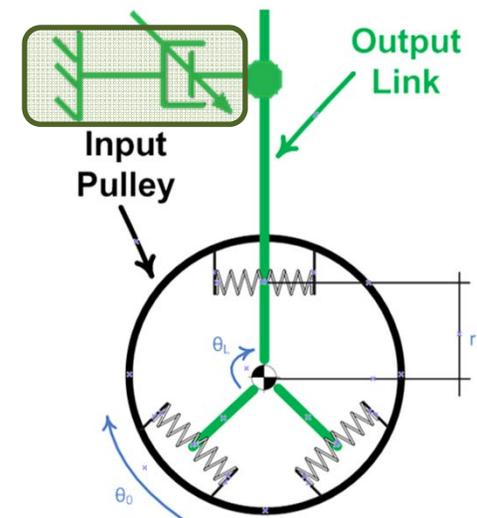
From CompAct to CompAct-VSA



Fixed stiffness joint



Variable damper



Stiffness and damping regulation in humans

- Humans improve accuracy and motion control by varying the stiffness and damping of the joints to appropriate values
- **Large amplitude oscillations:**
 - muscles co-contraction
 - damping $\uparrow\uparrow$
 - stiffness $\uparrow\uparrow$
- **Low amplitude oscillations:**
 - Intrinsic damping of muscles $\uparrow\uparrow$
 - low energy expenditure
- **Voluntary motions**
 - damping, stiffness inverse
 - function of velocity

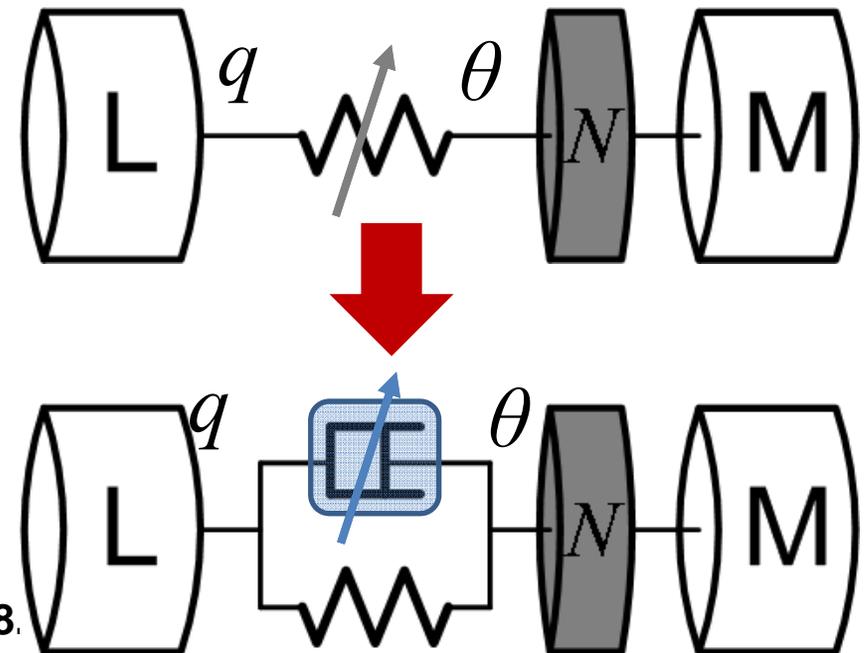
Elbow flex-extension

(Lacquaniti et al, '82)

$$C = [0.22 - 1.56] \text{ [Nms/rad]}$$

$$\zeta = [0.08 - 0.2]$$

$$K = [14.8 - 125] \text{ [Nm/rad]}$$



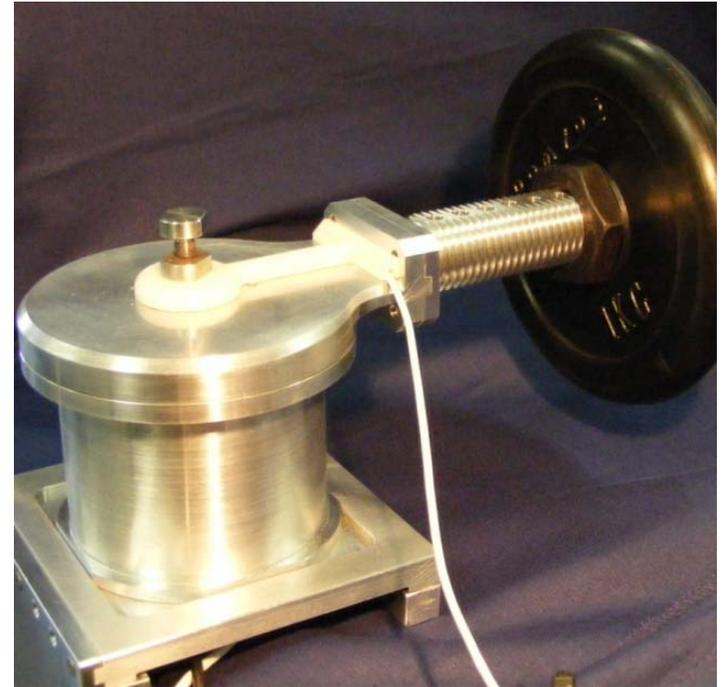
Milner and Cloutier, *Exp. Brain Research*, 1998.

Motivation

- facilitates control
 - inherently damps vibrations
 - reduces control effort
 - Intrinsically passive
- improve dynamic performance
- Spring energy management

Principle & Features

- semi-Active Solution
- introduces “real” physical damping
- piezoelectric actuation



SEA + Variable physical damping actuator

VPDA

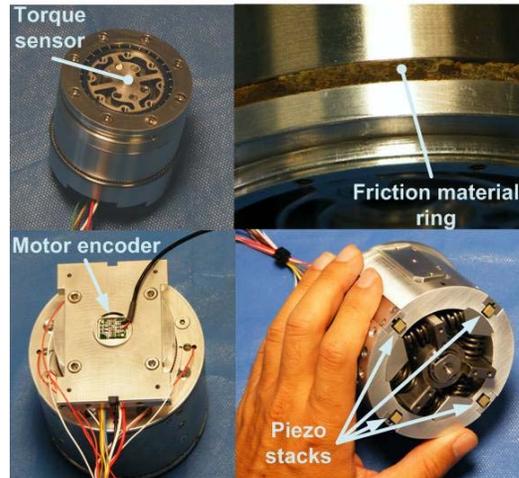
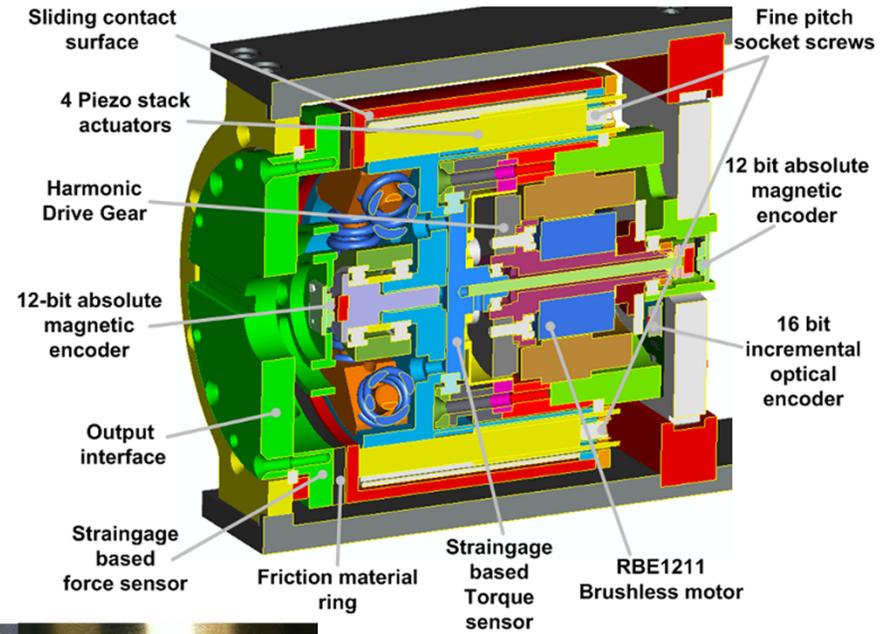
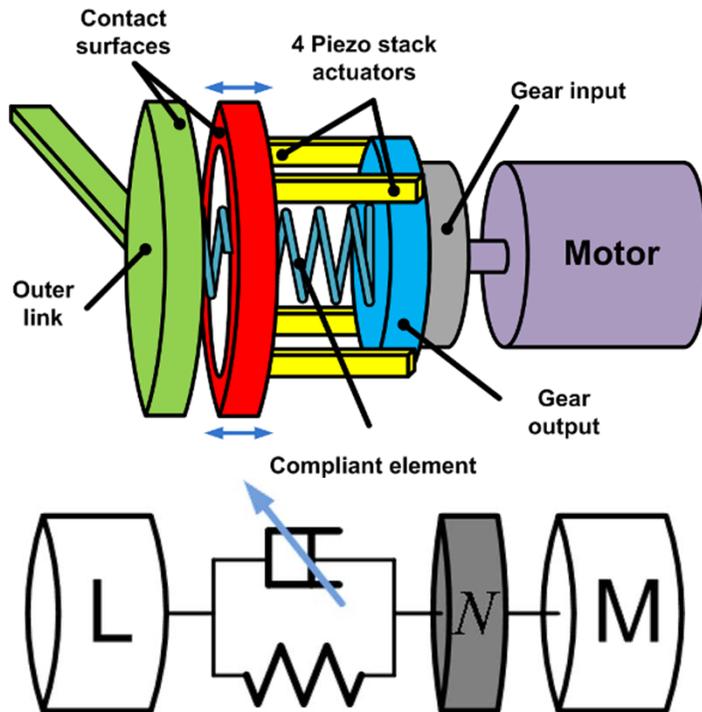


+

SEA

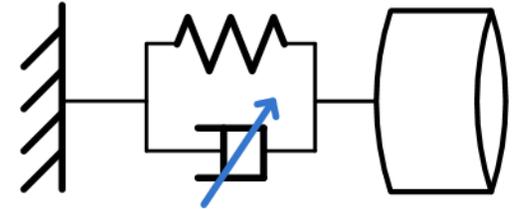


Lafranchi et al. ICRA 2010

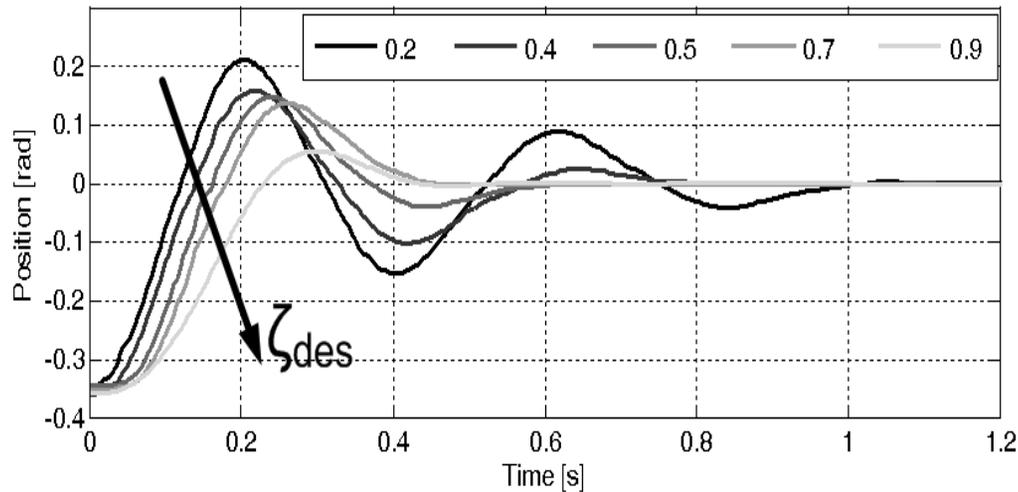


Mass-spring-damper system

- Damping ratio
- Free response to initial conditions

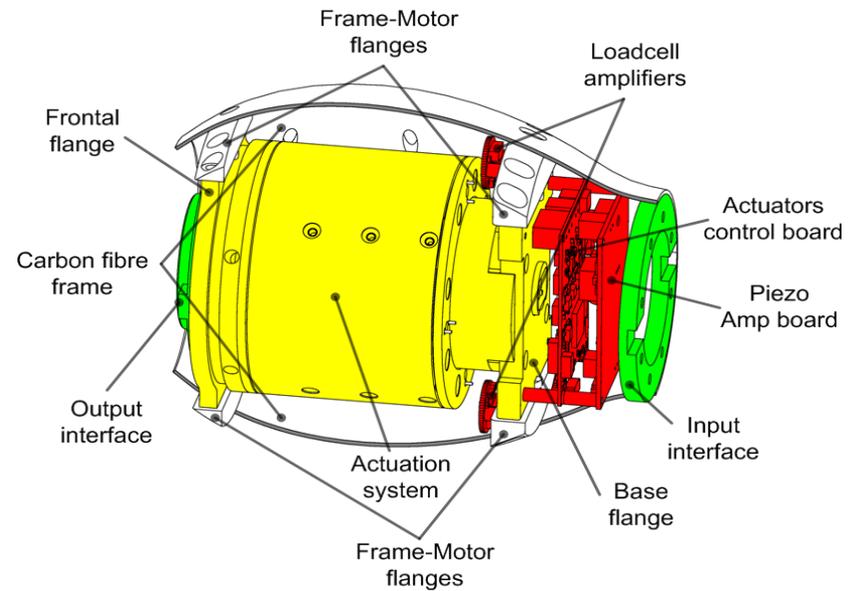
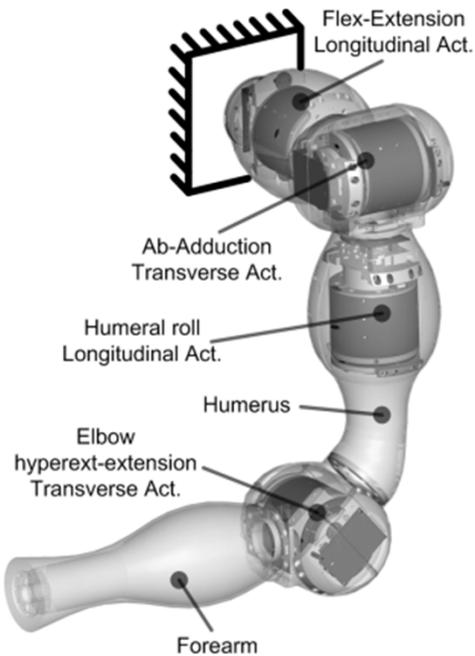
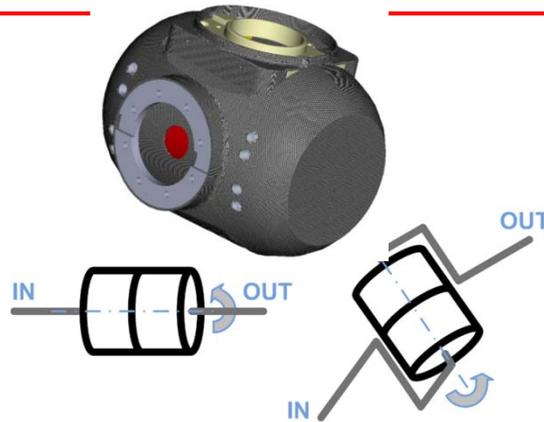


Experimental setup

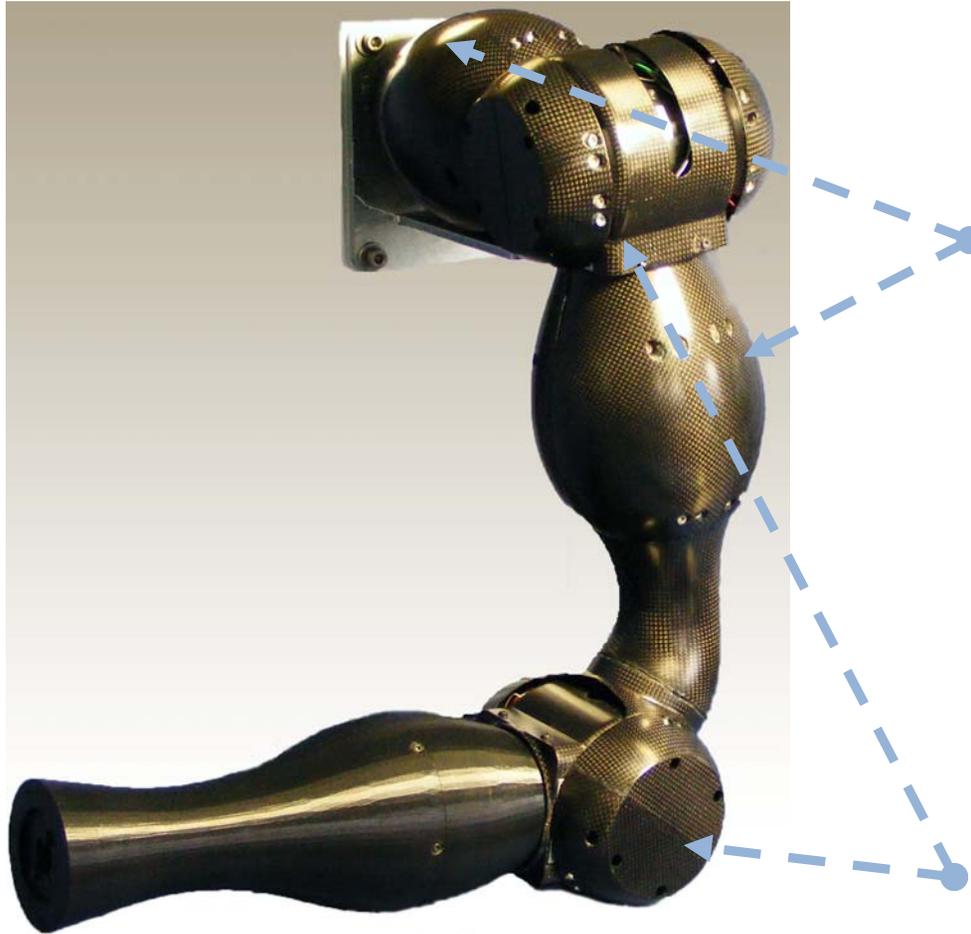


The Role of
Physical Damping
in Compliant Actuation Systems

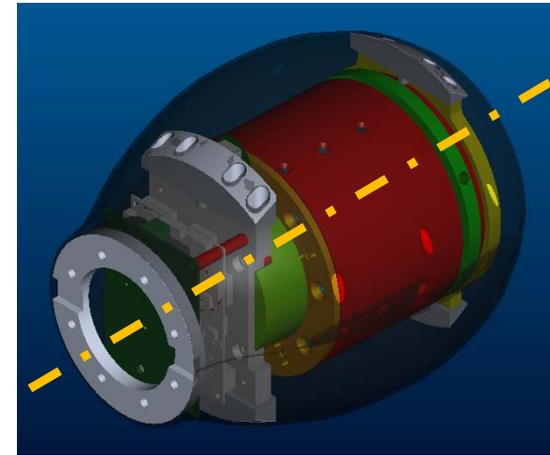
CompAct-VPDA Manipulator



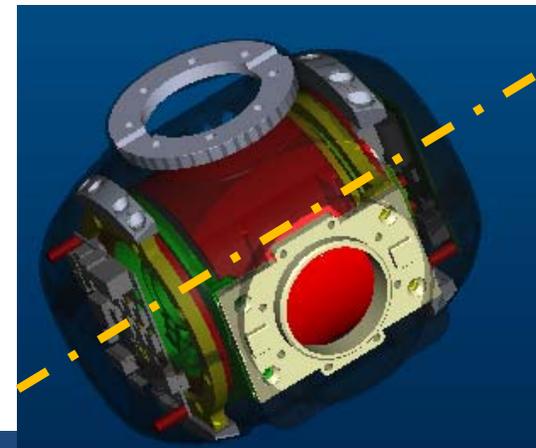
CompAct-VPDA Manipulator



LONGITUDINAL



TRANSVERSE



M. Laffranchi, N.G. Tsagarakis, Darwin G. Caldwell. **CompAct™ Arm: a Compliant Manipulator with Intrinsic Variable Physical Damping**. Robotics: Science and Systems VIII (RSS 2012), Sydney, Australia.

CompAct-VPDA Manipulator



CompAct-VPDA Manipulator

